Lean Six Sigma Black Belt

Using JMP Software

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2.	Basic Statistics and Statistical Graphics
3.	Fitting and Using Distributions
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5.	Analyzing Life Data
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Lean Six Sigma Black Belt, Volume II

Course outline with slide numbers

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Lean Six Sigma Black Belt Volume II

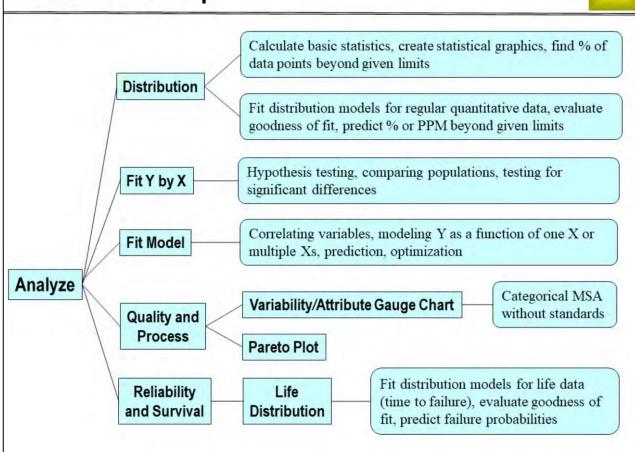
Tab 1 Statistical Analysis Graphs

Presented by



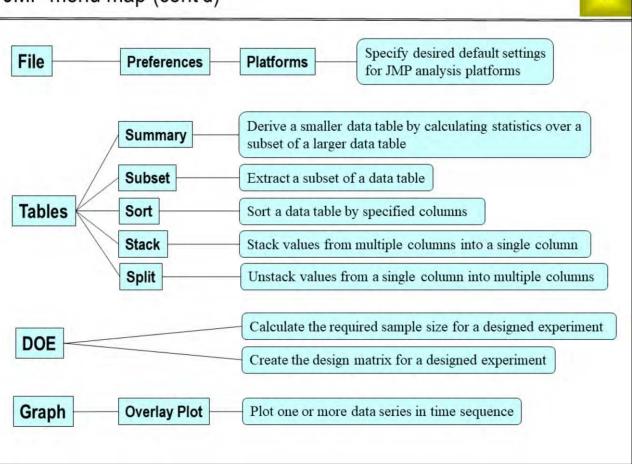
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1 JMP menu map



Notes			

JMP menu map (cont'd)



Notes			

2 Basic Statistics and Statistical Graphics

- · Frequency histogram
- · Cumulative distribution function
- · Percentiles
- · Box and whisker plot
- · JMP distribution analysis
- · Data validation
- · Distribution analysis options
- · Plotting data in time sequence
- · Saving analyses and data tables

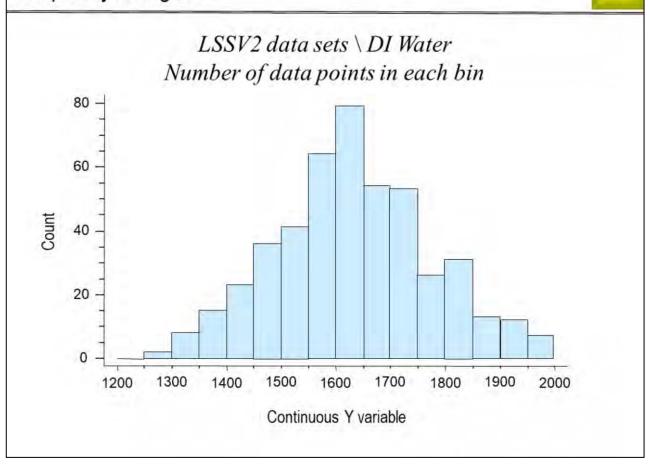
Notes		

Y variables are characteristics of parts or transactions that determine customer satisfaction, or lack thereof. They provide the data from which project metrics are computed. In sections 2 and 3 we focus on *quantitative* Y variables. Examples include:

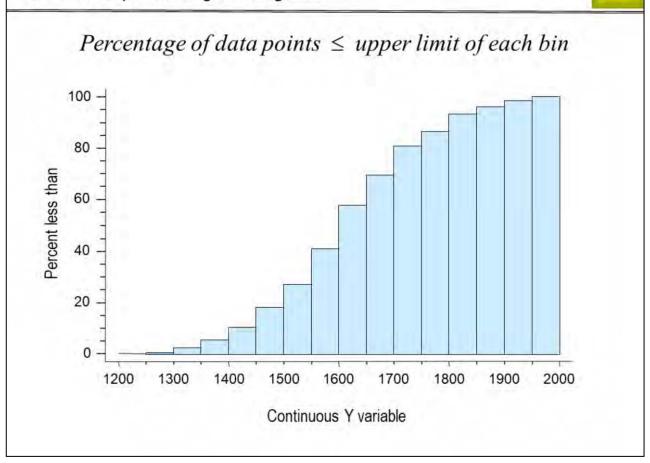
- · Properties: physical, chemical, electrical, optical, . . .
- · Distance, time, dimensions, cost, quantity
- Event counts (when there is not a discrete number of opportunities for the event to occur)

JMP uses the term *continuous* for quantitative variables, and often uses the term *nominal* for categorical variables.

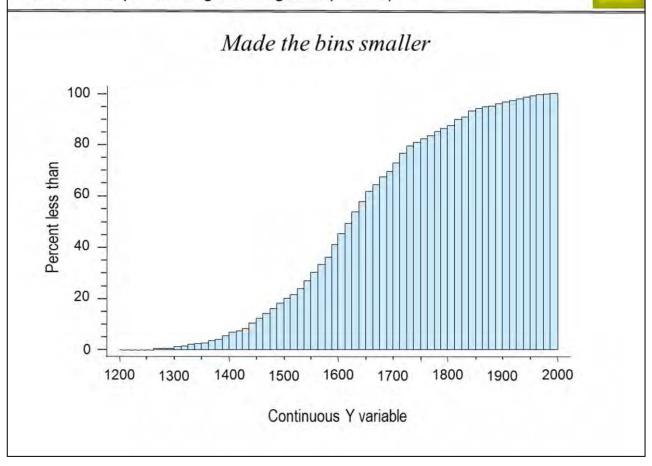
Notes			



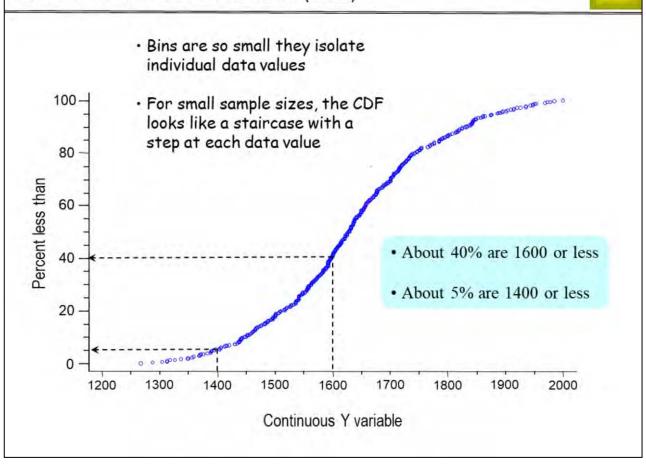
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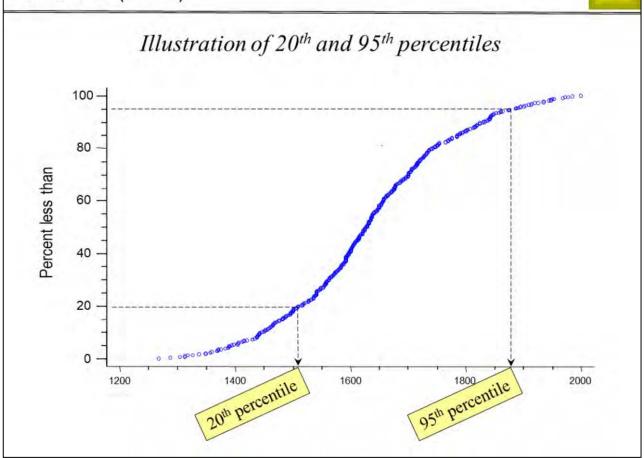
Notes			

Percentiles

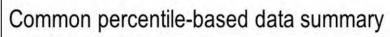
A *percentile* is a value that divides a population or data set into two groups, based on a stated percentage

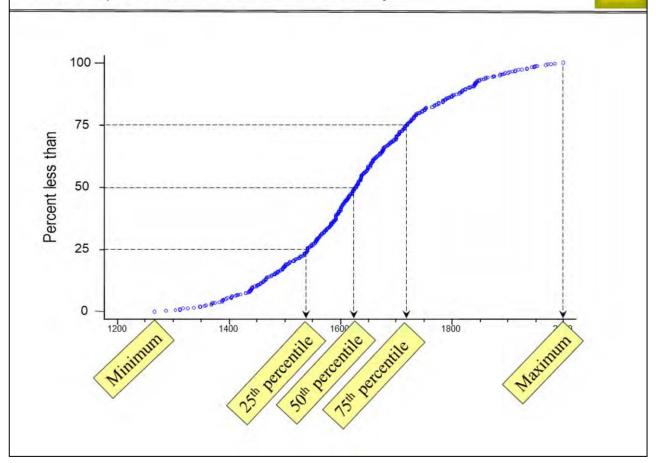
10% are less than the 10th percentile, 90% are greater 25% are less than the 25th percentile, 75% are greater 50% are less than the 50th percentile, 50% are greater 75% are less than the 75th percentile, 25% are greater 90% are less than the 90th percentile, 10% are greater

Notes		

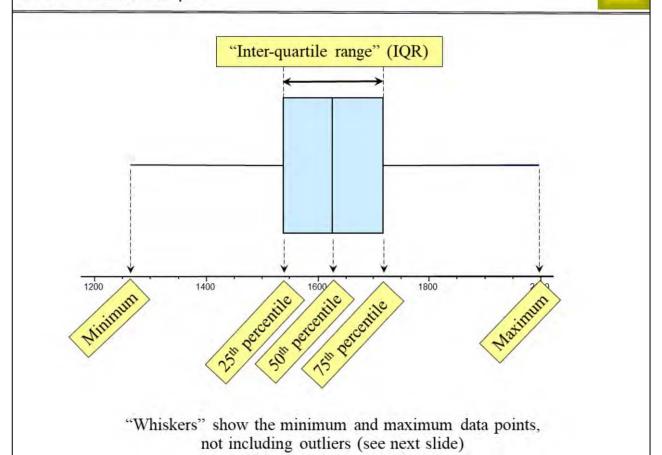


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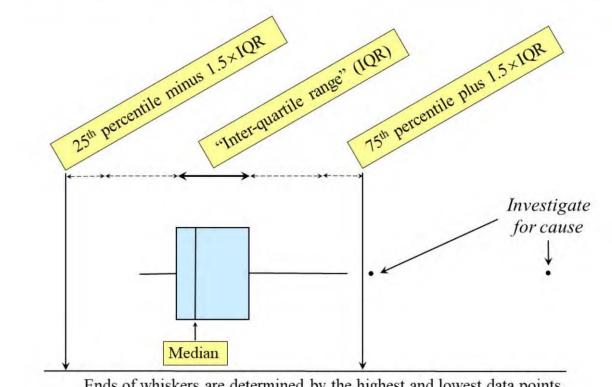




Notes				



Notes		



Ends of whiskers are determined by the highest and lowest data points that are inside the calculated ranges.

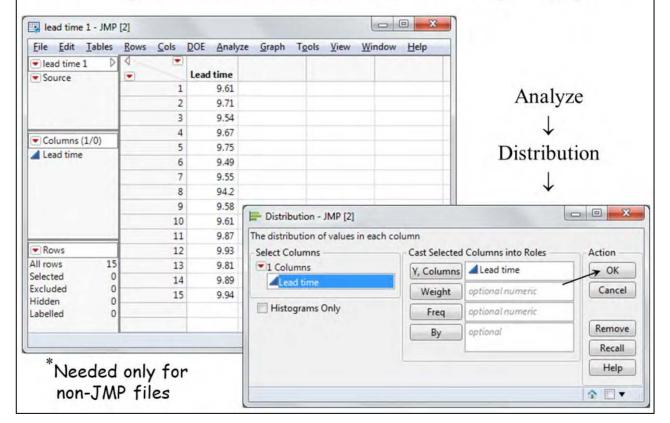
Points plotted separately are outliers, and should be investigated.

Notes			

JMP distribution analysis

Notes

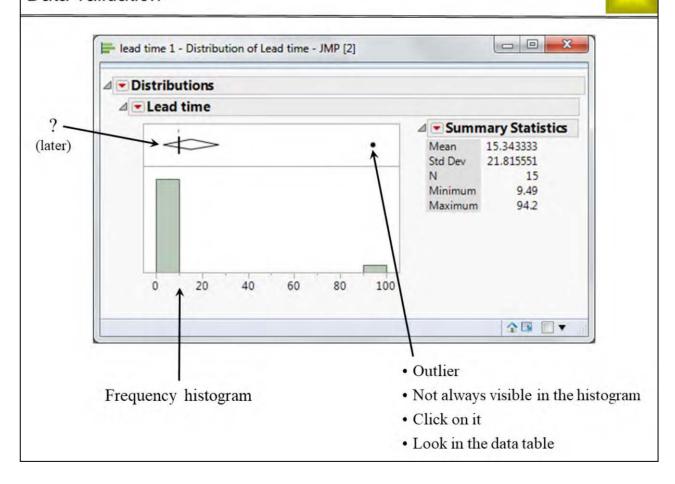
 $File \rightarrow Open \rightarrow All \ Files \rightarrow Data \ sets \setminus lead \ time \ 1 \rightarrow Open \rightarrow Import^*$



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Data validation

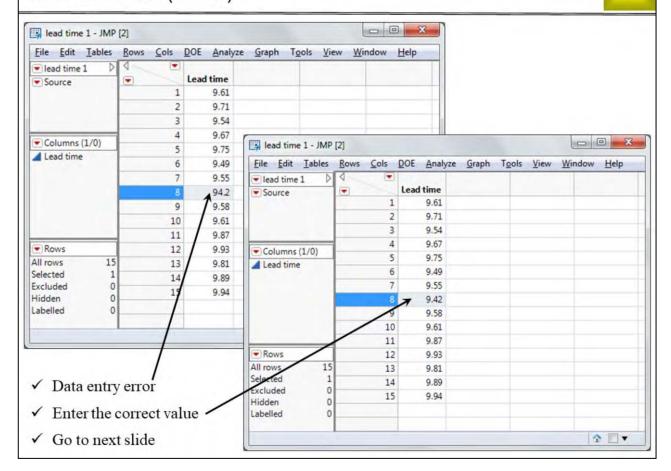
TAT 4



Notes			

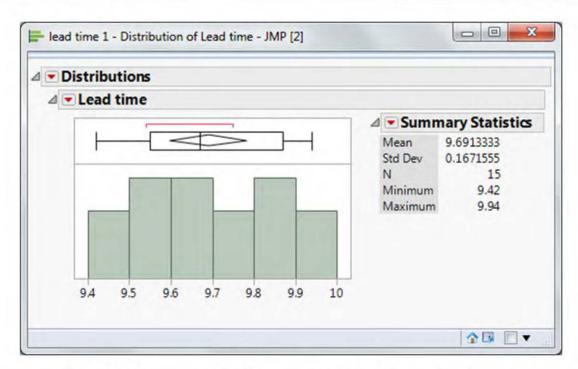
Data validation (cont'd)

TAT 4



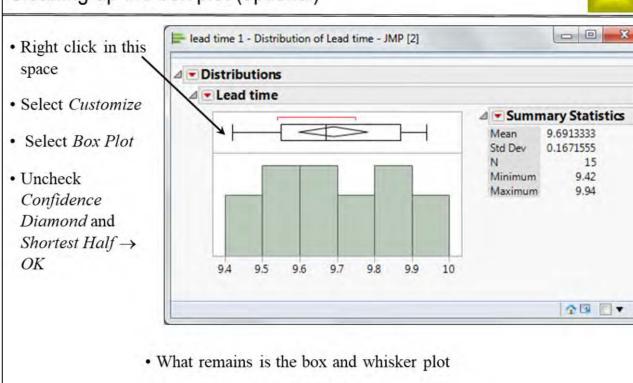
Notes			

Distribution analysis with data correction



Note the change in the histogram and the summary statistics

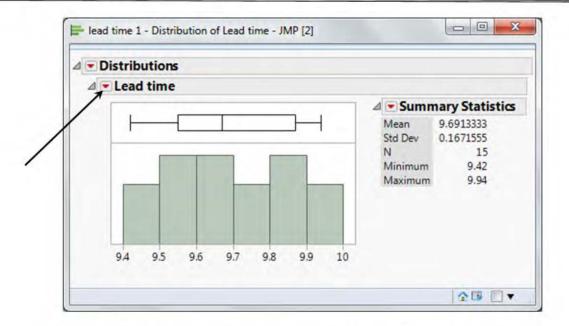
Notes			



• JMP calls it *Outlier Box Plot* because its main purpose in this context is to show outliers

Notes		

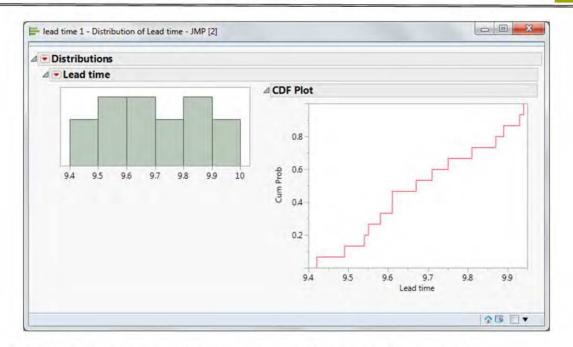
Distribution analysis options



- Click on the red triangle next to Lead time while holding down the Alt key
- This will show the default analysis options for the Distribution platform
- · See next slide

Notes			

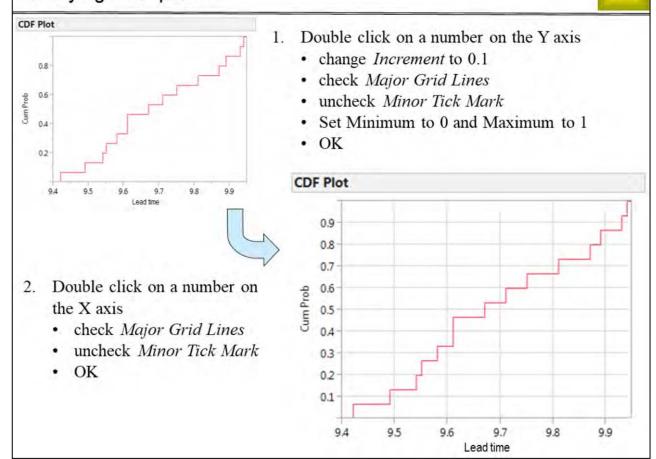
Cumulative distribution function (CDF plot)



- Plots the proportion of data points ≤ each value in the data set
- The step size at each data value is usually 1/N, where N is the sample size
- If the same value occurs twice in the data set, the step size there is 2/N

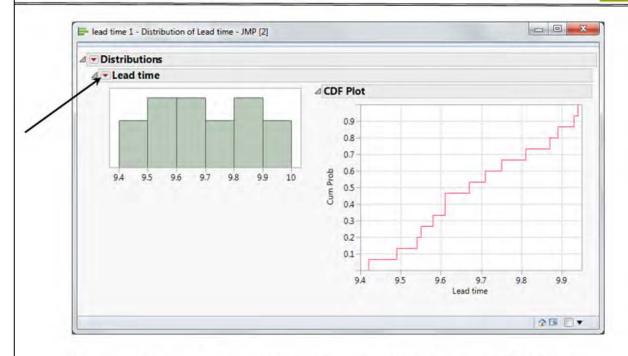
Notes			

Modifying JMP plots



Notes			

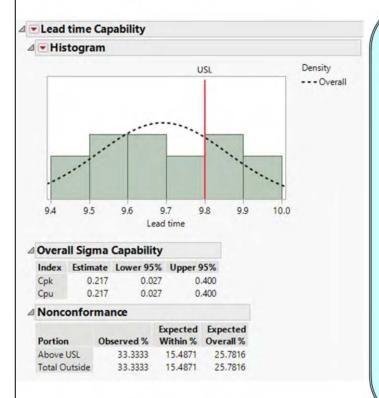
Calculating percentages



- · Suppose we want to know the percentage of data points exceeding 9.8
- Click the Lead time red triangle → select Process Capability
- Enter 9.8 for the Upper Spec Limit → click OK

Notes			

Percentages (cont'd)



Nonconformance shows:

- · Observed percent out-of-spec
- Expected (predicted), based on the Normal distribution

Capability indices are calculated:

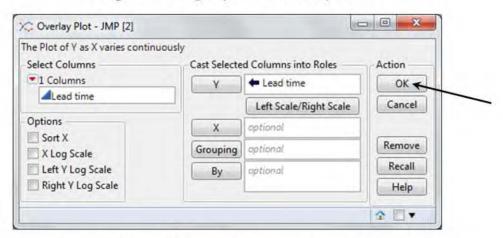
- Within Sigma Capability can be used when small samples are collected, such as for an Xbar-R chart
- Turn this off by clicking on the red triangle next to Lead time Capability
- Turn off the Within curve on the histogram by clicking on the red triangle next to Histogram

We will cover distribution fitting in the next section

Notes			

Plotting data in time sequence

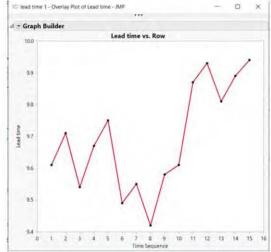
Graph → Legacy → Overlay Plot



- You can have different left and right scales for plotting multiple Y variables
 - Cast both Y variables into Y
 - o Select the one you want to display on the secondary (right) scale
 - o Click Left Scale/Right Scale.
 - o Arrows point to the Y-scale for each Y variable
- A date, time, or other sequencing variable could be cast into X

Notes			

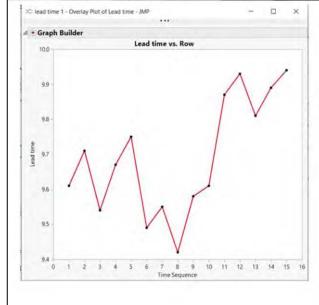




- · Modify the chart as follows:
 - Double Click X-Axis: Minimum = 0, Maximum = 16, Increment = 1, Dec = 0
 - Double Click on Y-Axis: Minimum = 9.4
 - Right Click on Chart: Customize > Line > Line Color > Red
 - Double Click on X-Axis Title: Change "Row" to "Time Sequence"

Notes			

Overlay plot (cont'd)



- Good way to look for assignable cause patterns versus their time sequence
- · Same as a line chart in Excel
- Overlay plot can be used to display different data sets on different Y-Axis

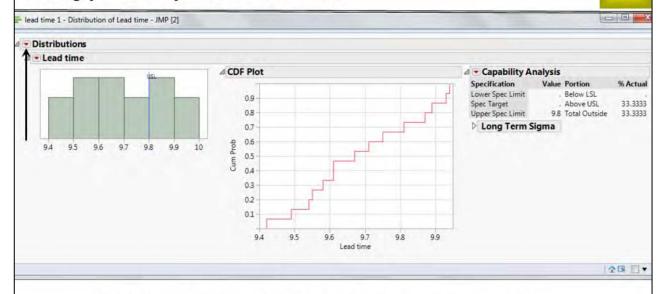


he Plot of Y as X varies cont	inuously		
Select Columns	Cast Selecte	d Columns into Roles	Action
1 Columns	Y	📜 🥒 Lead time	OK
Lead time		Left Scale/Right Scale	Cancel
Options	X	optional	
☐ Sort X	Grouping	optional	Remove
☐ X Log Scale ☐ Left Y Log Scale	Ву	optumal	Recall
Right Y Log Scale			Help

Notes			

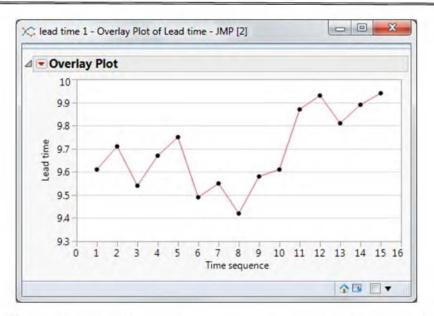
Saving your analyses and data table





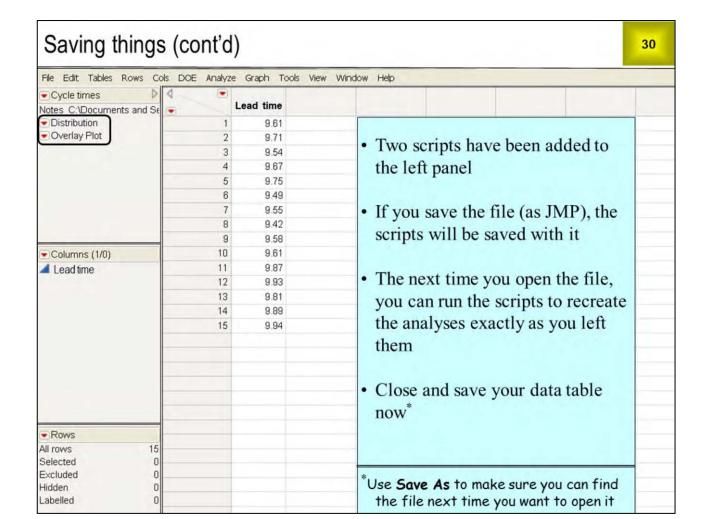
- Click on the thumbnail for the distribution analysis at the bottom of the data table
- Click the red triangle next to Distributions
- Save Script → To Data Table → Name: Distribution → OK

Notes			



- Click on the thumbnail for your overlay plot, click the red triangle next to *Overlay Plot*
- Save Script \rightarrow To Data Table \rightarrow Name: Overlay Plot \rightarrow OK
- Go to your data table

Notes			



Notes			

TAT 4

Open *Data sets* \ *quotation process*. Perform the following data analysis tasks for the variable *TAT* (turnaround time).

- (a) Run a distribution analysis. Note the large number of points plotted separately on the outlier box plot. This pattern is common with asymmetric "ski slope" distributions that pile up near zero. These points are *not* assignable causes, so they would not be investigated or removed.
- (b) Record the average, standard deviation, sample size, minimum, maximum and median.
- (c) Turn off the outlier box plot.
- (d) Find the % of data points exceeding 3.
- (e) Turn off the Within Sigma Capability.
- (f) Save your analysis script. Close and save the data table.

Notes			

Data sets \ DI water. Perform the following data analysis tasks for the variable Resistivity.

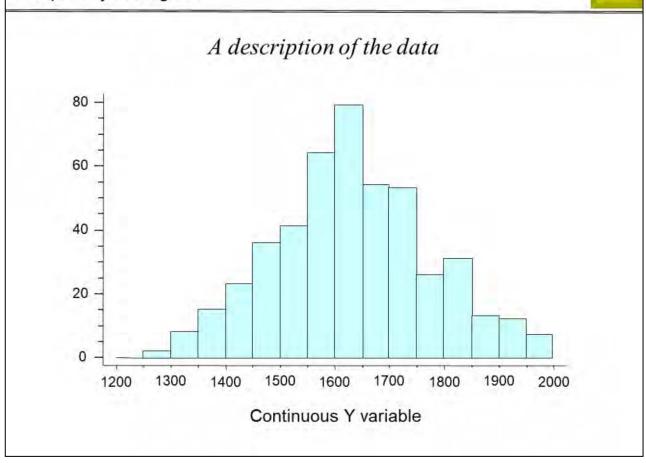
- (a) Create an overlay plot. You should see something that suggests bad data (stretch the graph if necessary). Use your mouse to draw a box around the suspicious data points. Right click in an uninhabited area of the plot, select Row Hide and Exclude.
- (b) Run a distribution analysis. Record the average, standard deviation, sample size, minimum, and maximum.
- (c) Turn off the outlier box plot.
- (d) Find the % of data points falling below 1500.
- (e) Turn off the Within Sigma Capability.
- (f) Save your analysis scripts. Close and save the data table.

Notes			

3 Fitting and Using Distributions

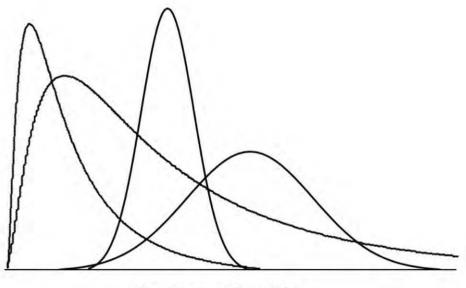
- · Distribution curves
- · Checking goodness of fit
- · JMP examples
- · Fitting and using the Normal distribution
- · Fitting and using the Lognormal distribution
- Finding the best fitting distribution(s)
- Using the best fitting distributions(s)

Notes			



Notes			

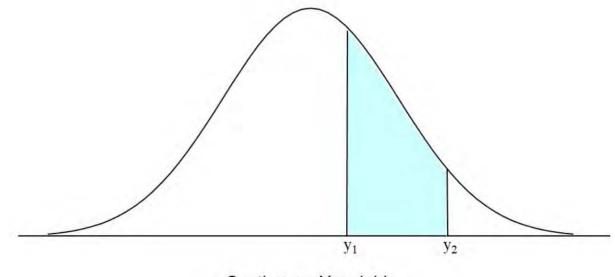
Possible descriptions of the population



Continuous	Υ	varia	bl	e
	- 75			

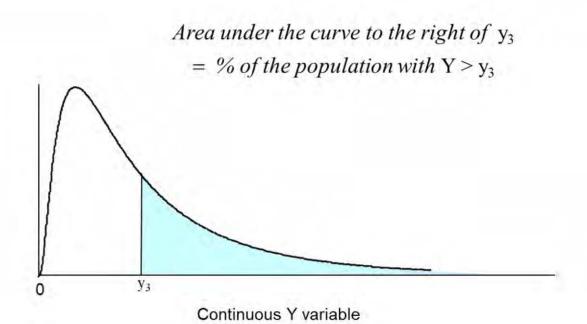
Notes			

Area under the curve between y_1 and y_2 = % of the population with $y_1 < Y \le y_2$

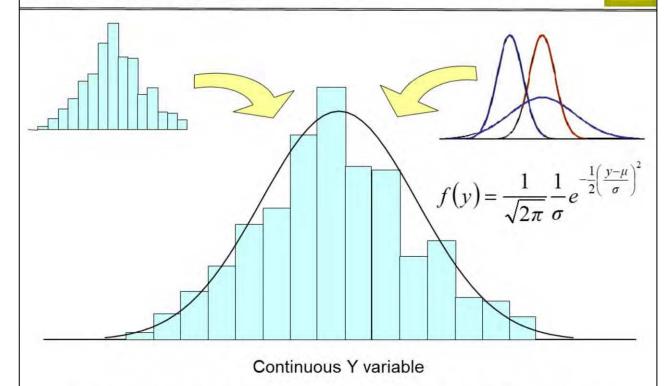


Continuous Y variable

Notes			

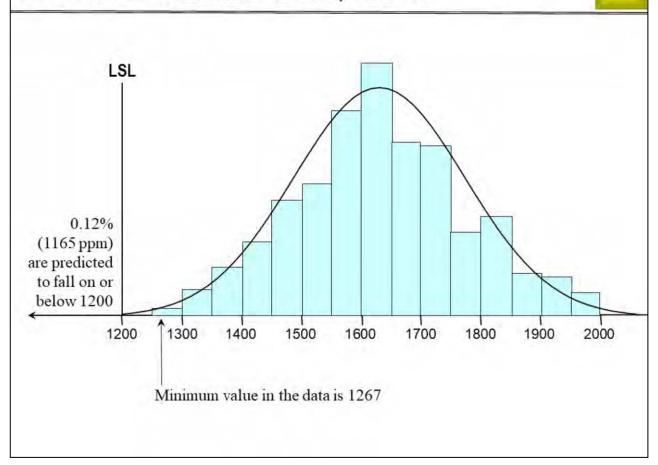


Notes				



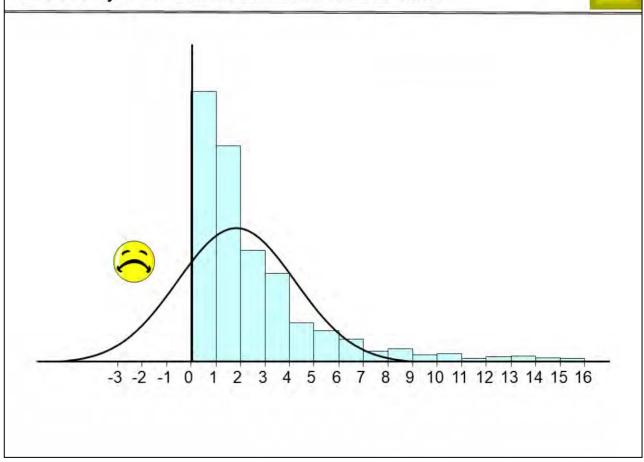
- The Normal curve depends only on μ and σ (population mean and std. dev.)
- Plug the sample mean and std. dev. into the formula in place of μ and σ

Notes		

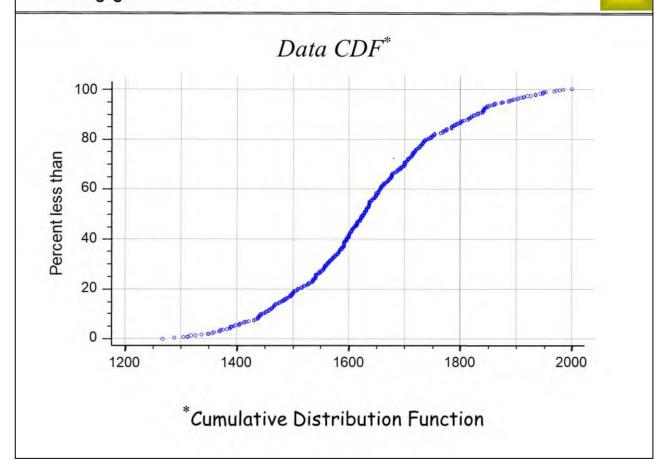


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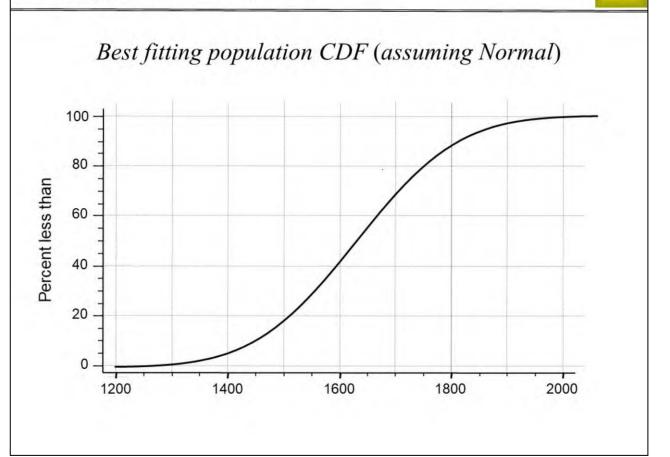
... but only if the distribution matches the data!



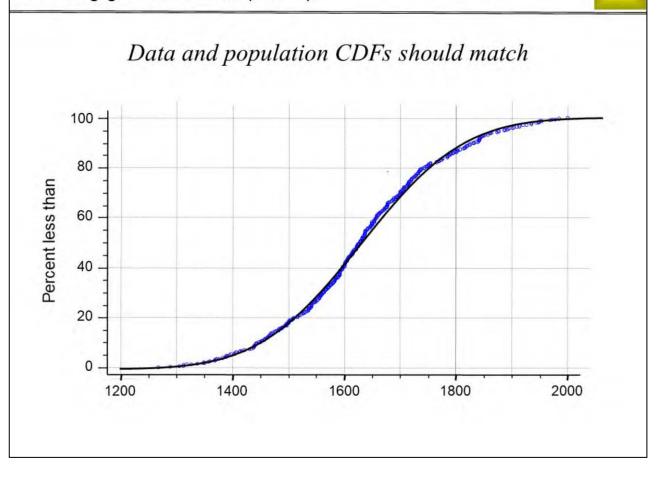
Notes		



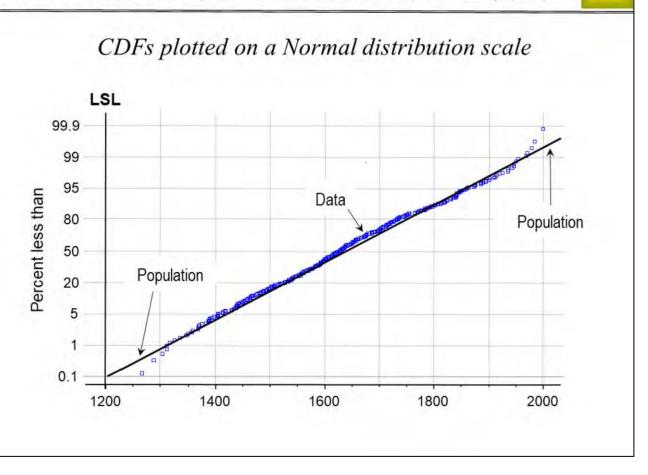
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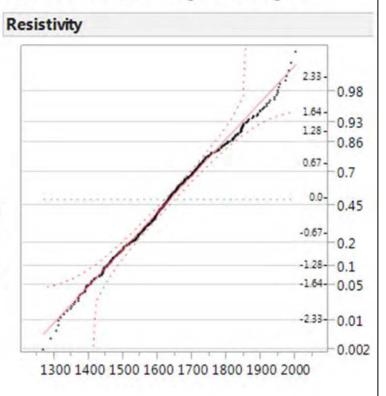


Notes			

JMP example: Normal data

$File \rightarrow Open \rightarrow Data\ sets \rightarrow DI\ water \rightarrow Open \rightarrow Import$

- Analyze → Distribution →
 Resistivity → Y, Columns → OK
- ▼Resistivity → Normal Quantile Plot
- Fit is good the points form a relatively straight line and stay within the hyperbolic band
 - It is common for the data to curve up a little at the top and down a little at the bottom of the Normal Quantile Plot
 - A curve throughout the graph indicates non-normal data
- Save the script to the data table
- File save as $\rightarrow DI$ water.jmp
- · Leave the data table open

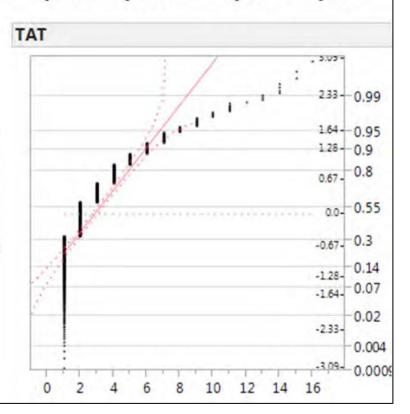


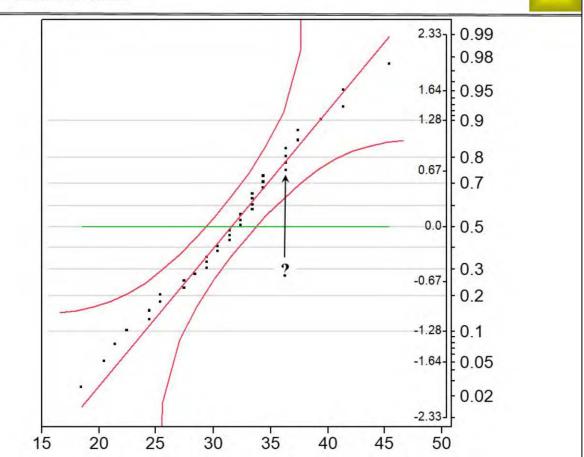
Notes			

$File \rightarrow Open \rightarrow Data\ sets \rightarrow quotation\ process \rightarrow Open \rightarrow Import$

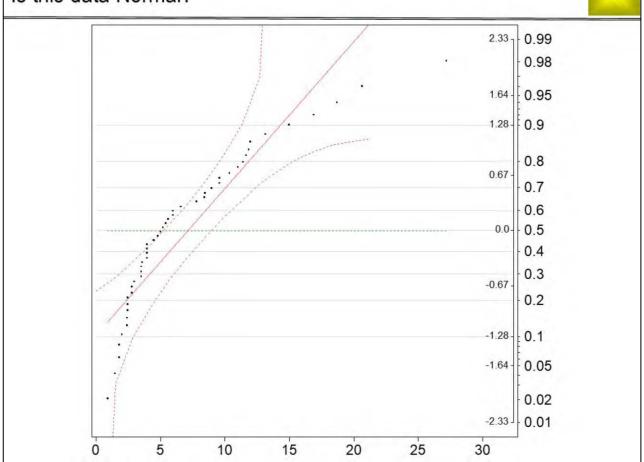
- Analyze \rightarrow Distribution \rightarrow Y, Columns \rightarrow $TAT \rightarrow$ OK
- Distributions → Stack
- $TAT \rightarrow Normal Quantile Plot$
- Fit is bad the points do not follow the line and do not stay inside the hyperbolic band
- · Save the script to the data table
- File save as → quotation process.jmp
- · Close the data table

Notes





Notes			



Notes			

Fitting and using the Normal distribution

- · Go to DI water.jmp
- The values of *Resistivity* in rows 205 to 214 are constant at 1454
- These are not true measurements, so we use the red triangle to hide and exclude the questionable values
- This reduces the sample size from 474 to 464
- · Next slide:

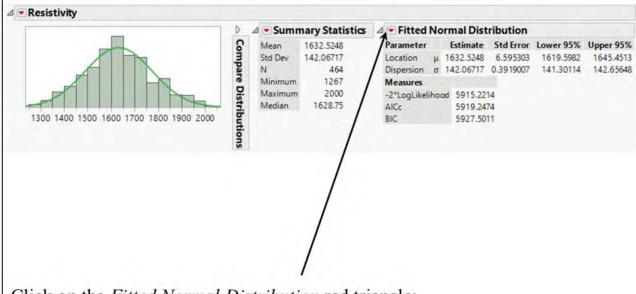
Notes

- Analyze → Distribution
- Red Triangle → Continuous Fit
- → Fit Normal

File Edit Tables	Rows Cols [OE Ar	alyze G	raph T <u>o</u> ol
▼ DI water ▷ ▶ Source	√	Day	Hour	Resistivity
	202	4-F	9	1389.0
_ /	203	4-F	9	1552.0
~	204	4-F	9	1616.0
/	⊘ € 205	4-F	10	1454.0
Columns (3/0)	⊘ € 206	4-F	10	1454.0
d Day	⊘ ≈ 207	4-F	10	1454.0
▲ Hour	⊘ € 208	4-F	11	1454.0
Resistivity	⊘ € 209	4-F	11	1454.0
	⊘ € 210	4-F	12	1454.0
	⊘ € 211	4-F	12	1454.0
	⊘ € 212	4-F	12	1454.0
	⊘ € 213	4-F	13	1454.0
	⊘ € 214	4-F	13	1454.0
Rows	215	4-F	14	1625.0
All rows 474	216	4-F	14	1563.0
Selected 10	217	4-F	14	1642.5
Excluded 10 Hidden 10	218	4-F	15	1857.0
Labelled 0	219	4-F	15	1516.5
	220	4-F	15	1748.0

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Normal distribution (cont'd)

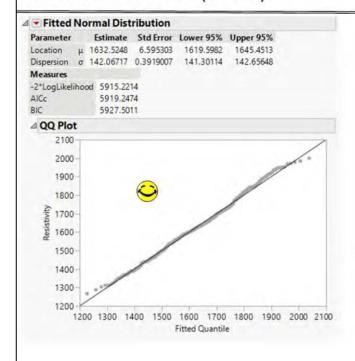


Click on the Fitted Normal Distribution red triangle:

- → Select Diagnostic Plots → QQ Plot
- → Next slide

Notes			

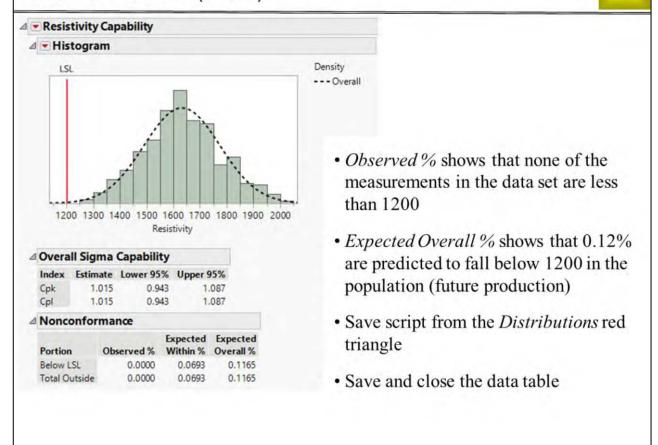
Normal distribution (cont'd)



- The QQ Plot is similar to the Normal Quantile Plot
 - When the distribution is a good fit, the data will fall in a line on the plot
- Click on the Fitted Normal Distribution red triangle again:
 - → Select Process Capability
 - → Enter 1200 for *Lower Spec Limit* → OK
 - → Next slide

Notes			

Normal distribution (cont'd)



Notes			

What if the Normal distribution isn't a good fit?

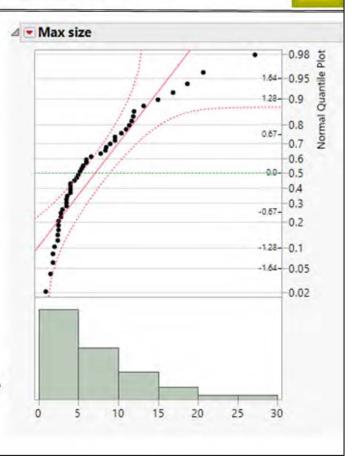
Steps for fitting a distribution to data:

- 1. Analyze \rightarrow Distribution
 - · Check Normal Quantile Plot—data in straight line indicates good fit
 - If uncertain: Continuous Fit → Fit Normal
 - ▼Fitted Normal Distribution → Goodness of Fit
 - Anderson-Darling p-value > 0.05 indicates good fit
- 2. If Normal not a good fit: Continuous Fit \rightarrow Fit Lognormal
 - Fitted Lognormal Distribution → Diagnostic Plots → QQ Plot
 - Data in a relatively straight line on the QQ Plot indicates good fit
 - If uncertain: ▼Fitted Lognormal Distribution → Goodness of Fit
 - Anderson-Darling p-value > 0.05 indicates good fit
- 3. If Lognormal is not a good fit: Continuous Fit → Fit All
 - Check QQ Plot and view the curve on the histogram to make sure that the fit makes sense for the data.
 - Standard distributions are Weibull, Gamma, Normal, Lognormal, Exponential, Cauchy.
 - JMP offers other specialty distributions that often don't apply, so use caution with them (Johnson Sb, SHASH, Normal 2 Mixture, etc.)

Notes			

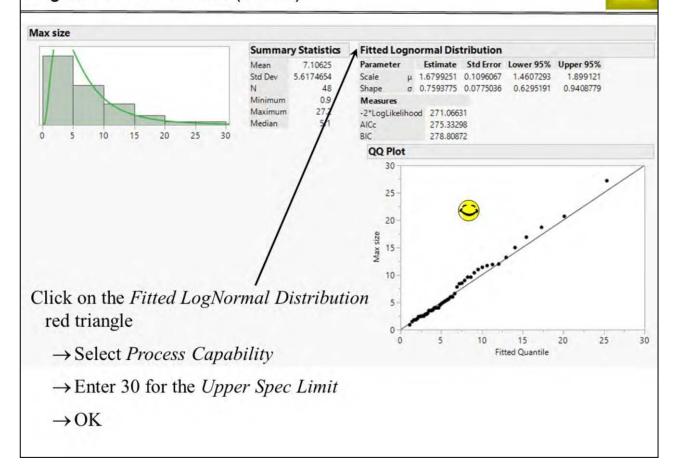
Fitting and using the Lognormal distribution

- Data sets → number & size of defects
- Analyze → Distribution → Max size
- · Max size is not Normal
- The *LogNormal* distribution is the most common alternative
- Red triangle Max Size
 - → Continuous Fit → Fit LogNormal
- Red triangle Fitted Lognormal Dist
 - → Diagnostic Plots → QQ Plot



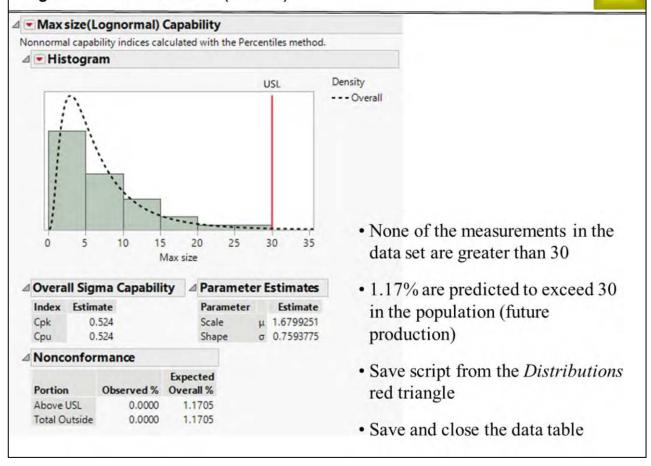
Notes			

Lognormal distribution (cont'd)



Notes			

Lognormal distribution (cont'd)



Notes			

Finding the best-fitting distribution(s)

△ 4/0 Cols 💌	Aligner	X dev	Y dev	R dev
1	1	-17	4	17.464249197
2	2	-7	6	9.2195444573
3	3	-10	-21	23.259406699
4	2	0	-1	1
5	2	-10	5	11.180339887
6	2	-7	0	7
7	3	-14	-15	20.518284529
8	2	-3	-17	17.262676502
9	2	-8	3	8.5440037453
10	2	-7	-8	10.630145813
11	1	-11	-6	12.529964086
12	2	-6	0	6
13	2	-7	5	8.602325267
14	3	-10	-5	11.180339887
15	2	-3	1	3.1622776602
16	2	-8	4	8.94427191
17	3	-16	-12	20
18	3	-16	-15	21.931712199
19	1	-14	3	14.317821063
20	2	-8	-8	11.313708499
21	3	-23	-2	23.086792761
22	3	-19	-15	24.207436874
23	2	-7	9	11.401754251
24	2	-10	0	10
25	2	-9	-5	10.295630141
26	1	-8	-11	13.601470509
27	2	-8	-3	8.5440037453
28	3	-16	0	16
29	1	-13	-21	24.69817807
30	3	-8	-4	8.94427191

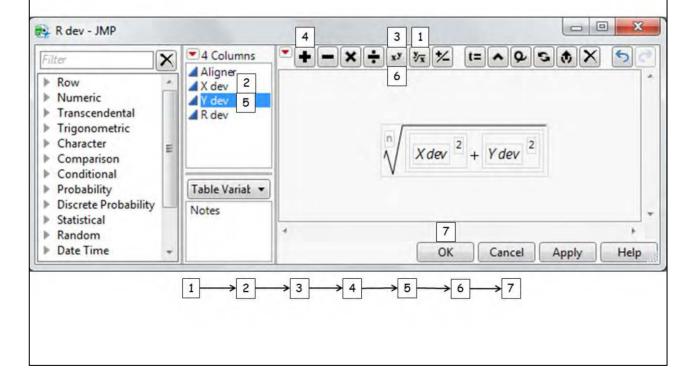
If neither the Normal or Lognormal are a good fit to the data, you'll need to find a better option.

- Data sets \ alignment process
- Three similar alignment tools are used to attach orifice plates to computer chips. Y dev and X dev are the vertical and horizontal deviations from target in mils.
- The alignment specification applies to the radial deviation calculated from X and Y. See slide below for the calculation of R dev.
- Analyze \rightarrow Distribution $\rightarrow R \ dev$
- · Remove:
 - √ Summary Statistics
 - ✓ Outlier Box Plot
- Red triangle (R Dev) → Continuous Fit → Fit All
- · Go to slide 61 to see the results

Notes			

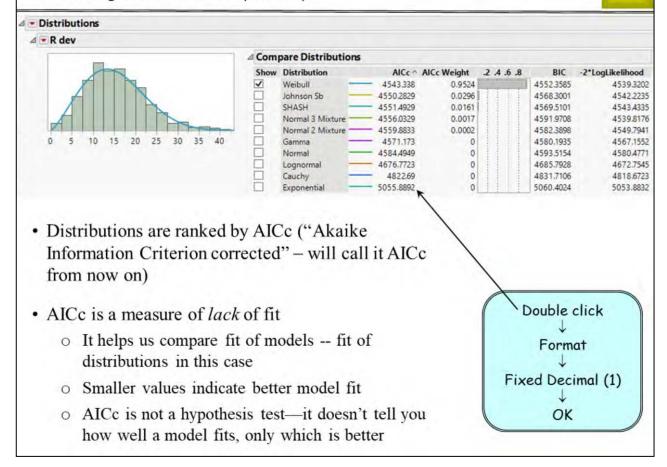
Using the formula tool

Double click on the blank column header next to *Y dev*, click on *Column 4*, rename as *R dev*. Click on *Column Properties*, select *Formula*, *Edit Formula*. Use your mouse to create the formula for *R dev* as shown below.

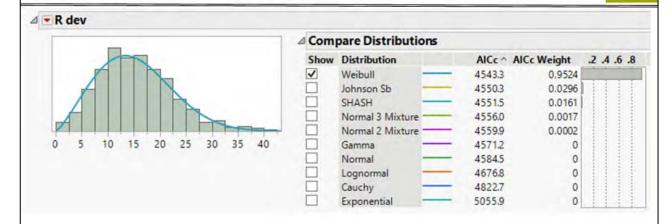


Notes		

Best-fitting distributions (cont'd)



Notes			

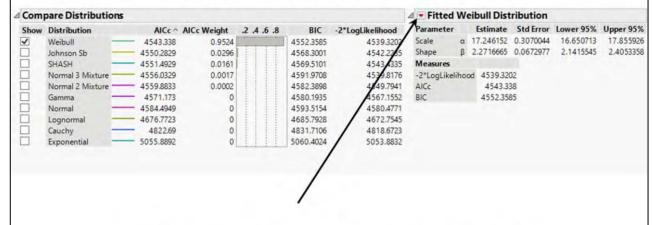


- Distributions with the same AICc (rounded to the nearest tenth) have the same lack of fit (or equivalently, the same goodness of fit)
- The distribution with the AICc Weight closest to one is the better fit

Notes			

Using the best-fitting distribution: Weibull

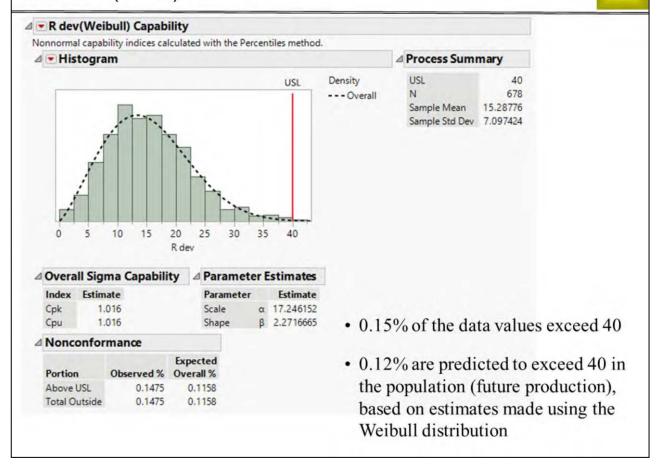
What % of future parts will have R dev > 40?



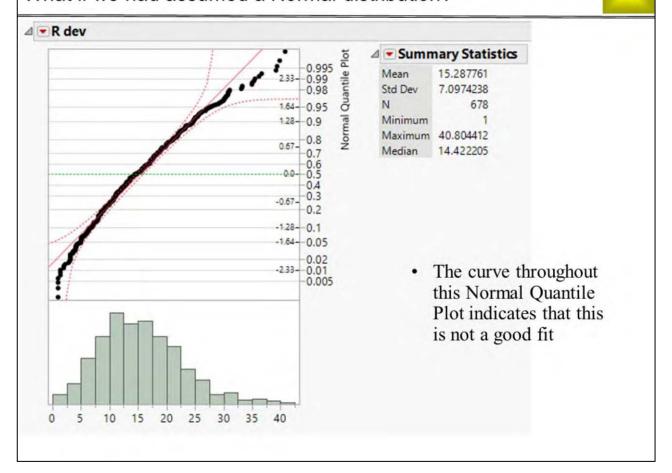
- Click on the Fitted Weibull Distribution red triangle
- Select Process Capability
- Enter 40 for $USL \rightarrow OK$

Notes			

Weibull fit (cont'd)

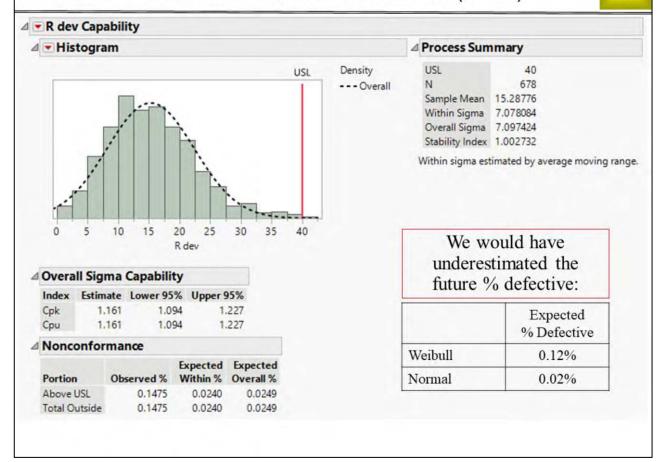


Notes			



Notes		

What if we had assumed a Normal distribution? (cont'd)



Notes			

Steps for fitting a distribution to data

If the Normal or Lognormal is a good fit, use it!

- 1. Analyze \rightarrow Distribution
 - Check Normal Quantile Plot—data in straight line indicates good fit
 - If uncertain: Continuous Fit → Fit Normal
 - Fitted Normal Distribution → Goodness of Fit
 - Anderson-Darling p-value > 0.05 indicates good fit
- 2. If Normal not a good fit: Continuous Fit \rightarrow Fit Lognormal
 - Fitted Lognormal Distribution → Diagnostic Plots → QQ Plot
 - · Data in straight line on the QQ Plot indicates good fit
 - If uncertain: ▼Fitted Lognormal Distribution → Goodness of Fit
 - Anderson-Darling p-value > 0.05 indicates good fit
- 3. If Lognormal is not a good fit: Continuous Fit \rightarrow Fit All
 - Check QQ Plot and view the curve on the histogram to make sure that the fit makes sense.
 - Standard distributions are Weibull, Gamma, Normal, Lognormal, Exponential, Cauchy.
 - JMP offers other specialty distributions that often don't apply, so use caution with them (Johnson Sb, SHASH, Normal 2 Mixture, etc.)

Notes			

	swer questions below. Save the analysis scripts, save and close the data tables. hen opening files, make sure JMP is looking for "All files" not "All JMP files."]						
	Data sets \ quotation process, variable TAT. What % of RFQs in the data set have TAT > 15?						
b)	What % (or PPM) of future RFQs will have TAT > 15?						
c)	Data sets \ solution properties, variable SG coded. What % of solution vials in the data set have SG coded > 50 ?						
d)	What % (or PPM) of future vials will have SG coded > 50?						
e)	Data sets \ number and size of defects, variable # Defects. What % of castings in the data set have more than 50 defects?						
_]	Notes						
_							
_							
_							
_							

Exercise 3.1 (cont'd)

What % (or PPM) of future castings will have more than 50 defects?
Data sets \ casting dimensions, variable Length. What % of castings in the data set have length outside the interval [598, 602]?
What % (or PPM) of future castings will have lengths outside this interval?
Data sets \ casting dimensions, variable Diam. What % of castings in the data set have diameters outside the interval [49, 51]?
What % (or PPM) of future castings will have diameters outside this interval?
Notes

4 Introduction to Life Data

Life = elapsed time until the occurrence of some event

- · Failure of an item on test
- · Planned end of test
- · Unplanned end of test
- · Failure of an item in service
- · Scheduled downtime

Definitions of "time"

- · Seconds, minutes, hours
- · Days, weeks, months
- · Usage cycles, number of moves, distance

Notes				

Life data (cont'd)

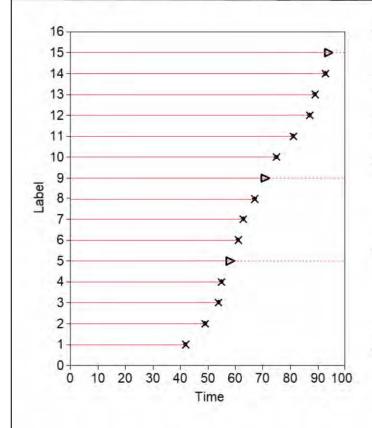
Usually there is one event of primary interest

· Usually, failure of an item

Other events may preempt the event of primary interest

- · Planned end of test
- · Unplanned end of test
- · These are called "suspensions"
- · We say that the time to failure is "censored"

Notes		

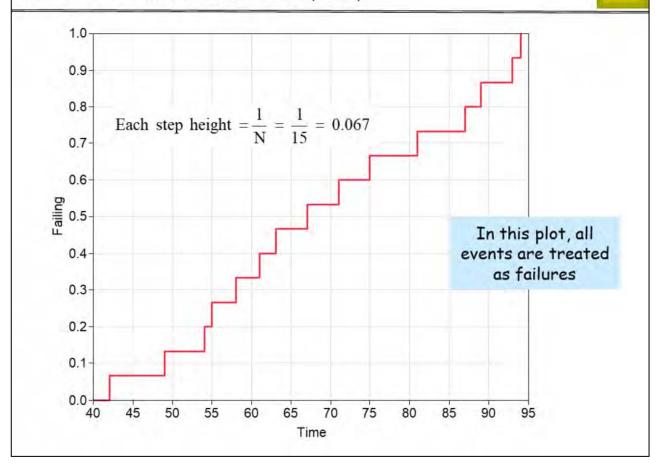


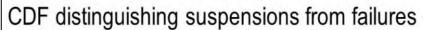
- · 15 items were tested
- 12 failures (x)
- 3 suspensions (▷——)
- This "event plot" distinguishes suspensions from failures and shows the event times
- If we don't distinguish suspensions from failures, the calculated failure probabilities will be biased upwards
- This will make our reliability look worse than it really is

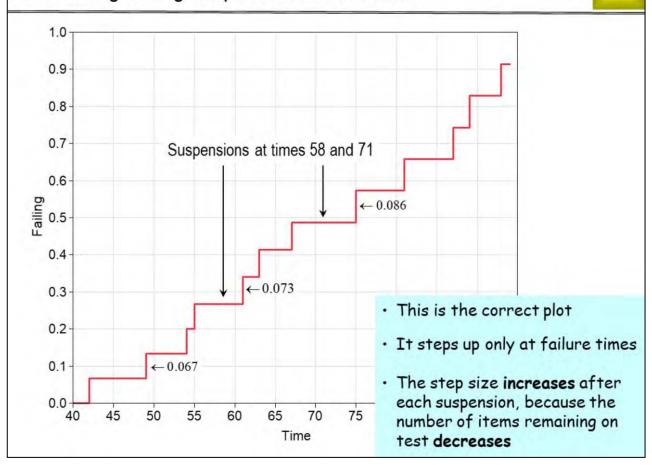
Notes			

Cumulative distribution function (CDF)

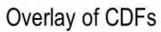


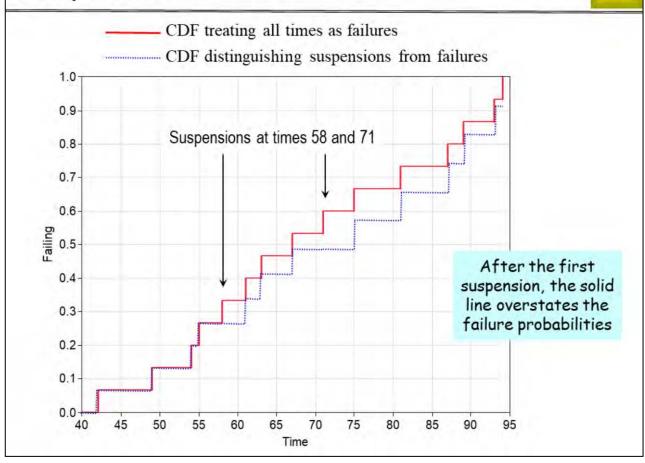




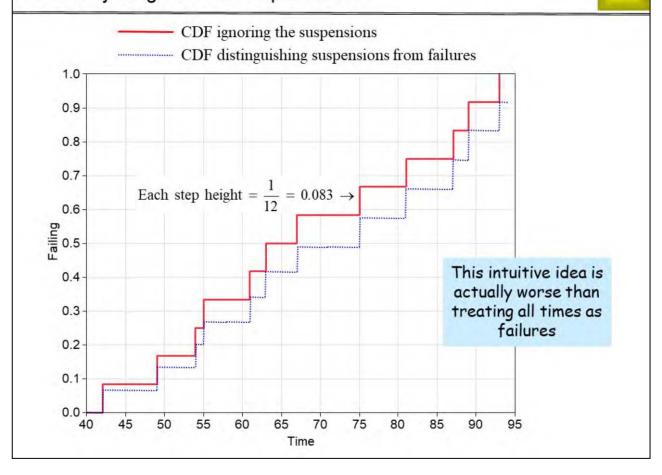


Notes			





Notes			

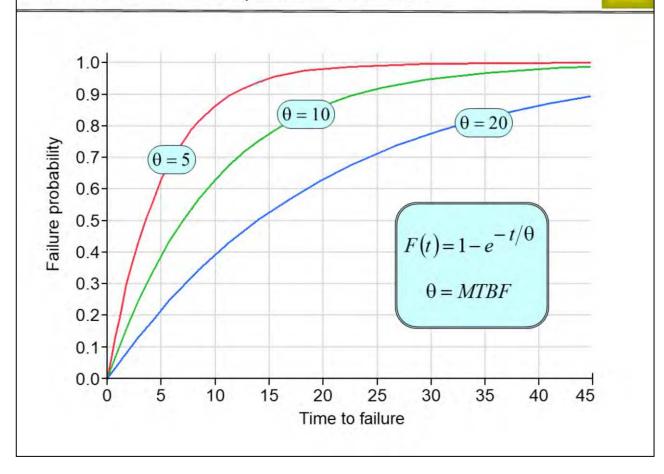


Notes			

5 Analyzing Life Data

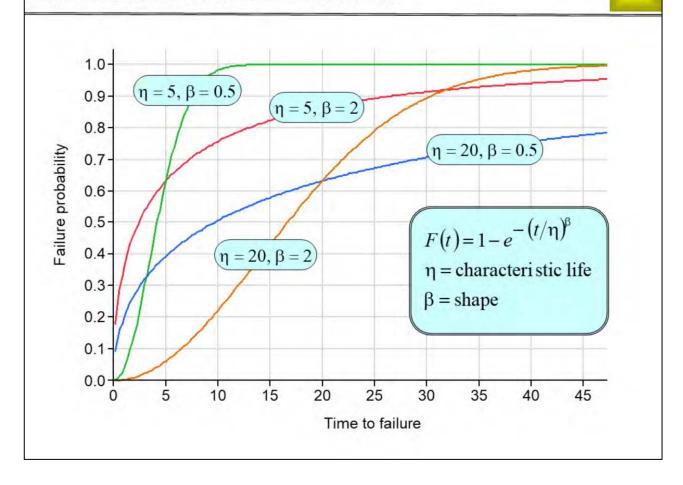
- The Exponential distribution
- The Weibull distribution
- Fitting life distributions in JMP
- Finding and using the best fitting life distribution

Notes			



Notes			

Notes
The Exponential distribution is the simplest life distribution. It has only one parameter: the mean time between/before failure (MTBF). The Greek letter θ (theta) is often used to denote the population value of the MTBF.
Shown above are the <i>failure functions</i> $F(t)$ for three different Exponential distributions. $F(t)$ is the probability that an item will fail before time t .
The <i>reliability function</i> is defined as $R(t) = 1 - F(t)$. $R(t)$ is the probability that an item will survive beyond time t . The Exponential reliability function is given by $R(t) = \exp(-t/\theta)$.
Notes



Notes			

Matag

The Weibull distribution was introduced to the reliability engineering community in the 1950s by a man named Waloddi Weibull. Prior to that, most reliability work was based on the Exponential distribution. Due to its greater flexibility, the Weibull has become one of the most widely-used life distributions.

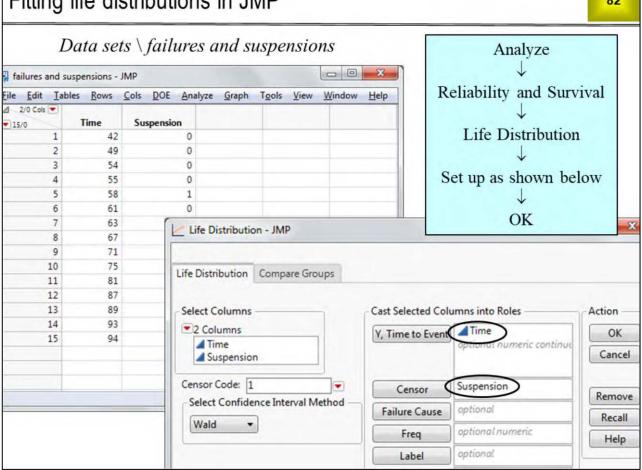
The Weibull distribution has two parameters: the *characteristic life* η (eta), and the *shape* β (beta). The characteristic life (η) has the same qualitative interpretation as the MTBF (θ). The shape parameter (β) determines which of two distinct failure modes are represented. When $\beta < 1$, we have a *burn-in* or *infant-mortality* failure mode. When $\beta > 1$, we have a *wear-out* failure mode. A Weibull distribution with $\beta = 1$ is identical to an Exponential distribution with $\theta = \eta$.

Shown above are failure functions F(t) for four different Weibull distributions. F(t) is the probability that an item will fail before time t.

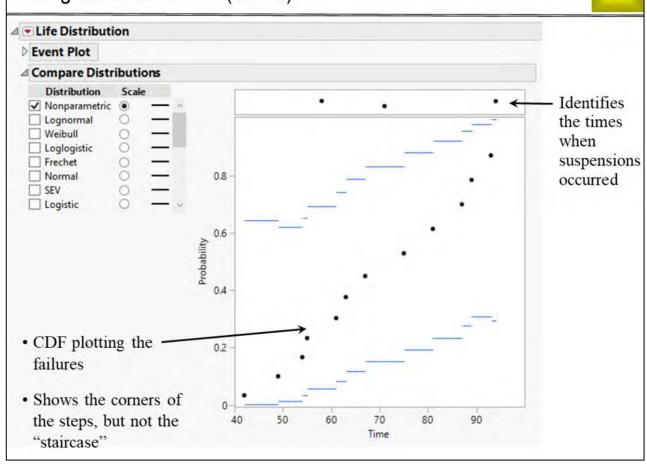
The Weibull reliability function (probability that an item will survive beyond time t) is given by $R(t) = \exp[-(t/\eta)^{\beta}]$.

Notes			

Fitting life distributions in JMP



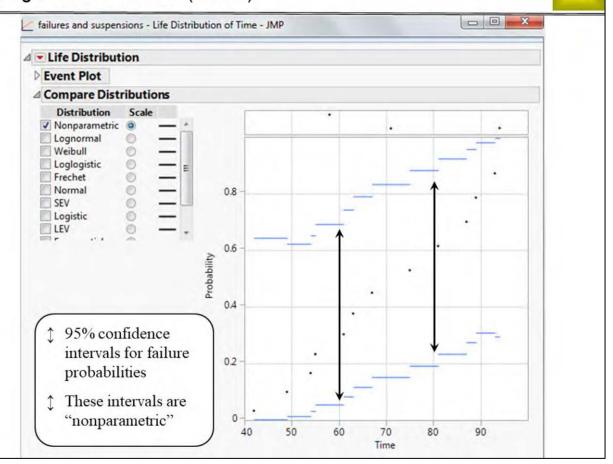
Notes			



Notes			

Fitting life distributions (cont'd)

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Notes			

NILLA

This analysis is referred to as *nonparametric*, meaning that it is not based on a statistical model (such as the ones listed on the left.) This is a good thing, because statistical models can be wrong. However, there are drawbacks:

- a) The nonparametric CDF is discontinuous.
- b) Large numbers of failures are required to get margins of error small enough to be useful.

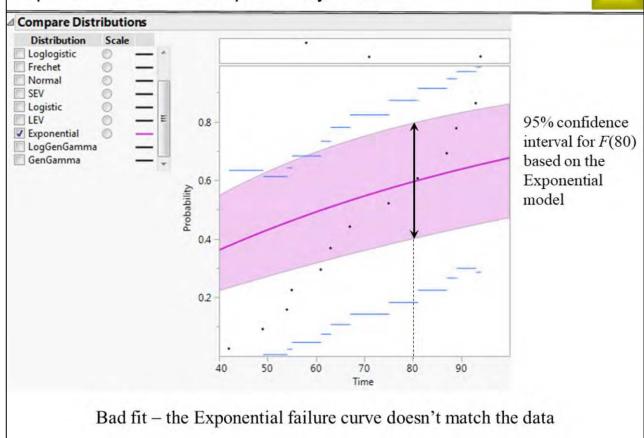
In practice, it is preferable to use a statistical model that fits the data well. This provides a continuous estimate of the failure function and smaller margins of error.

You can change the confidence level by selecting *Change Confidence Level* on the menu produced by the red triangle next to *Life Distribution*.

Notes			

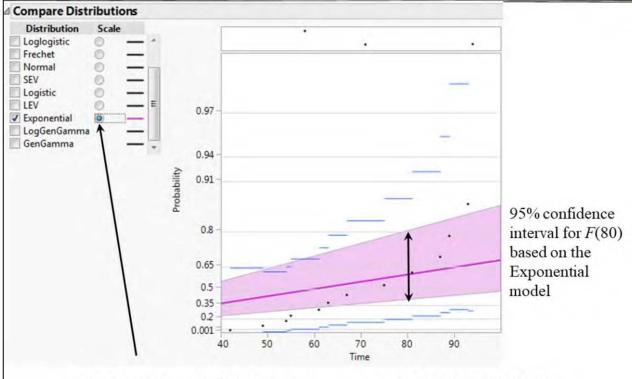


Exponential fit — linear probability scale



Notes			

Exponential fit — Exponential probability scale

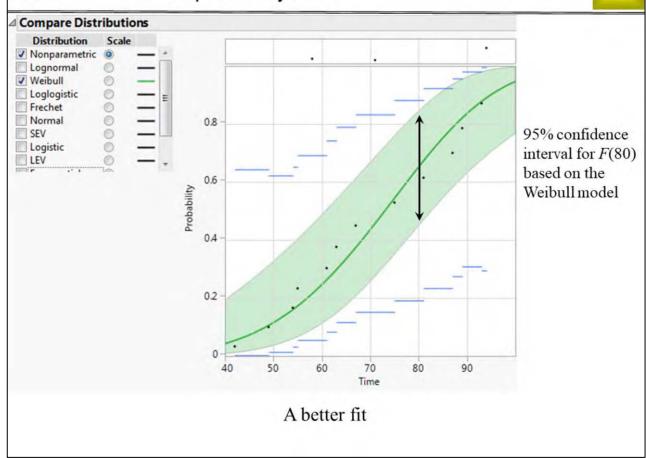


- The Scale button allows the failure curve to plot as a straight line
- This used to be the only way to plot failure curves

Notes			

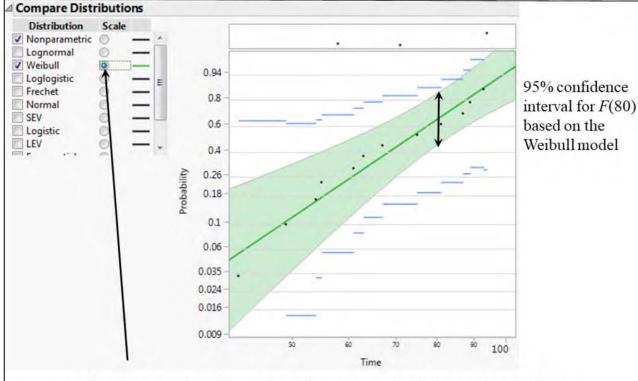


Weibull fit — linear probability scale



Notes			

Weibull fit — Weibull probability scale



- The Scale button allows the failure curve to plot as a straight line
- This used to be the only way to plot failure curves

Notes			

Finding and using the best fitting distribution

*You can't have a negative time to failure!

- Click the Life Distribution red triangle → Fit All Nonnegative* **△** Compare Distributions · JMP plots the best Distribution fitting model on the ✓ Nonparametric **✓** Lognormal corresponding Weibull Loglogistic probability scale Frechet Normal 0.9 SEV · In this case, Logistic E LEV Lognormal gives 0.65 Probability the best fit · See next slide 0.25 0.08 100 Time **Statistics**
 - Notes

Best fitting distribution (cont'd)

Exponential

△ Model Comparisons AICc -2Loglikelihood Distribution BIC Lognormal 112.6 107.57926 112.99536 Weibull 112.8 107.81732 113.23342 Loglogistic 113.3 108.33193 113.74804 Frechet 113.8 108.75681 114.17291 Generalized Gamma 115.7 107.51791 115.64206

• As before, models are ranked by AIC (smaller is better)

133.4

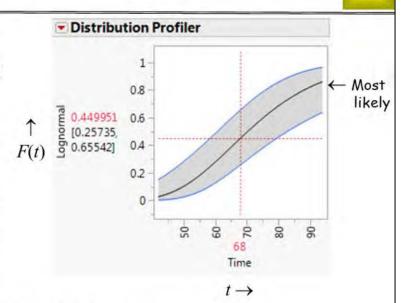
131.06658 133.77463

- · As before, round the AIC values to the nearest tenth
- In this case, Lognormal gives the best fit

Notes			

The distribution profiler

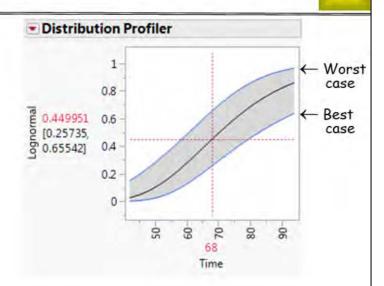
- *F*(*t*) is the probability that an item from this population will fail *before* time *t*
- The middle curve is the *most likely* value of *F*(*t*)
- For example, the most likely value of F(68) is 0.45 (45%) (shown in red on the left side of the profiler)



- The *reliability* function R(t) is defined as 1 F(t)
- *R*(*t*) is the probability that an item from this population will not fail until *after* time *t*
- For example, R(68) = 0.55 (55%)

Notes			

- The upper and lower curves give 95% confidence intervals for *F*(*t*)
- The upper curve gives the worst case value of F(t)*
- For example, the worst case value of F(68) is 0.655 (65.5%)

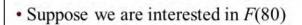


- The lower curve gives the *best case* value of $F(t)^{**}$
- For example, the best case value of F(68) = 0.257 (2.57%)

*For Engineering.

**For Sales.

Notes			



- Change the value 68 to 80 (click and edit)
- The most likely value of F(80) is 68.4
- The worst case value of F(t) is 85.6%
- The best case value of F(80) is 45.7%

Notes

	1-		
	0.8		
0.683682 [0.457, [0.85634]	0.6		
0.85634]	0.4	///	
	02-		
	0-		
	20	09 20	08
		→80 Time	

Data sets \ print life. The "time" to failure is Pages.
a) Identify the best fitting non-negative distribution. Use that distribution to answer the following questions.
b) What is the most likely value of $F(10,000)$?
c) With 95% confidence, what is the worst-case value of $F(10,000)$?
d) Save the analysis script, close and save the data table.
Notes

Data sets \ probe reliability. The "time" to failure is Hits.
a) Identify the best fitting non-negative distribution. Use that distribution to answer the following questions.
b) What is the most likely value of $F(200)$?
c) With 95% confidence, what is the worst-case value of $F(200)$?
d) Save the analysis script, close and save the data table.

Notes			

Data sets \ field reliability. The time to failure is Days in field.
a) Identify the best fitting non-negative distribution. Use that distribution to answer the following questions.
b) What is the most likely value of $F(365)$?
c) With 95% confidence, what is the worst-case value of $F(365)$?
d) Save the analysis script, close and save the data table.
Notes

6 Categorical MSA Without Standards

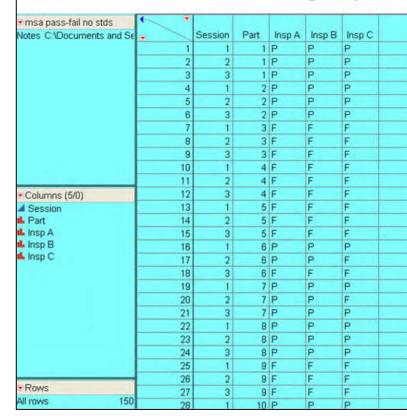
- It is preferable to base nominal MSA on a set of items whose true status is known (standards)
- With standards, we can determine the probabilities of passing bad items and failing good ones
- Creating standards can be difficult and time consuming
- Lacking standards, "% agreement within and between appraisers" can serve as a proxy for "% agreement with standard"

Notes			

Example 1

Notes

Data sets \ pass-fail no stds

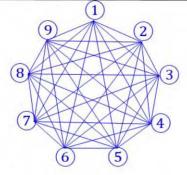


- · 50 parts
- · Appraisers A, B, C
- 3 inspections per part per appraiser
- Part is actually nominal, since part numbers are only identifiers without a numerical relationship. Change by:
- Right click on next to Part and Select Nominal, or
- Right click on field name "Part" > Column Info > Data Type = Character
- Please be aware that JMP is occasionally inconsistent in its terminology

110165			

,	Session	Part	Insp A	Insp B	Insp C
1	1	1	P	P	P
	2	1	Р	P	P
	3	1	P	P	P
4	1	2	P	P	P
5	2	2	P	P	P
6	3	2	P	P	P
7	1	3	F	F	F
8	2	3	F	F	F
9	3	3	F	F	F
10	- 1	4	F	F	F
11	2	4	F	F	F
12	3	4	F	F	F
13	- 1	5	F	F	F
14	2	5	F	F	F
15	3	5	F	F	F
16	1	6	P	P	P
17	2	6	P	P	F
18	3	6	F	F	F
19	- 1	7	P	P	P
20	2	7	Р	P	F
21	3	7	P	P	P
22	1	8	P	P	P
23	2	8	P	P	P
24	3	8	P	P	P
25	1	9	F	F	F
26	2	9	F	F	F
27	3	9	F	F	F
28	1	10	P	P	P
29	2	10	P	P	P
30	3	10	P	P	P
31	1	11	P	P	P
32	2	11	P	P	P
33	3	11	P	P	P
34	1	12	F	F	F
	2	12	F	F	P
36	3	12	F	F	F

• 100% agreement

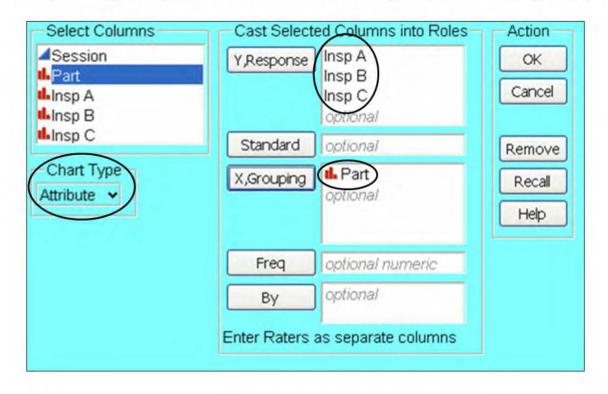


- 36 opportunities for pairwise agreement
- 16 pairwise agreements
- Agreement = 16/36 = 0.444
- 36 opportunities for pairwise agreement
- 8 pairwise disagreements
- Agreement = 28/36 = 0.778

Notes			

Analyzing a categorical MSA without standards

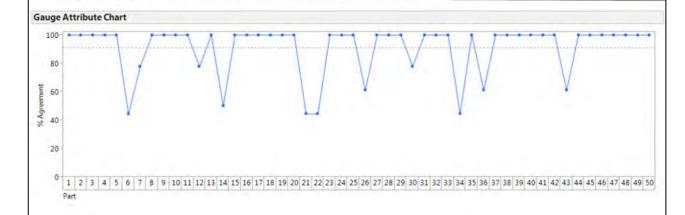
 $Analyze \rightarrow Quality \ and \ Process \rightarrow Variability / \ Attribute \ Gauge \ Chart$



Notes	

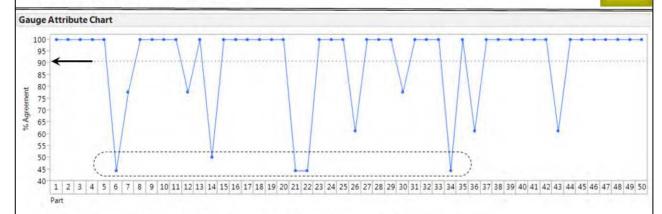
Agreement report

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- Plot of the agreement percentages for the items in the study
- · It is helpful to rescale the vertical axis
- · See next slide

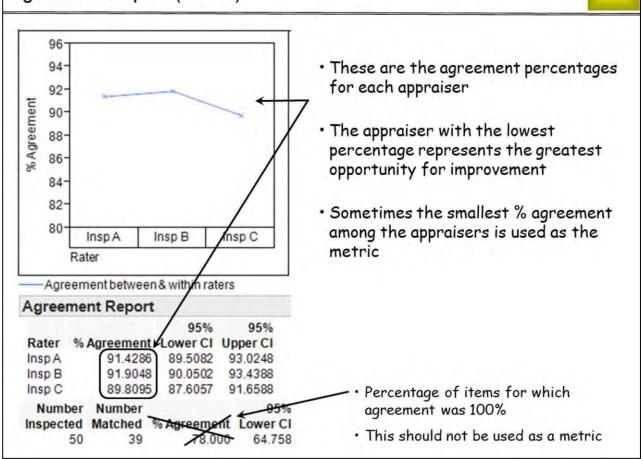
Notes	



- · The horizontal dotted line marks the "agreement grand mean"
- · In this example, the agreement grand mean is a little over 90 (read off graph)
- Nowhere in the report is this number printed bad JMP!
- If the agreement grand mean is too low, follow-up should focus on the items with the lowest % agreement
- There are no recognized standards for the agreement grand mean. A lower bound of 95% is fairly common. 99% is often used in applications involving safety.

Notes			

TAT A



Notes			

Save the script, close and save the data table.

Agreement Comparisons:

Each rater compared to all others, using Kappa statistics

 $K \ge 0.9 \rightarrow \text{Good measurement system}$

 $K \le 0.7 \rightarrow \text{Bad measurement system}$

 $0.7 \le K \le 0.9 \rightarrow \text{Marginal measurement system}$

Agreement across Categories:

Agreement in classification corrected for the amount of agreement which would be expected by chance. Kappa assesses the agreement between a fixed number of raters when classifying items.

When K = 1, perfect agreement exists.

When K = 0, agreement is the same as would be expected by chance.

When K < 0, agreement is weaker than expected by chance; this rarely occurs and usually means that the appraisers have different definitions of the assigned categories.

Notes			

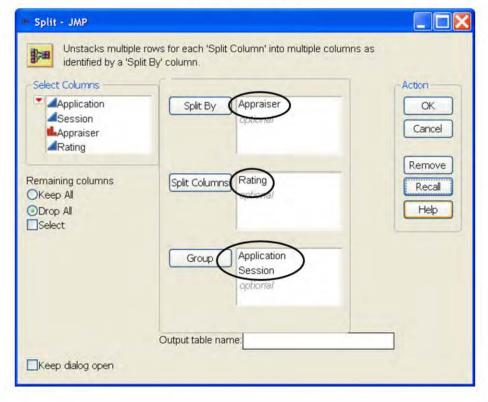
$Data\ sets \ \backslash\ application\ rating\ no\ stds$

application rating no stds	•							
Notes C:\Documents and Se	•	Application	Session	Appraiser	Rating			
	1	1	1	Simpson	5	• 15 employment applications		
	2	1	1	Montgomery	5	T		
	3	1	1	Holmes	5			
	4	1	1	Duncan	4	• 5 appraisers		
	5	- 1	- 1	Hayes	5			
	6	2	1	Simpson	2 2 2	• 2 inspections per application		
	7	2	1	Montgomery	2	per appraiser		
	8	2	1	Holmes	2			
	9	2	1	Duncan	1			
	10	2	1	Hayes	2	• Five point coals higher is		
	11	3	1	Simpson	4	Five point scale, higher is		
Columns (4/0) Application Session Appraiser Rating	12	3	1	Montgomery	3	better		
	13	3	1	Holmes	3			
	14	3	1	Duncan	3	C1 D : 1		
	15	3		Haves		• Change <i>Rating</i> to nominal		
	16		1	Simpson	1			
	17	4	1	Montgomery Holmes	1	For categorical MSA, we		
	19	4	1	Duncan	- 1			
	20	4	- 1	Haves	1	must <i>unstack</i> this data table		
	21	5	1	Simpson	3			
	22	5	1	Montgomery	3			
	23	5	1	Holmes	3			
	24	5	1	Duncan	2			
	25	5	1	Hayes	3			
	26	6	1	Simpson	4			
Rows	27	6	1	Montgomery	4			
All rows 150								

Notes			

Unstacking a data table

$Tables \rightarrow Split$



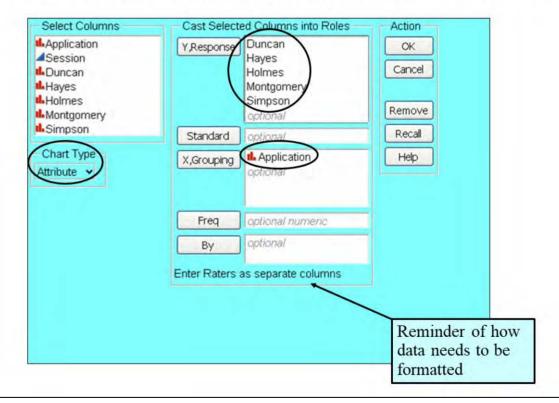
Notes			

Example 2 in required format

Untitled 12	•								
Source		Application	Session	Duncan	Hayes	Holmes	Montgomery	Simpson	
	1	1	1	4	5	5	5	5	
	2	2	1	1	2	2	2	2	
	3	3	1	3	3	3	3	4	
	4	4	1	1	1	1	1	1	
	5	5	1	2	3	3	3	3	
	6	6	1	4	4	4	4	4	
	7	7	1	4	5	5	5	5	
	8	8	1	3	3	3	3	3	
	9	9	1	-1	2	2	2	2	
	10	10	1	3	5	4	4	4	
-0.1 (710)	11	11	1	1	2	1	1	1	
Columns (7/0)	12	12	1	2	3	3	3	3	
Application Session	13	13	1	5	5	5	5	5	
L Duncan	14	14	1	2	2	2	2	2	
L Hayes	15	15	1	4	4	4	4	4	
L Holmes	16	1	2	4	5	5	5	4	
. Montgomery	17	2	2	1	2	2	2	2	
ll. Simpson	18	3	2	3	3	4	4	4	
	19	4	2	1	1	1	1	1	
	20	5	2	2	3	3	3	3	
	21	6	2	4	4	4	5	5	
	22	7	2	4	5	5	5	5	
	23	8	2	3	4	3	3	3	
	24	9	2	1	2	2	2	2	
	25	10	2	3	5	4	4	4	
	26	11	2	1	2	1	1	1	
Rows	27	12	2	2	3	3	3	3	
All rows 30	28	13	2	5	5	5	5	5	

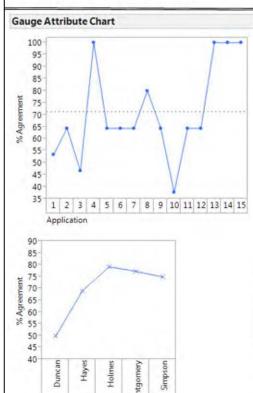
Notes			

$Analyze \rightarrow Quality\ and\ Process \rightarrow Variability/Attribute\ Gauge\ Chart$



Notes		

Example 2 (cont'd)



Agreement between & within raters

- The agreement grand mean is about 71

 way too low
- Follow-up: focus on application 1, 3 and 10
- Greatest opportunity for improvement: further training of Duncan and Hayes

Agreement Report

			95%	95%	
Rater	% Agreen	nent	Lower Cl	Upper CI	
Duncan	49.8	3039	27.2673	72.4205	
Hayes	69.0	196	43.9053	86.3784	
Holmes	79.2	2157	53.9935	92.5247	
Montgomery	77.2	2549	51.9716	91.4246	
Simpson	74.9	9020	49.5997	90.0500	
Number	Number			95%	95%
Inspected	Matched	% Agu	reement	Lower CI	Upper CI
15	4	/	26.66Z	10.897	51.950
	Duncan Hayes Holmes Montgomery Simpson Number Inspected	Duncan 49.8 Hayes 69.0 Holmes 79.2 Montgomery 77.2 Simpson 74.8 Number Number Inspected Matched	Duncan 49.8039 Hayes 69.0196 Holmes 79.2157 Montgomery 77.2549 Simpson 74.9020 Number Number Inspected Matched % Age	Rater % Agreement Lower CI Duncan 49.8039 27.2673 Hayes 69.0196 43.9053 Holmes 79.2157 53.9935 Montgomery 77.2549 51.9716 Simpson 74.9020 49.5997 Number Number Inspected Matched Agreement	Rater % Agreement Lower CI Upper CI Juncan 49.8039 27.2673 72.4205 Hayes 69.0196 43.9053 86.3784 Holmes 79.2157 53.9935 92.5247 Montgomery 77.2549 51.9716 91.4246 Simpson 74.9020 49.5997 90.0500 Number Number 95% Inspected Matched Agreement Lower CI

Notes				

Notes	112
Save the analysis script to the data table, close and save the data table as:	
application rating no stds unstacked	
Notes	

Data sets \ print samples 1 no stds. In this study 3 appraisers inspected 18 print samples 3 times each.
a) Reformat the file as needed and run the analysis.
b) Record the approximate agreement grand mean.
c) Which sample(s) would be most useful in follow-up?
d) Of the 3 appraisers, which has the highest % agreement? What is the highest % agreement?
e) Save the script, close and save the data table as print samples 1 no stds unstacked
Notes

	ta sets \ print samples 2 no stds. This is the follow-up study after the appraisers eived additional training.
a)	Reformat the file as needed and run the analysis.
b)	Record the approximate agreement grand mean.
c)	Of the 3 appraisers, which has the lowest % agreement? What is the lowest % agreement?
d)	Save the script, close and save the data table as print samples 2 no stds unstacked.
	Notes
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7 Comparing Populations – Continuous Y

- Example of comparing populations
- Analysis of variance (ANOVA) for comparing populations
- Interpreting P-values
- · Degrees of freedom for signal and noise
- ANOVA in JMP

Notes			

Notes

Notes

Y variables are characteristics of parts, products or transactions	
customer satisfaction, or lack thereof. They provide the data fr metrics can be computed.	om which project

Comparison of statistical populations is equivalent to Y = f(X) analysis where the X variable is categorical. The distinct values of the X variable define the populations or sub-populations to be compared.

JMP uses the term *continuous* for quantitative variables. Except in the DOE section, JMP uses the term *nominal* for categorical variables.

110165			

Example of comparing populations

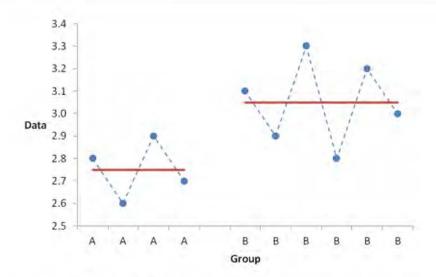
Data sets \ Anova 2 groups

Group	Data	Avg.	SD			
Α	2.8					
Α	2.6	0.75	0.400			
Α	2.9	2.75	0.129			
Α	2.7					
В	3.1					
В	2.9					
В	3.3	3.05	0.107			
В	2.8	3.05	0.187			
В	3.2					
В	3.0	0				

- We have two groups of data
- Could be a before/after comparison
- Could be a stratification analysis

- The sample means for the two groups are different
- Is this enough to conclude that the population means are different?

Notes			



- · Plotting the data is helpful, but it doesn't give a definitive answer
- How far apart do the sample means have to be before we can say the population means are different?
- How do we take into account the scatter around the means?

Notes			

LSSV2 student files \ ANOVA two groups

В	C	D	Е	F	G	Н	- 1	J	K	L	M
Group		Data		Grand mean		Difference	e	Group		Error	
Α		2.8		2.93		-0.13		-0.18		0.05	
Α	П	2.6		2.93		-0.33		-0.18		-0.15	
Α	Н	2.9		2.93		-0.03		-0.18	- 14	0.15	
Α	Н	2.7		2.93		-0.23		-0.18		-0.05	
В	Н	3.1	_	2.93	=	0.17	-	0.12	+	0.05	
В	П	2.9		2.93		-0.03		0.12		-0.15	
В	П	3.3		2.93		0.37		0.12		0.25	
В	П	2.8		2.93		-0.13		0.12		-0.25	
В		3.2		2.93		0.27		0.12		0.15	
В		3.0		2.93		0.07		0.12		-0.05	

Notes			

ANOVA (1 of 6, cont'd)

This worksheet shows all the calculations used to determine, based on the data, whether or not the population means are different.	
The first step is to calculate the <i>Difference</i> column by subtracting the grand mean from the <i>Data</i> column. The <i>Difference</i> is then decomposed into <i>Group</i> (the "signal") plus <i>Error</i> (the "noise").	
The <i>Group</i> column captures the portion of total variation caused by the difference between the sample means.	
The first step is to calculate the <i>Difference</i> column by subtracting the grand mean from the <i>Data</i> column. The <i>Difference</i> is then decomposed into <i>Group</i> (the "signal") lus <i>Error</i> (the "noise"). The <i>Group</i> column captures the portion of total variation caused by the difference	
Notes	

LSSV2 student files \ ANOVA two groups

Α	В	C D	E	F	G	Н	1	J	K	L	M
	Grand										
	Group	Data	1	mean		Differenc	е	Group		Error	
	Α	2.8		2.93		-0.13		-0.18		0.05	
	Α	2.6		2.93		-0.33		-0.18		-0.15	
	Α	2.9		2.93		-0.03		-0.18		0.15	
	Α	2.7		2.93		-0.23		-0.18		-0.05	
	В	3.1	-	2.93	=	0.17	=	0.12	+	0.05	
	В	2.9		2.93		-0.03		0.12		-0.15	
	В	3.3		2.93		0.37		0.12		0.25	
	В	2.8		2.93		-0.13		0.12		-0.25	
	В	3.2		2.93		0.27		0.12		0.15	
	В	3.0		2.93		0.07		0.12		-0.05	
Degrees of free	dom (DF)	10	-	1	=	9	=	1	+	8	

Notes		

ANOVA (2 of 6, cont'd)

The Data column consists of 10 mathematically independent quantities. We describe this by saying it has 10 degrees of freedom (DF).
The <i>Grand mean</i> column consists of 10 values, but they are all identical. This column has 1 DF.
The <i>Difference</i> column contains 10 values, but they are mathematically constrained to sum to 0. This column contains only 9 independent quantities, so it has 9 DF.
The <i>Group</i> column inherits the zero-sum constraint from the <i>Difference</i> column (it must sum to zero), and it consists of only 2 distinct values. This column contains only one independent quantity, so it has 1 DF.
The Error column has 8 DF, because DFs have to add up.
The DFs for <i>Group</i> and <i>Error</i> play a role in determining whether or not the population means are different.

Notes			

LSSV2 student files \ANOVA two groups

A B	C D	E	F	G	Н	4	J	K	L	M
Grand										
Group	Data		mean	ı	Difference	е	Group		Error	
А	2.8		2.93	ļ. — i	-0.13		-0.18		0.05	
А	2.6		2.93		-0.33		-0.18		-0.15	
А	2.9		2.93		-0.03		-0.18		0.15	
A	2.7		2.93		-0.23		-0.18		-0.05	
В	3.1	-	2.93	=	0.17	=	0.12	+	0.05	
В	2.9		2.93		-0.03		0.12		-0.15	
В	3.3		2.93		0.37		0.12		0.25	
В	2.8		2.93		-0.13		0.12		-0.25	
В	3.2		2.93		0.27		0.12		0.15	
В	3.0		2.93		0.07		0.12		-0.05	
Degrees of freedom (DF)	10	-	1	=	9	-	1	+	8	
Sum of squares (SS)	86.29	-	85.85	-	0.441	-	0.216	+	0.225	
Mean square (MS)	(SS/DF)			0.049		0.216		0.028	

Notes			

ANOVA (3 of 6, cont'd)

The sum of squares (SS) is a measure of the magnitude of each column. It is the sum of the squares of the values in a column.
The sums of squares for the $Difference$, $Group$, and $Error$ columns are usually much smaller than those of the $Data$ and $Grand$ $mean$ columns.
The mean square (MS) is the statistically normalized measure (averaged, in a sense) of the magnitude of each column. It is the SS for a column divided by the DF for that column.
The mean squares for the <i>Data</i> and <i>Grand mean</i> columns play no role in determining whether or not the population means are different, so the MS is usually calculated only for the <i>Difference</i> , <i>Group</i> , and <i>Error</i> columns.
Notes

ANOVA (4	4 of 6)					- 77				1	125
	LSSV2 student files \ ANOVA two groups										
Α	В	C D	E	F	G	Н	1	J	K	L	M
				Grand							
	Group	Data		mean		Differenc	e	Group		Error	
	Α	2.8		2.93		-0.13		-0.18		0.05	
	Α	2.6		2.93	H	-0.33		-0.18		-0.15	
	Α	2.9		2.93		-0.03		-0.18		0.15	
	Α	2.7		2.93		-0.23		-0.18		-0.05	
	В	3.1	-	2.93	=	0.17	=	0.12	+	0.05	
	В	2.9		2.93		-0.03		0.12		-0.15	

2.93

2.93

2.93

2.93

1

85.85

0.37

-0.13

0.27

0.07

9

0.441

0.049

0.25

-0.25

0.15

-0.05

8

0.225

0.028

7.680

0.12

0.12

0.12

0.12

1

0.216

0.216

В

В

В

F ratio

Degrees of freedom (DF)

Sum of squares (SS)

Mean square (MS)

3.3

2.8

3.2

3.0

10

86.29

(SS/DF)

(Group MS / Error MS)

Notes			

ANOVA (4 of 6, cont'd)

The <i>Group</i> MS measures the magnitude of the variation caused by the difference between the sample means.
The <i>Error</i> MS measures the magnitude of the variation caused by everything <i>except</i> the difference between the sample means.
The F ratio is the Group MS divided by Error MS. It is a signal-to-noise ratio.
The larger the F ratio, the stronger the evidence of a difference between the population means.
Notes

A B	C D	E	F	G	Н	1	J	K	L	М
*			Grand							
Group	Data		mean		Difference	е	Group		Error	
A	2.8		2.93		-0.13		-0.18		0.05	
A	2.6		2.93		-0.33		-0.18		-0.15	
A	2.9		2.93		-0.03		-0.18		0.15	
A	2.7		2.93		-0.23		-0.18		-0.05	
В	3.1	-	2.93	=	0.17	-	0.12	+	0.05	
В	2.9		2.93		-0.03		0.12		-0.15	
В	3.3		2.93		0.37		0.12		0.25	
В	2.8		2.93		-0.13		0.12		-0.25	
В	3.2		2.93		0.27		0.12		0.15	
В	3.0		2.93		0.07		0.12		-0.05	
Degrees of freedom (DF)	10	-	1	=	9	-	1	+	8	
Sum of squares (SS)	86.29	-	85.85	=	0.441	=	0.216	+	0.225	
Mean square (MS)	(SS/DF)			0.049		0.216		0.028	
F ratio	(Group I	MS/E	Frror MS)					7.680	
P value	(Probabi	lity of	an F rati	io this l	large by cl	hance	alone)		0.0242	

Notes			

	is a probability the DF for the		he F ratio, the	ne DF for th	ie Group
Notes					

Interpreting P-values

0.0001 Evid	Evidence that populations are different or variables are correlated	Confidence level (CL)				
		None	None			
0		Some	85% ≤ <i>C</i> L < 95%			
P-value	0.01	Strong	95% ≤ <i>C</i> L < 99%			
		Very strong	<i>C</i> L ≥ 99%			
0	0001					

	Notes
-	

P-values (cont'd)

As shown above, the P-value has fixed reference values for interpretation.

The P value is inversely related to the F ratio:

> The smaller the P-value, the stronger the evidence of a difference between the population means.

If there are 3 or more groups, the interpretation is:

> The smaller the P-value, the stronger the evidence of one or more differences among the population means.

Notes			

A	В	C D	Е	F	G	Н	1	J	K	L	М
				Grand							
	Group	Data		mean		Difference	9	Group		Error	
	Α	2.8		2.93		-0.13		-0.18		0.05	
	Α	2.6		2.93		-0.33		-0.18		-0.15	
	Α	2.9		2.93		-0.03		-0.18		0.15	
	Α	2.7		2.93		-0.23		-0.18		-0.05	
	В	3.1	-	2.93	-	0.17	-	0.12	+	0.05	
	В	2.9		2.93		-0.03		0.12		-0.15	
	В	3.3		2.93		0.37		0.12		0.25	
	В	2.8		2.93		-0.13		0.12		-0.25	
	В	3.2		2.93		0.27		0.12		0.15	
	В	3.0		2.93		0.07		0.12		-0.05	
Degrees of freed	dom (DF)	10	-	1	, = ,	9	=	1	+	8	
Sum of squa	ares (SS)	86.29	-	85.85	=	0.441	=	0.216	+	0.225	
Mean squ	are (MS)	(SS/DF	=)			0.049		0.216		0.028	
	F ratio	(Group	MS/E	Error MS)					7.680	
	P value	(Probab	ility of	an F rati	o this l	arge by cl	hance	alone)		0.0242	
Root mean squa	re (RMS)	(Square	root o	of MS)		0.221				0.168	

Notes			

ANOVA (6 of 6, cont'd)

The Root Mean Square (RMS) for a column is the square root of the MS for that column.
The RMS for the <i>Difference</i> column (0.221) is equal to the usual standard deviation of the data (STDEV function in Excel).
The RMS for the <i>Error</i> column (0.168) is the standard deviation of the noise variation (error, residual, unexplained, etc.).
JMP uses the term $Root\ Mean\ Square\ Error\ (RMSE)$ for the RMS of the $Error\ column.^*$
*Given that Statistics is a body of knowledge dedicated to quantifying and reducing variation, the variation in statistical terminology is appalling.
Notes

N = total sample size

G = number of groups being compared

G-1 = DF for the group column

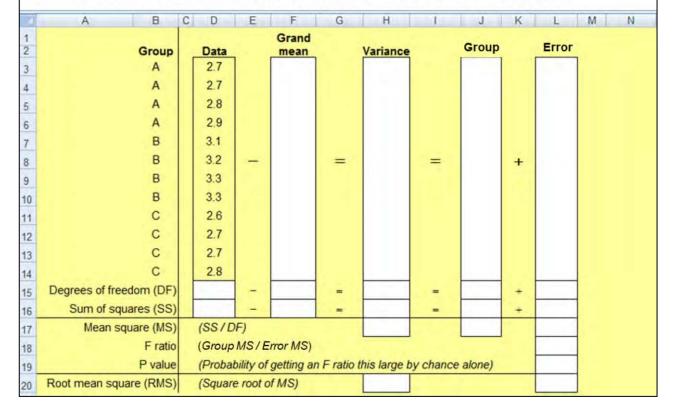
N-G = DF for the error column

- The Error DF is more important than the Group DF
- It determines the accuracy of the predicted values
- Larger is better, 10 is OK, bare minimum is 5
- When DF is mentioned without a qualifier, it always means Error DF

	Notes
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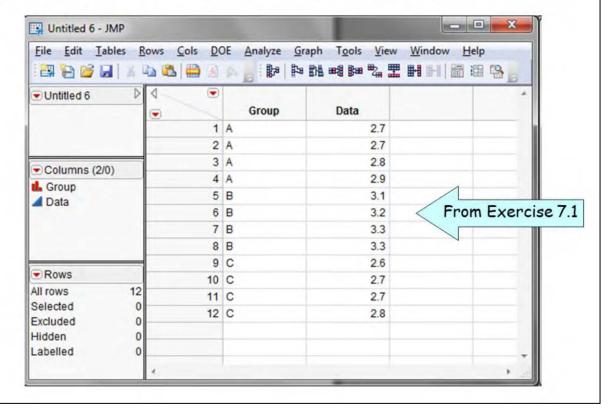
Exercise 7.1

LSSV2 student files \ ANOVA three groups. Enter the appropriate numbers and formulas into the white cells to produce an ANOVA for the data shown here.



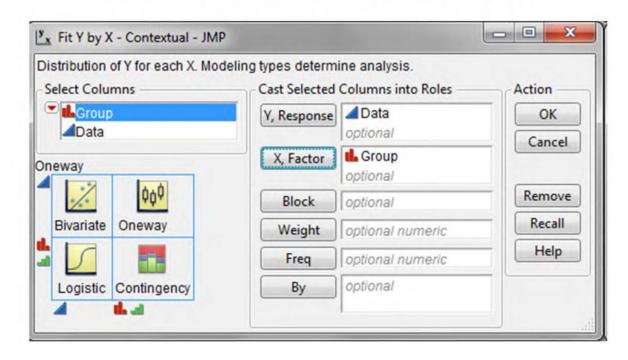
Notes			

 $File \rightarrow New \rightarrow Data \ Table \rightarrow Enter$ (or copy-paste) data as shown

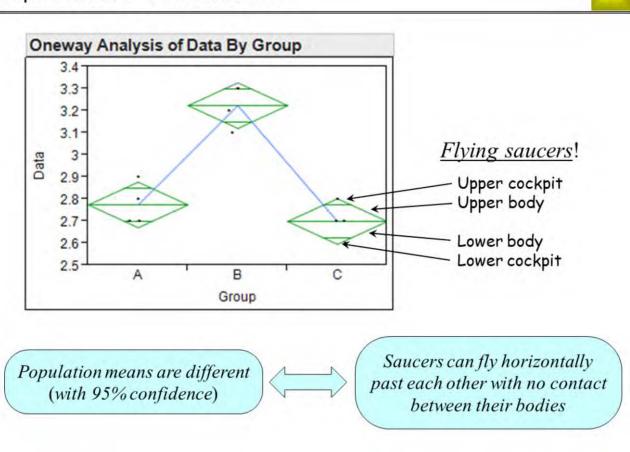


Notes			

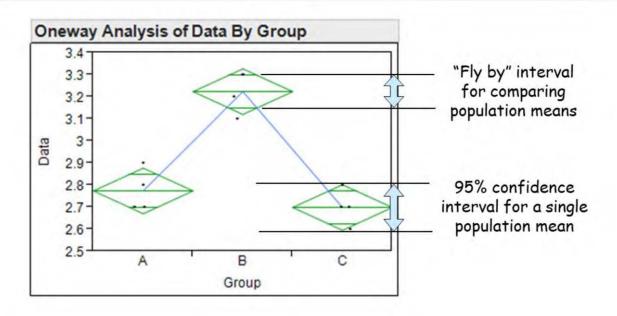
$Analyze \rightarrow Fit \ Y \ by \ X \rightarrow Set \ up \ as \ shown \rightarrow OK$



Notes			



Notes			



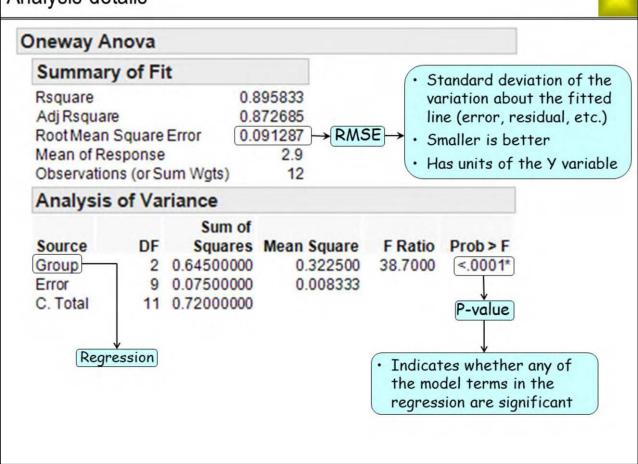
Approx. formula for "fly by" interval: Sample mean $\pm \sqrt{2} \left(RMSE / \sqrt{N} \right)$

Approx. formula for 95% confidence interval: Sample mean $\pm 2(RMSE/\sqrt{N})$

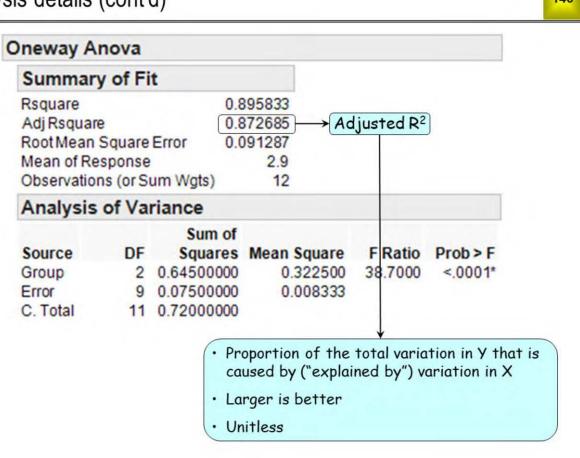
N = sample size for each group

Notes			

Analysis details

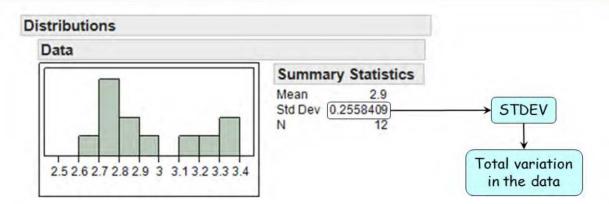


Notes			



Notes			

TAT 4



Proportion of Y variation NOT caused by
$$X = \left(\frac{RMSE}{STDEV}\right)^2 = \left(\frac{0.091287}{0.2558409}\right)^2 = 0.127315$$

Proportion of Y variation CAUSED by
$$X = 1 - \left(\frac{RMSE}{STDEV}\right)^2 = 0.872685 = Adjusted R^2$$

Notes			

	ta sets \ number and size of defects. Max size is the area in square centimeters of largest contiguous weld repair area on each casting. Smaller Max size is better.
a)	Test for a difference between welders A and B with respect to <i>Max size</i> . Give the P value and interpret the result. (Ignore the <i>t Test</i> section of the output.)
b)	Which welder represents best practice? What follow-up action should be taken?
c)	Give the value and the units of the RMSE in this example.
d)	The RMSE is meaningful only if each group has roughly the same amount of variation. Is this true in this case?
e)	Save your analysis script to the data table, close and save the data table.
	Notes

Data sets \ quotation process. Supplier business units (BUs) receive requests for quote (RFQs) from customers. Account managers develop and submit the quotes. TAT is the turnaround around time in days. The shorter the TAT, the happier the customer.
a) Is the modeling type for BU correct? If not, change it to what it should be.
b) Test for differences among the BUs. Give the P value and interpret the result.
c) Use the "flying saucers" to determine which BUs represent best practice.
d) What follow-up action should be taken?
e) Save your analysis script to the data table, close and save the data table.
Notes

	ta sets \ alignment process. If the modeling type for Aligner is incorrect, change it what it should be.
a)	Test for differences among the three aligners with respect to <i>R dev</i> . Give the P-value and interpret the results.
b)	Use the "flying saucers" to determine which aligner represents best practice. (Smaller <i>R dev</i> is better.)
c)	What follow-up action should be taken?
d)	Save your analysis script to the data table, close and save the data table.
_	Notes
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Data sets \ casting dimensions. We want to reduce variation in the length of cylindrical metal castings. The specification for Length is 600 ± 1.5 . The wax patterns for these castings are molded on two machines A and B.
a) Test for differences between the molding machines with respect to Length. Give the P-value and interpret the result.
b) Use the "flying saucers" to determine which machine represents best practice? (It is helpful to draw a reference line at the nominal value. Right click on one of the numbers on the vertical axis, select Axis Settings, use the Reference Lines tool.)
c) What follow-up action should be taken?
d) Save your analysis script to the data table, but don't close the data table.
Notes

Exercise 7.5 (cont'd)

We also want to reduce variation in the diameter of the castings. The specification Diam is 50 ± 0.75 .	for
d) Test for differences between the molding machines with respect to Diam. Give the P-value and interpret the result.	ve
e) Use the "flying saucers" to determine which machine represents best practice. (Draw a reference line at the nominal value.)	
f) What follow-up action should be taken?	

- g) For each of the variables Length and Diam, a certain proportion of the total variation is caused by the difference between the machines. For which variable is this proportion highest?
- h) Save your analysis script to the data table, close and save the data table.

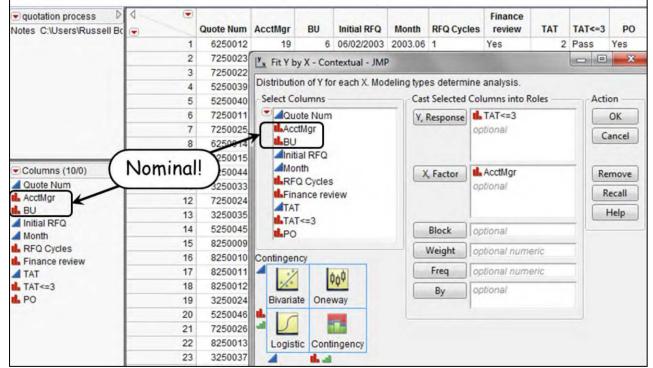
Notes			

8	Comparing Popu	lations – Pass/fail Y	147
	Raw data	One part or transaction per row	
	Tabulated data	Multiple parts or transactions per row	

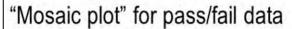
Notes			

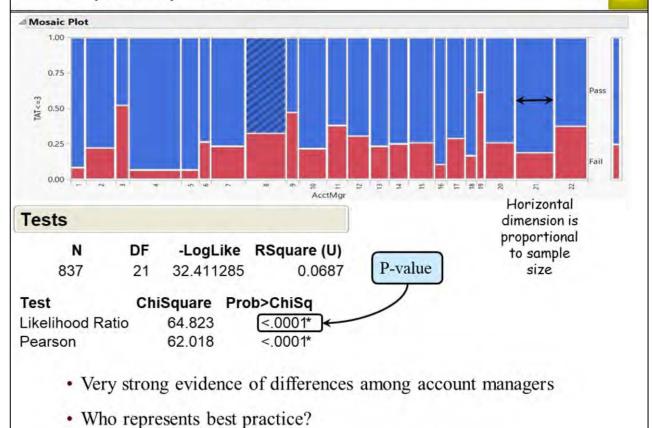
Raw data example

Data sets \ quotation process We want to compare the account managers in terms of % late $Analyze \rightarrow Fit \ Y \ by \ X \rightarrow set \ up \ as \ shown \rightarrow OK$



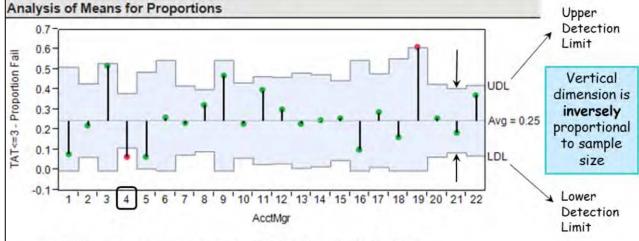
Notes			





Notes			

• Red triangle (Contingency Analysis) → Analysis of Means for Proportions



- · "Flying saucers" are not available for pass/fail data
- · Points outside the shaded region are significantly different from points inside
- AcctMgr 4 represents best practice (lowest failure rate)
- Find out what AcctMgr 4 is doing, make it the standard
- · Save your analysis script to the data table, but don't close the data table

Notes			

a)	Analyze $TAT \le 3$ as a function of BU . Give the P-value and interpret the result. Is there best practice? If so, where is it?
b)	Analyze PO as a function of BU . Give the P-value and interpret the result. Is there best practice? If so, where is it?
c)	Right click on the PO header in the data table. Select $Column\ Properties o Value\ Ordering o Reverse o OK$. This reverses the Yes and Yo positions on the PO axis. Most people focus on the PO hit rate rather than the miss rate.
d)	Analyze PO hit rate as a function of $TAT \le 3$. Give the P-value and interpret the result.
e)	Save your scripts, close and save the data table.
_ _	Notes
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_	
_	

Data sets $\ \ ATE\ data.$ If necessary, change the modeling types for part number (P/N) and Tester.

- a) Test for a difference between the part numbers (P/N) with respect to *Result*. Give the P-value and interpret the results.
- b) Test for differences among the testers with respect to Result. Give the P-value and interpret the results. If significant differences exist, describe them. If possible, suggest causes of the differences.
- c) Test for differences among the *P/N-Tester* groupings with respect to *Result*. Give the P-value and interpret the results. If significant differences exist, describe them. If possible, suggest causes of the differences.
- d) Save your scripts, close and save the data table.

Notes			

- · Pass/fail data often comes in tabulated form
- · Each row may represent a
 - ✓ Production lot
 - √ Work order
 - √ Time period
 - ✓ Machine
 - √ Work center
 - ✓ Part number . . .
- · This format is perfect for plotting % defective
- However, it is the wrong format for comparing populations in JMP

Notes			

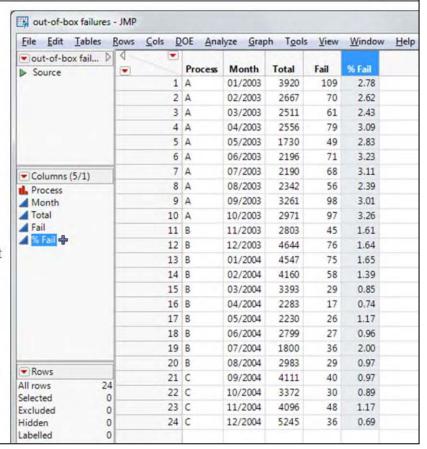
Data sets \ out-of-box failures

Plotting % fail

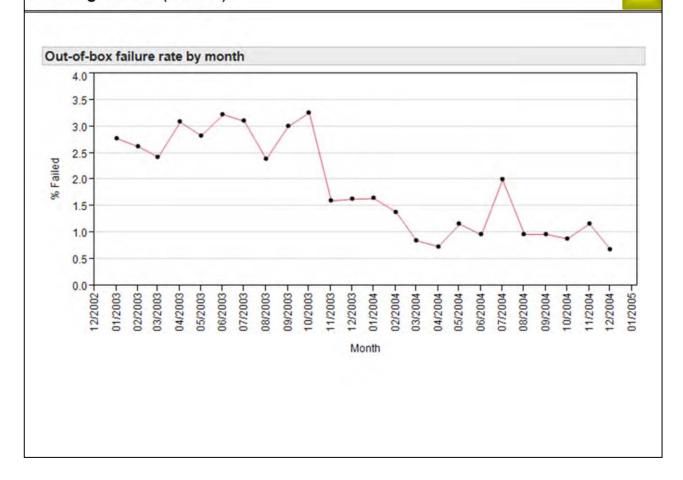
- 1. Create a new column called % Fail
- 2. Define it by the formula

$$\left(\frac{\text{Fail}}{\text{Total}}\right) \cdot 100$$

- 3. To edit decimal places: Right click column → Column Info → Format to Fixed Decimal and Dec = 2
- 4. Use *Graph* → *Legacy* → *Overlay Plot* to create the plot on the next slide



Notes			



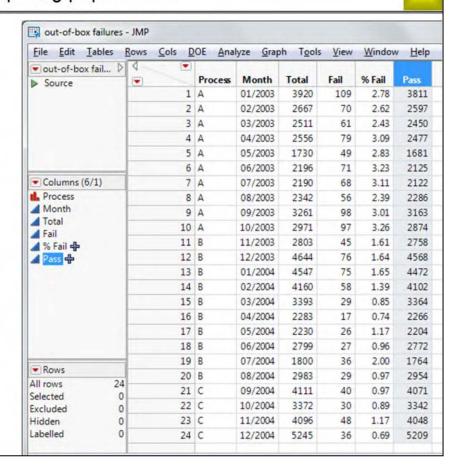
Notes			

Reformatting for comparing populations

1. Create a new column called *Pass* defined by the formula

Total - Fail

- 2. Go to *Tables* → *Stack*
- 3. Use Fail and Pass as the Stack Columns
- 4. See next slide

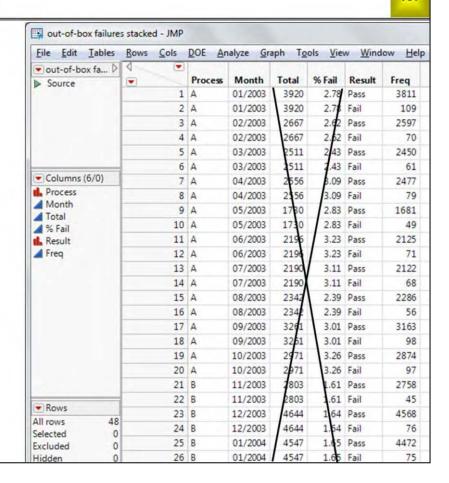


Notes			

Reformatting (cont'd)

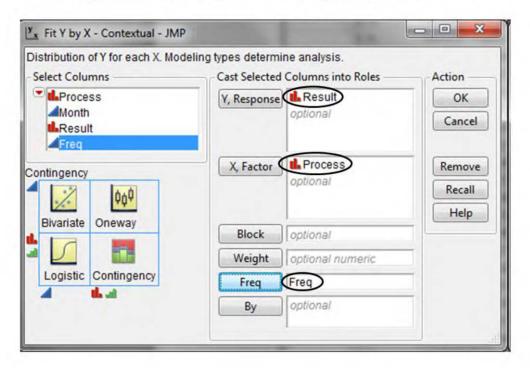
- 6. Change the name of the *Data* column to *Freq* and the *Label* column to *Result*
- 7. There are now two rows for each month. The *Total* and *% Fail* columns are no longer relevant, and may be deleted.
- Save the new data table as out-of-box failures stacked

Notes



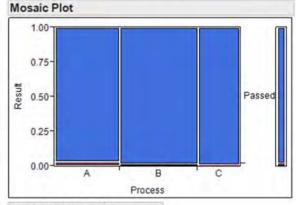
110103		
		_

Analyze \rightarrow Fit Y by $X \rightarrow$ set up as shown \rightarrow OK



Notes			

Data analysis (cont'd)



Contingency Table

		Re	sult	
	Count Row %	Failed	Passed	
	A	758 2.88	25586 97.12	26344
loces	В	418 1.32	31224 98.68	31642
1	С	154 0.92	16670 99.08	16824
		1330	73480	74810

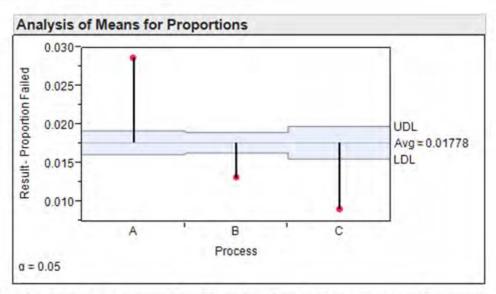
Tests

N DF -LogLike RSquare (U) 74810 2 141.17363 0.0211

Test ChiSquare Prob>ChiSq Likelihood Ratio 282.347 (-0.001* Pearson 291.850 (-0.001*

- Very strong evidence that processes
 A, B, and C do not all have the same failure rate
- The mosaic plot does not help us determine where the differences are
- Click on the red triangle at the top of the analysis window
- Select Analysis of Means for Proportions
- · See next slide

Notes			



- . This plot shows that Processes B and C are significant improvements over Process A
- · It does not tell us whether or not C is a significant improvement over B
- · Save your script, but don't close the data table.
- You may prefer to display the Result as Proportion Passed: Click on Red Triangle by Analysis of Means for Proportions and select Switch Response Level for Proportion

Notes			

Data sets \ molding process - stratification.

- a) Did JMP assign the correct modeling type for Machine?
- b) Go to Tables \rightarrow Summary \rightarrow use PN as the Group variable \rightarrow use Machine as the Subgroup variable \rightarrow OK.

₹ 10/0	PN	N Rows	N(01)	N(02)	N(03)	N(09)	N(10)	N(11)	N(13)	N(14)	N(15)
1	GV0098	43	0	0	0	0	0	0	0	11	32
2	GV0101	31	0	0	0	30	0	0	0	0	1
3	GV0119	42	3	0	39	0	0	0	0	0	0
4	GV0129	89	0	0	0	0	0	0	0	88	1
5	GV0132	64	0	64	0	0	0	0	0	0	0
6	GY0251	37	0	0	0	0	0	17	20	0	0
7	GY0298	31	0	0	0	24	7	0	0	0	0
8	GY0306	53	0	0	0	0	0	27	26	0	0
9	GY0325	36	1	0	0	0	0	34	1	0	0
10	KU0041	84	83	1	0	0	0	0	0	0	0

c) Note that each part number runs on only one or two of the machines. A comparison of part numbers could be biased by differences among the machines, and a comparison of machines could be biased by differences among the part numbers. Because of this, we should use the concatenated variable *PN-Machine* as the X variable in the analysis.

Notes			

Exercise 8.4 (cont'd)

d)	Reformat the data for comparing populations (follow steps 1 through 7 in the worked example).
e)	Test for significant differences among the <i>PN-Machine</i> groupings with respect to fraction defective. Give the P-value and interpret the results.
f)	Which three <i>PN-Machine</i> groupings would be the best focus for an improvement project? (Hint: highest fractions defective.)
g)	Save your script, save the data table as molding process - stacked, then close it.
	Notes
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Appendix: Reformatting Data for Pareto Analysis

- Data on defect types or failure reasons often is available only in tabulated form
- Each row may represent a production lot, work order, time period, machine work center, part number, . . . , or some combination thereof
- Common problem with tabulated data: wrong format for Pareto analysis

Notes			

Each row = Date, Machine, P/N, ...

	A	В	C	D	E	F	G	H	I	J
1	Date	Machine	P/N	Primary material	Primary lot #	Concentrate	Concen lot #	Regrind type	Parts palletized	Total defective
2	03-Apr-06	9	LSGV0101	CHEIL VE-1877S DrkGry	121642	NA	NA	25	120	7
3	03-Apr-06	11	LSGY0251	CHEIL VE-1877S Blk	101200	NA	NA	NA	300	17
4	03-Apr-06	15	LSGV0098	CHEIL HF1690H DrkGry	122930	NA	NA	8	372	18
5	04-Apr-06	2	LSGV0093	CHEIL VE-1877S DrkGry	121642	NA	NA	25	288	6
6	04-Apr-06	9	LSGV0101	CHEIL VE-1877S DrkGry	121642	NA	NA	25	600	2
7	04-Apr-06	11	LSGY0251	CHEIL VE-1877S Blk	101200	NA	NA	NA.	690	33
8	04-Apr-06	13	LSGY0307	CHEIL HF1690H LtGry	133232	NA	NA	NA	160	8
9	04-Apr-06	15	LSGV0098	CHEIL HF1690H DrkGry	122930	NA	NA	8	624	0
10	05-Apr-06	2	LSGV0102	CHEIL VE-1877S DrkGry	121642	NA	NA	25	120	15
11	05-Apr-06	11	LSGY0251	CHEIL VE-1877S Blk	101200	NA	NA	NA	650	15 21
12	05-Apr-06	13	LSGY0252	CHEIL VE-1877S Blk	101200	NA	NA	NA	300	18
13	05-Apr-06	13	LSGY0307	CHEIL VE-1877S LtGry	133232	NA	NA	NA	160	0
14	05-Apr-06	14	LSGY0308	CHEIL HF1690H LtGry	133232	NA	NA.	NA	240	25
15	05-Apr-06	15	LSGV0098	CHEIL HF1690H DrkGry	122930	NA	NA	8	336	17
16	06-Apr-06	2	LSGV0102	CHEIL VE-1877S DrkGry	121642	NA	NA	25	780	0
17	06-Apr-06	11	LSGY0251	CHEIL VE-1877S Blk	101200	NA	NA	NA	600	7
18	06-Apr-06	13	LSGY0252	CHEIL VE-1877S Blk	101200	NA	NA	NA	500	49
19	06-Apr-06	14	LSGV0130	CHEIL HF1690H DrkGry	122930	NA	NA	8	108	34
20	06-Apr-06	15	LSGV0099	CHEIL HF1690H DrkGry	122930	NA	NA	8	276	95
21	07-Apr-06	2	LSGV0102	CHEIL VE-1877S DrkGry	121642	NA	NA	25	300	0
22	07-Apr-06	2	LSGV0102	CHEIL VE-1877S DrkGry	121642	NA	NA	25	1020	5
23	07-Apr-06	11	LSGY0251	CHEIL VE-1877S Blk	101200	NA	NA	NA	360	6
24	07-Apr-06	13	LSGY0252	CHEIL VE-1877S Blk	387487	NA	NA	NA	200	16
25	07-Apr-06	13	LSGY0252	CHEIL VE-1877S Blk	387487	NA	NA	NA	700	7
26	07-Apr-06	14	LSGV0130	CHEIL HF1690H DrkGry	122930	NA	NA	8	72	0
27	07-Apr-06	14	LSGV0131	CHEIL HF1690H DrkGry	122930	NA	NA	8	120	17
28	07-Apr-06	15	LSGV0099	CHEIL HF1690H DrkGry	122930	NA	NA	8	180	0

Notes			

Total delective a cost per pe.	Total	defective	x Cost	per pc.
--------------------------------	-------	-----------	--------	---------

	K	L	M	N	0	P	Q	R	S	T	U	V	W	X	Y	Z	AA
1	Cost per	Total cost	Start- up	Sink	Flash	Weld	Flow	Short		Burn marks	Silver	Gas marks	Color/ carbon	Oil	Broken part	Scratches	Bubbles
2	\$2.89	\$20.25	3	0	0	0	0	0	0	0	4	0	0	0	0	0	0
3	\$5.08	\$86.43	4	0	0	0	0	4	0	0	0	0	0	0	0	0	9
4	\$11.10	\$199.76	0	0	0	0	0	6	0	0	12	0	0	0	0	0	0
5	\$2.69	\$16.12	6	0		0	0	0	0	0	- 0	0	0	0	0	0	0
6	\$2.89	\$5.79	0	0	0	0	0			0	2	0	0	0	0	0	0
7	\$5.08	\$167.77	0	4	0	0	0	2	0	0	0	0	0	0	0	2	0
8	\$3.55	\$28.44	8	0			0	0	0	0	0	0	0	0		0	0
9	\$11.10	\$0.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
10	\$4.13	\$62,00	6	6	0	0	0	3	0	0	0	0	0	0	0	0	0
11	\$5.08	\$106.76	0	17	0	0	0	3	0	0	0	0	0	0	0	. 0	1
12	\$4.96	\$89.28	. 8	0	0	0	0	0	0	0	0	0	0	0	0	1	9
13	\$3.55	\$0.00					0-		C	1	سميد	-C 1-	C4			V	0
14	\$8.97	\$224.36					Col	unts	ior e	each	type	of de	iect				0
15	\$11.10	\$188.66	U	U			U	12	U	U	- 5	U	U	U			0
16	\$4.13	\$0.00	0	0		0	0	0	0	0	0	0	0	0	0	0	0
17	\$5.08	\$35.59	0	2		0	0	4	0	0	0	0	0	0	0	1	0
18	\$4.96	\$243.04	3	15	0	0	0			0		0	0	. 0	0	4	27
19	\$10.33	\$351.07	8	0		0	0	14	0	0	12	0	0	0	0	0	0
20	\$14.19	\$1,347.62	56	30	0	0	0	0	0	0	9	0	0	0	0	0	0
21	\$4.13	\$0.00	0	- 0	0	0	0	0	0	0	0	0	0	0	0	0	0
22	\$4.13	\$20.67	5	0		0	0	0	0	0	0	0	0	0	0	0	0
23	\$5.08	\$30.50	4	0	0	0	0	0	0	0	0	0	0	0	0	0	2
24	\$4.96	\$79.36	0	14	0	0	0	0	0	0	0	0	0	0	0	1	1
25	\$4.96	\$34.72	0	0	0	0	0	0	0	0	0	0	0	0	0	0	7
26	\$10.33	\$0.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
27	\$15.15	\$257.56	8	0	0	0	0	0	0	0	1	0	0	8	0	0	0
28	\$14.19	\$0.00	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0

Notes			

Another thing we would want from a data set like this is a Pareto breakdown of defect types by total cost. It is not impossible to do this with the format shown above, but, once again, it would be extremely tedious compared to a pivot table.

Notes			

Small example

Open molding process - small (in JMP)

→ 7/0 Cols ▼	Total defective	Cost per pc.	Total cost	Start-up	Short shot	Silver	Bubbles
1	7	3	21	3	0	4	0
2	17	5	85	4	4	0	9
3	18	11	198	0	6	12	0

This is what we have

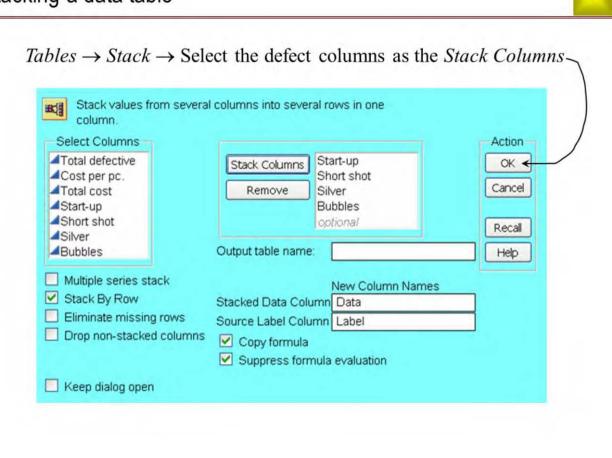
This is what we need \rightarrow

 \rightarrow How do we get there?

	470 Cois 💌				
	●12/0	Cost per pc.	Defect	Freq	Total cost
	1	3	Start-up	3	9
	2	3	Short shot	0	0
	3	3	Silver	4	12
	4	3	Bubbles	0	0
	5	5	Start-up	4	20
_	6	5	Short shot	4	20
	7	5	Silver	0	0
	8	5	Bubbles	9	45
	9	11	Start-up	0	0
	10	11	Short shot	6	66
	11	11	Silver	12	132
	12	11	Bubbles	0	0

Notes			

Stacking a data table



Notes		

Editing the columns

5/0 Cols 💌	1				
12/0	Total defective	Cost per pc.	Total cost	Label	Data
1	7	3	21	Start-up	3
2	7	3	21	Short shot	0
3	7	3	21	Silver	4
4	7	3	21	Bubbles	0
5	17	5	85	Start-up	4
6	17	5	85	Short shot	4
7	17	5	85	Silver	0
8	17	5	85	Bubbles	9
9	18	11	198	Start-up	0
10	18	11	198	Short shot	6
11	18	11	198	Silver	12
12	18	11	198	Bubbles	0

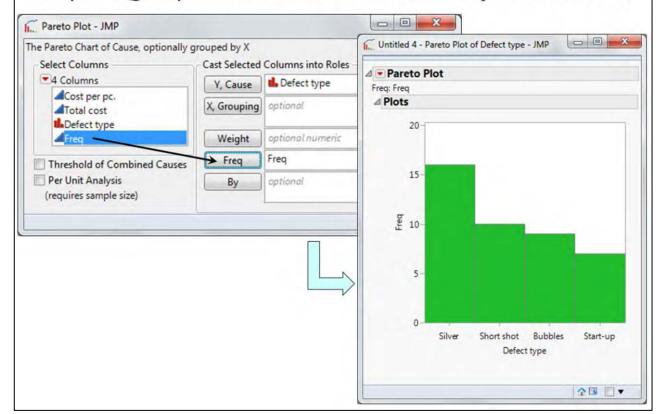
Total defective and Total cost are now incorrect row by row

- 1. Right-click on Data
- 2. Select Column Info
- 3. Rename as $Freq \rightarrow OK$
- 4. Rename Label as Defect type
- 5. Delete Total defective
- 6. Right-click on Total cost
- 7. Select Formula \rightarrow Cost per pc.*Freq
- 8. Save as molding data small stacked.xls

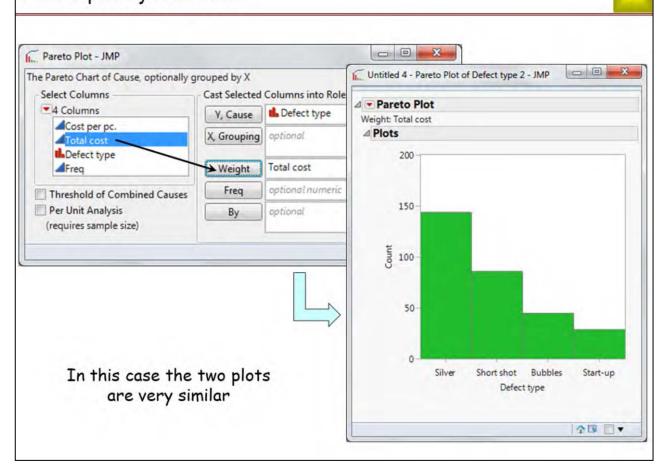
→ 4/0 Cols 💌				
400000	Cost per	Total	Defect	
●12/0	pc.	cost	type	Freq
1	3	9	Start-up	3
2	3	0	Short shot	0
3	3	12	Silver	4
4	3	0	Bubbles	0
5	5	20	Start-up	4
6	5	20	Short shot	4
7	5	0	Silver	0
8	5	45	Bubbles	9
9	11	0	Start-up	0
10	11	66	Short shot	6
11	11	132	Silver	12
12	11	0	Bubbles	0

Notes			

Analyze \rightarrow Quality and Process \rightarrow Pareto Plot \rightarrow set up as shown \rightarrow OK

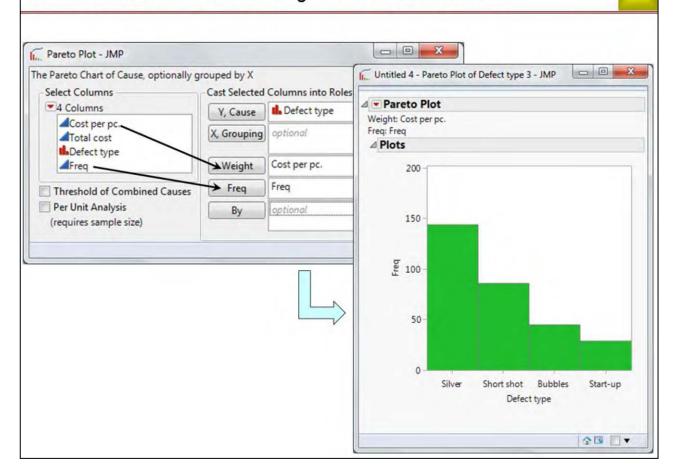


Notes			



Notes			

TAT 4



Notes			

Exercise: Appendix

Data sets \ molding process - Pareto.
Use the method described in this section to reformat the file for Pareto analysis. Save the reformatted file as <i>molding process - stacked</i> . Create Pareto plots of defect types by frequency of occurrence and total cost.
Notes

Lean Six Sigma Black Belt Volume II

Tab 2 Regression

Presented by



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www.etigroupusa.com

1 Introduction to Regression

Regression analysis is used to create an empirical model of the relationship between process inputs (x's) and outputs (y's).

- ➤ It is the method for analyzing designed experiments.
- ➤ It can also be used with historical data to help identify some factors for an experiment, or to develop an empirical model with that data.

Topics:

- Terminology
- · Purposes of regression analysis
- Data collection for use in regression analysis
- · The line of best fit
- · Simple Regression

Notes		

Terminology

- The term correlation is often used any time we speak of relating one variable to another
 - o Correlation is a measure of the relationship
 - An input/output relationship between the two variables is not required (for example, two variables measured at the same point in a process)
 - As a result, unrelated things can be "correlated." Remember, correlation does not prove causation.
- **Regression** analysis yields a model equation of the input-output relationship, Y = f(X), which can be useful in prediction
 - In the dataset, a series of inputs and their resulting output measures are aligned
 - o Regression is used to investigate and model the relationship

Notes			

The result of regression analysis is an empirical model, created from the data/observations, that can be used to:

- Understand and describe the relationship between Y and X's
- Predict Y from X's
- Determine best setting for X's (optimization)
- · Reduce variation in Y by controlling X's

Notes			

Data collection for use in regression analysis

Regression analysis is only as good as the data used.

Three basic sources of data are:

- Historical data (data that exists in routine collection systems)
- An observational study (data collected from uncontrolled processes for a specific purpose)
- A designed experiment (data from structured and controlled tests)

Regression analysis is a very big statistical topic and is commonly the analysis type for data from all three sources listed above.

Designs of experiments (DOEs) is the best strategy for many problems we are trying to solve as it is constructed to eliminate many of the problems that exist with the first two sources. However, historical and observational data is often easier to get and can still give powerful insights, although care must be taken with the analysis and conclusions drawn.

Notes			

Considerations when using historical data

Historical data is often plentiful and easily accessible.

It may be useful in identifying some variables that are critical to our process

However, there are several potential issues in using it:

- Some relevant data is not available, such as values of critical x's that are not recorded as part of the on-going process
- Reliability of the data is often questionable, including data being missing or lost
- The nature of the data is not helpful in solving the problem, as in situations
 when an x variable is controlled, so its impact cannot be seen in the
 regression analysis
- Often, data is used in ways that were not intended, such as using available data as a surrogate for what was really needed

Caution: We will not be able to cover the many aspects of creating and validating regression models from historical data in this course. If you choose to do this, proceed with caution! Better yet, get additional help.

Notes				

In an observational study, we would observe the process, with as little interaction or disturbance as possible, in order to obtain the data.

- With adequate planning, an observational study can yield accurate, complete, reliable data
- These studies can lead to ideas on what might be impacting the process
- However, these studies often provide limited information about specific relationships of interest, such as the impact of a variable that is tightly controlled in normal operation

Notes			

Simple linear regression refers to the case when there is only one regressor (variable) x used.

- · In simple regression, the model equation is for a best-fit line
- The form of the model equation created is:

$$Y = b_0 + b_1 x_1 + error$$

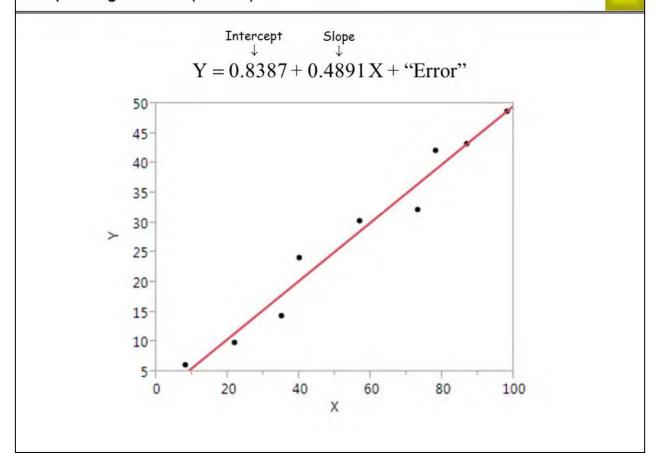
where b_0 is the intercept and b_1 is the slope of the line.

 This may remind you of your early algebra days, when you learned the equation for a line between two points:

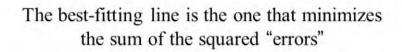
$$Y = mx + b$$

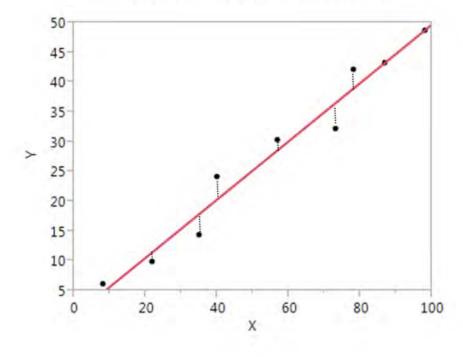
 Because there is variation (and more than two points to create the line), there will be scatter around the best-fit line determined by regression analysis.

Notes			



Notes			





	Notes
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- "Errors" are the vertical distances between each Y data value and the fitted line
- The line of best fit is the one that minimizes the sum of the squared errors
- This is the simplest example of least-squares model fitting
- The fitted line is often referred to as the predicted Y value

Notes			

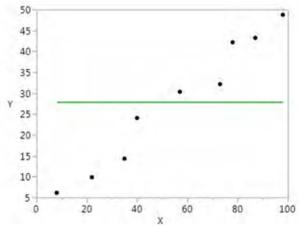
LSSV2 student files \ ANOVA linear fit Worksheet \ Prediction & error 1

4	A B C	D E	F	G	Н	1	J K L M N O P
1							
2	X data	Y data	- 1	Prediction		Error	Y = 27.9033 + 0.0000 X
3	8	6.16		27.90		-21.74	
4	22	9.88		27.90		-18.02	
5	35	14.35		27.90		-13.55	
6	40	24.06		27.90		-3.84	
7	57	30.34	=	27.90	+	2.44	
8	73	32.17		27.90		4.27	
9	78	42.18		27.90		14.28	
10	87	43.23		27.90		15.33	
11	98	48.76		27.90		20.86	
12	Sum of squares (SS)	8901.3	=	7007.4	+	1893.9	
13	Degrees of freedom (DF)	9	=	1	+	8	
14	Root mean square error (RMSE)					15.39	
15	A	V 27.00					
16 17	Average STDEV of						
- 1	OIDLVOI	, ,0.00					

Notes			

Finding the line of best fit (cont'd)

In this worksheet we ignore the X variable completely, and use the average value of Y as the prediction. This is just the calculation of the mean and standard deviation of the Y variable. (The values in cells I14 and E17 are the same.)



The sum of the squared errors (cell I12) can be dramatically reduced by using the X variable to "explain" more of the variation in the Y variable.

Notes			

	Work	csh	eet \ P	rea	liction	& e	error 2				
	A B C	D	E	F	G	Н		J K L	М	N O	Р
1											
2	X data		Y data		Prediction	r	Error	Y =	0.838	7 + 0.48	91 X
3	8		6.16		4.75		1.41				
4	22		9.88		11.60		-1.72				
5	35		14.35		17.96		-3.61				
6	40		24.06		20.40		3.66				
7	57		30.34	=	28.72	+	1.62				
8	73		32.17		36.54		-4.37				
9	78		42.18		38.99		3.19				
10	87		43.23		43.39		-0.16				
11	98	L	48.76		48.77		-0.01				
12	Sum of squares (SS)		8901.3	=	8838.0	+	63.3				
13	Degrees of freedom (DF)		9	=	2	+	7				
14	Root mean square error (RMSE)						3.007				
15 16	Average	Y	27.90								
17	STDEV of		15.39				on of to				d
18	Adjusted R squa	re	0.962			у ("	explaine	a by	^ vario	ilon	

Notes			

N = total sample size

G = number of parameters in the equation

= DF for the prediction column

N-G = DF for the error column

- The Error DF is more important than the Prediction DF
- It determines the accuracy of the predicted values
- When DF is mentioned without a qualifier, it usually means Error DF

	Notes
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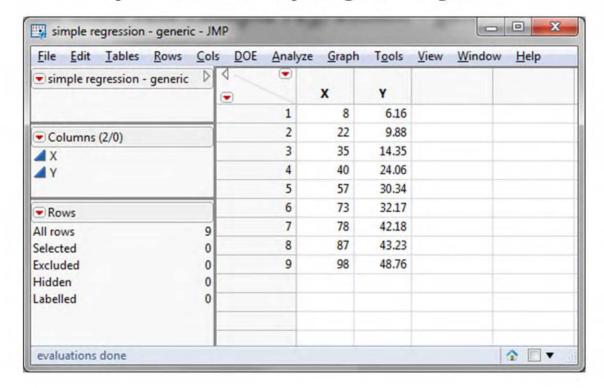
Steps in Simple Regression

- Run Analyze > Fit Model in JMP to investigate the relationship between y and x
- Check the p-value for the fit to determine whether the regression is significant. If not, then no need to go further.
- 3. If the regression is significant, determine the strength of the relationship, using the $Adjusted R^2$
- 4. Check model adequacy by reviewing the residuals plots
 - Residual Normal Quantile Plot
 - Residual by Predicted Plot
 - Studentized Residuals (in run order)

We'll go through these steps and additional analysis details, for simple regression in the following example.

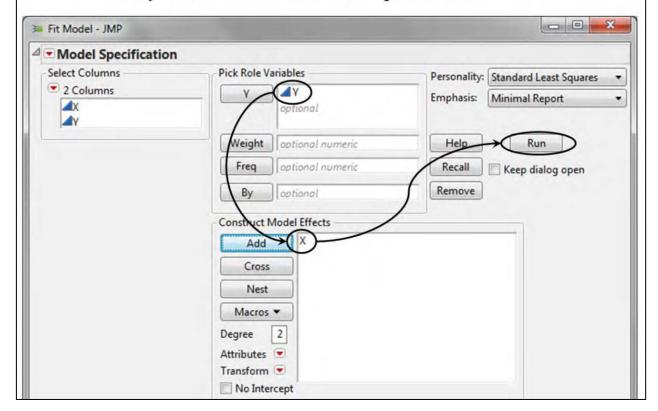
Notes		

Open: Data sets \ simple regression - generic



Notes			

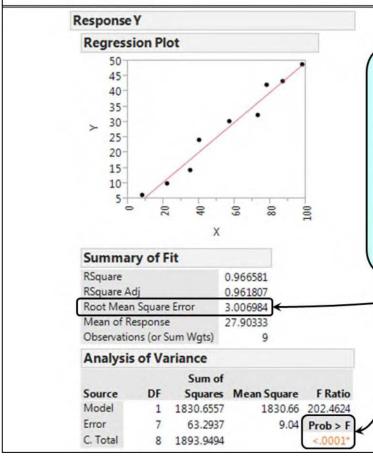
$Analyze \rightarrow Fit\ Model \rightarrow Set\ up\ as\ shown \rightarrow Run$



Notes			

Analysis details

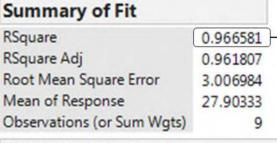
Notes



- The Root Mean Square Error (RMSE) is the standard deviation of Y caused by factors other than X
- It can be thought of as the standard deviation about the fitted line (or model)
- Also known as the "error" or "residual" standard deviation
- · Smaller is better
 - **P-value** indicates whether the regression is significant
 - This low p-value shows that it is significant

- 1000			

Analysis details (cont'd)



Analysis of Variance

Source	DF	Squares	Mean Square	F Ratio
Model	1	1830.6557	1830.66	202.4624
Error	7	63.2937	9.04	Prob > F
C. Total	8	1893.9494		<.0001*

• Proportion of the variation in Y that is "explained by" variation in X.

 R^2

"Coefficient of

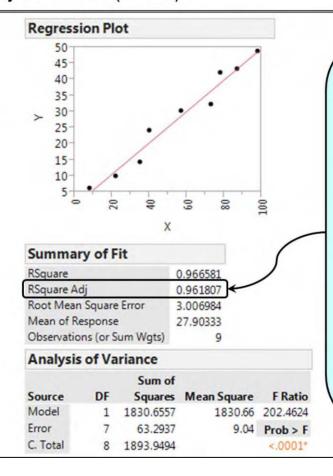
Determination"

- Varies from 0 to 1.
- Larger is better
- Unitless

Notes			

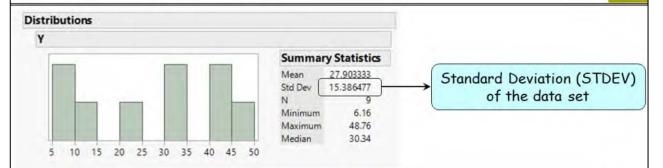
Analysis details (cont'd)

Notes



- Adjusted R² also gives us the proportion of Y variation explained by the model (a line in simple regression)
- · Varies from 0 to 1
- · Larger is better
- Always use the Adjusted R² value, not R²
- Adjusted R² takes the number of model terms into account and penalizes for including insignificant terms
- In this example, the simple regression model explains much of the variation in Y.

110165	



$$R^2 = 1 - \frac{SS_{Error}}{SS_{Total}}$$

$$R_{Adj}^2 = 1 - \frac{SS_{Error}/(n-p)}{SS_{Total}/(n-1)} = 1 - \left(\frac{RMSE}{STDEV}\right)^2$$

p = number of terms in the model (including the intercept)

n = sample size (number of measurements in the data set)

 SS_{Total} is the sum of squares of the data (measurements in the data set)

 SS_{Error} is the sum of squares of the Errors or residuals

We saw the sum of squares calculations earlier, in the ANOVA

Notes			

There is a potential problem with R^2 :

- R² always increases when terms are added to a model, even when the terms are not significant
- This is particularly a problem in multiple regression, as it can lead to "overfitting," giving false confidence in using the model, especially for prediction.
- Adjusted R² corrects for this by considering the number of terms in the model
- Adjusted R² can actually decrease if non-significant terms are added to a model

Adjusted R² is the recommended statistic for determining the proportion of variation in Y explained by the model

Notes			

P-values for the ANOVA and individual model parameters

Red triangle next to Response $Y \rightarrow Regression Reports \rightarrow Parameter Estimates$

Analysis of Variance					
Source	DF	Sum of Squares	Mean Square	F Ratio	
Model	1	1830.6557		202,4624	
Error	7	63.2937	9.04	Prob > F	
C. Total	8	1893.9494		<.0001*	

Parameter Estimates					
Term	Estimate	Std Error	t Ratio	Prob> t	
Intercept	0.8386661	2.150023	0.39	0.7081	
X	0.4891205	0.034375	14.23	<.0001*	

- In regression of Y on a single X, the Analysis of Variance P-value is the same as the P-value for the slope of the line.
- The P-value for the slope of the
 line indicates the evidence of a correlation between Y and X.
- Significance of individual model terms are determined by testing whether their regression coefficient is equal to 0, using the t statistic. Hypotheses are:

$$H_0$$
: $b_i = 0$
 H_1 : $b_i \neq 0$

 This is a test of the contribution of the model term, given the other terms in the model.

Notes			

Estimates and P-values for the slope and intercept X Parameter Estimates Std Error t Ratio Prob>|t| 0.8386661 2.150023 0.39 0.7081 0.4891205 0.034375 14.23 0.001*

Model:
$$Y = 0.84 + 0.50X + error$$

- In this example, the P-value for the slope of the line indicates very strong evidence of a correlation between Y and X.
- The P-value for the Intercept indicates that it is not significant.
 - Best practice is to leave the Intercept in the model, whether or not the P-value indicates that it is significant
 - Regression equations are developed, and are only valid, over the region of the regressor variables (x's) contained in the data set
 - o Forcing the model to pass through (0, 0) by removing the intercept, can create problems in the region being modeled

Notes			

Using Adjusted R2 and p-values

Both the Adjusted R^2 and the p-values must be considered, in order to understand what has been learned in the analysis.

When the resulting model has:

- High Adjusted R² and significant model term p-values, this is ideal.
 Factors driving the response have been identified and the variation is largely explained. A decent model has been created.
- Low Adjusted R² and significant model term p-values, more work must be
 done. Some significant factors influencing the response have been identified,
 but the low Adjusted R² indicates that other important factors exist. These need
 to be found, for the model to be useful.
- High R² and insignificant model terms, this is usually due to the data
 violating the assumptions of the regression analysis. There is more information
 on this scenario in upcoming slides.
- Low Adjusted R² and insignificant model terms, no relationship between X and Y variables have been found. Usually this means that new ideas about which factors influence Y must be developed, although it can occasionally be due to missing higher order terms.

Notes			

2 Checking Model Adequacy

In least squares fit regression (continuous Y), the analysis methods used to calculate regressor coefficients and their p-values, depend on certain assumptions being met.

Assumptions:

- Errors (residuals) are normally and independently distributed with mean zero and constant variance (σ^2)
- Observations are adequately described by the model

Whether performing regression from "file cabinet" data or analyzing the results of a designed experiment, these assumptions must be validated.

Notes			

To validate that these assumptions have been met, the *residuals* are examined:

1. Normal Probability Plot of Residuals

- Validate that the residuals are normally distributed
- In JMP, this is the Residual Normal Quantile Plot

2. Residuals vs. Predicted (or Fitted) Values

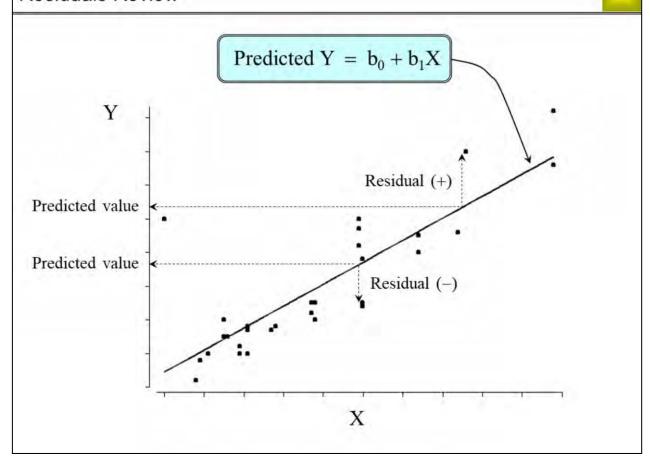
- Validate constant variance and mean 0
- In JMP, this is the Residual by Predicted Plot

3. Residuals vs. Run Order

- Verify independence of errors
- There should be no patterns over the timeframe of the data
- In JMP, the best graph to use is Studentized Residuals
- The JMP data <u>table must be in run order</u> for *Studentized Residuals* to graph the residuals in run order

Notes			

Residuals Review



Notes			

A fitted model, the equation generated during regression, gives the predicted mean value of the response variable as a function of the predictor variables. These predicted mean values are also called *predicted values*, or just *predicted* for short. The *residual value* is the data (observation) value minus the predicted value. Residual values are called *residuals* for short.

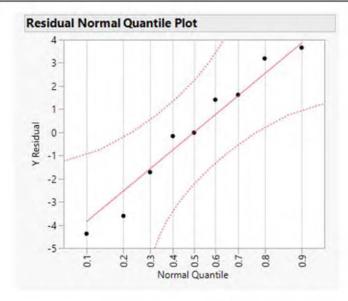
These terms are easiest to visualize in the simple linear model shown above. A predicted value is the fitted line evaluated at some X value. A residual is the difference between a measured (observed) Y value and the predicted value at the corresponding X.

Residuals contain information about the magnitude and direction of variability in the data relative to the fitted model.

- An unusually large residual might signal a measurement error, data entry error or some other type of outlier.
- A systematic trend or pattern in the residuals might signal an inadequacy in the fitted model.

Notes			

Residual Analysis



In viewing the Residual Normal Quantile Plot for the *simple regression-generic*, we can see whether the residuals are normally distributed.

Notes			

If residuals are normally distributed, the plot will be approximately a straight line.

Emphasis should be on the central values of the plot, rather than the ends

It is common for plots to bend upward at the high end and downward at the low end.

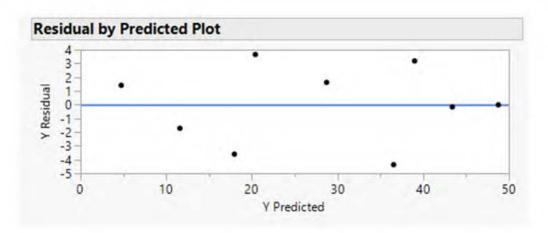
Small sample sizes, such as from experiments, often appear more non-normal

Use the "Fat Pencil" Rule: If a "fat pencil" placed over the central points would cover them on the plot, then the residuals are approximately normal (good enough). Hyperbolic bands displayed in JMP plots give these bounds.

A curve throughout the plot is a strong indication of non-normality. In this case, a transformation would be needed.

The plot above shows an error (residuals) distribution that is approximately normal, so it is not concerning.

Notes			



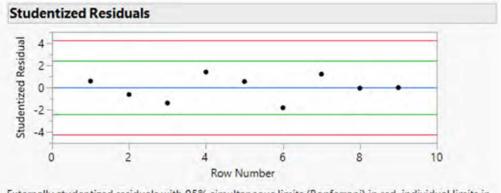
In viewing the Residual by Predicted Plot for the *simple regression-generic*, we can see whether the residuals have constant variance and mean 0.

Notes			

24	
24	
-2.4	

Notes	34
Here the residuals are plotted against the predicted values. This is a good all-aroun diagnostic plot.	d
"Healthy" residuals look like random scatter around 0. There should be no obvious patterns. The amount of "scatter" or variance (how high and low the plot goes) should be consistent across the graph. This verifies the assumption of constavariance. If the variance is increasing or decreasing across the graph, a transformat is needed.	nt
Notes	

Residual Analysis (cont'd)



Externally studentized residuals with 95% simultaneous limits (Bonferroni) in red, individual limits in green.

In viewing the Studentized Residuals for the *simple regression-generic*, the best form for checking residuals by run order, we can see whether there are any patterns over the timeframe of the data.

Note that the data table must be in run order for this plot.

Notes			

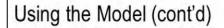
votes
Again, on this graph, healthy residuals look like a random scatter around 0.
Runs (points in a row) of positive-negative-positive-negative residuals indicate correlation between runs. This implies that the assumption of independence has been violated. In designed experiments, randomization protects against this! Do it every time!
This plot can also show a change in variance over the time span of the experiment. This could be due to increased skill as the experiment progresses, a process drift, operator fatigue, tool wear, etc. This type of problem would show as an increase or decrease in spread or "scatter" of the residuals across the graph. Increasing or decreasing variance indicates the need for a transformation.
Notes

3 Using the Model: RMSE and Prediction Profiler

In this section, we'll see how we can:

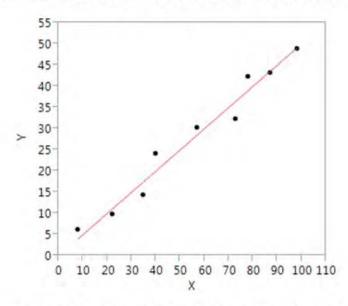
- Use the Root Mean Square Error (RMSE) in predicting our future process variation,
- Use JMP's Prediction Profiler to help us optimize our process, and
- Estimate our future % defective, using the t distribution calculator.

Notes			



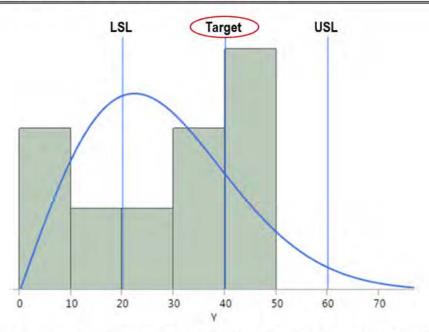
38

When Y is correlated with a controllable X variable,



how can we use the regression to improve the Y capability?

N	0	tes	5

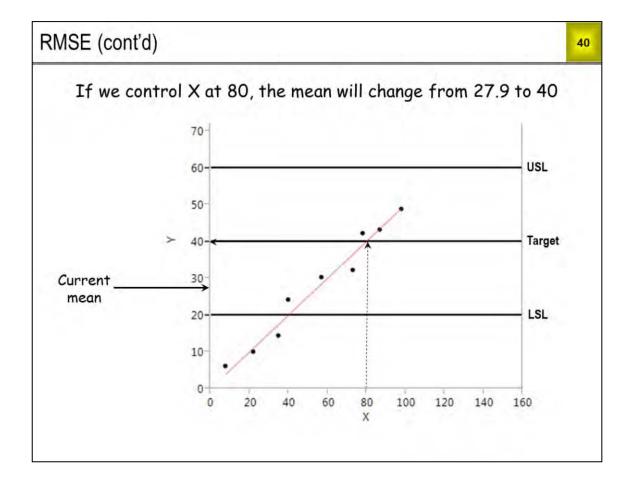


Suppose we are not happy with our current process capability Mean = 27.9, Std dev = 15.4

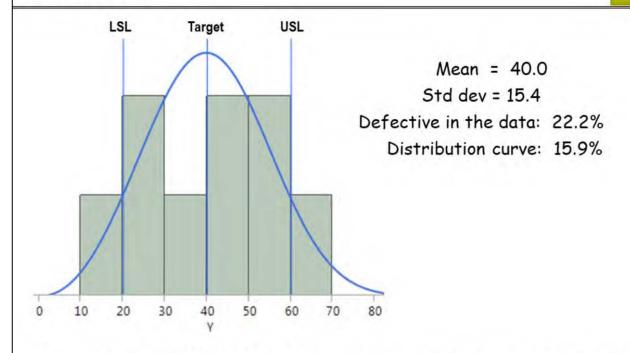
Defective in the data: 33.3%

Predicted from distribution curve: 35.8%

Notes			



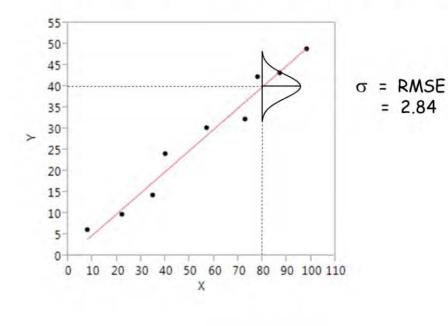
Notes			



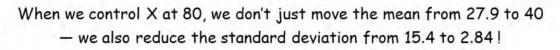
- Moving mean Y to the center of the spec range does reduce % defective
- Is the mean the only thing that changes when we control X at 80?

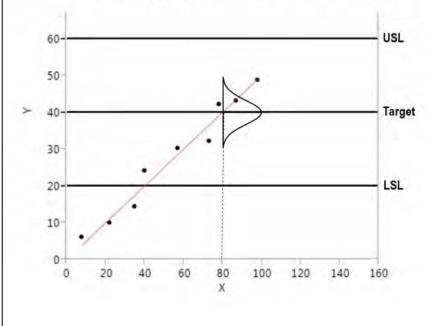
Notes			

By definition, RMSE is the standard deviation of Y that would result from eliminating the variation in \boldsymbol{X}



Notes			

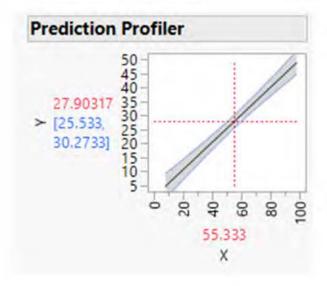




Notes			

4. Introduction to the Prediction Profiler

JMP's Prediction Profiler helps us use our regression model to make predictions and optimize our process.



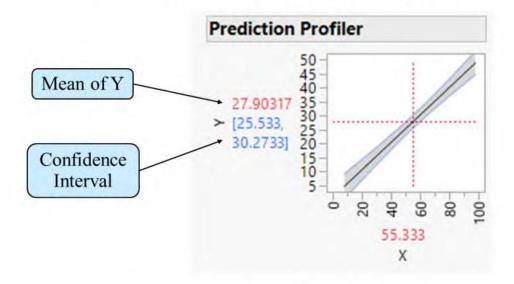
Follow these steps to access the prediction profiler:

Analyze > Fit Model > Y = Y,
 Model Effects = X > Run > Red
 Triangle > Factor Profiling >
 Profiler

Notes			

Introduction to the Prediction Profiler (cont'd)

JMP's Prediction Profiler helps us use our regression model to make predictions and optimize our process.



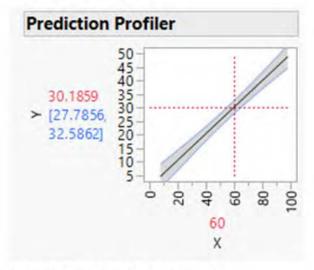
- Calculates predicted mean Y as a function of X
- · Calculates confidence intervals for predicted means

Notes			

Simple example of prediction of Mean Y

Continuing with the simple regression-generic data:

- Suppose we are interested in the predicted mean Y for X = 60
- Click on the 55.333, change it to 60

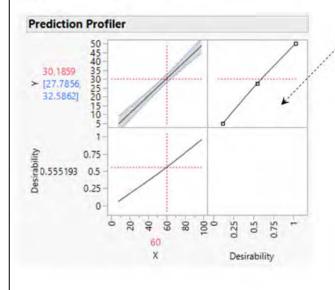


- Predicted mean Y (based on the data) is 30.19
- With 95% confidence, the population mean lies between 27.79 and 32.59

Notes			

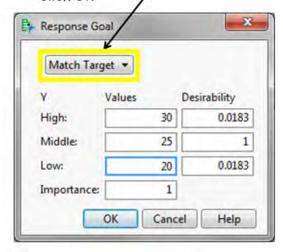
Simple example of optimization

- Suppose we want to find the X value that predicts a mean Y value of 25
- Red triangle next to Prediction Profiler → Optimization and Desirability → Desirability Functions



Notes

- Double click in here (don't touch the line plot)
- · Modify the Response Goal dialog as shown below
- · Click OK

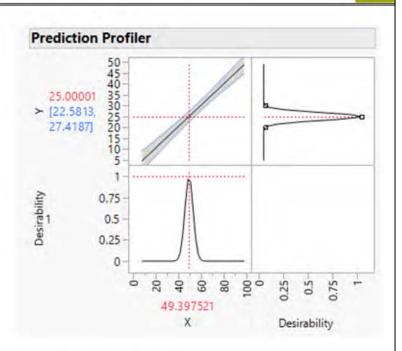


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Red triangle
next to
Prediction Profiler

↓
Optimization and Desirability

↓
Maximize Desirability



- Predicted mean Y of 25 is achieved when X = 49.4
- With 95% confidence, this population mean lies between 22.6 and 27.4

Notes			

- The 95% Confidence Interval on the Mean Response gives the range which will contain the "true" mean, μ , 95% of the time
 - · For a sample, the confidence interval is calculated:

$$\bar{Y} - t_{.025,n-1} \frac{s}{\sqrt{n}} \le \mu \le \bar{Y} + t_{.025,n-1}$$

- For a regression, calculation of the confidence interval is similarly structured, but considerably more complicated, involving matrix math.
- A 95% Prediction Interval gives the range which will contain future individual response observations 95% of the time.
 - The prediction interval is wider than the confidence interval, because it is to contain individual measurements, not averages.
 - Calculation of this interval is complicated, involving matrix math.

Notes		

a)	Continuing with <i>simple regression-generic</i> , find the X value that predicts a mean Y value of 35. Give the confidence limits for the predicted mean.
b)	The overall standard deviation of Y is 15.39. The RMSE from the regression is 2.84. Which of these would be the standard deviation of Y if we controlled X to a constant value?
c)	Save your script, close and save the data table.
	Notes

	CTOISC T.Z					
Da	ta sets \ production vs capacity.					
(a)	Fit a regression for <i>Production qty</i> as a function of <i>Capacity utilized</i> (%) (using <i>Model</i> , of course). Is there a correlation? Give the appropriate P-value and stren of evidence.					
(b)	For this exercise, we will not review the residuals plots. Use your model to find the capacity utilization level that predicts a mean daily production quantity of 3500. Give the confidence limits.					
(c)	The overall standard deviation of <i>Production qty</i> is 733.5 (not shown in Fit Model output—calculated in Distribution Platform). The RMSE from the analysis in (a) is 409.732. Which of these would be the standard deviation if capacity utilization was held constant?					
(d)	Save your scripts, close and save the data table.					
	Notes					

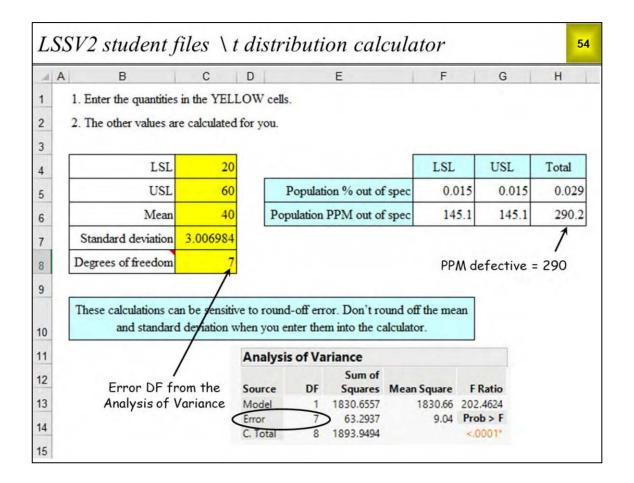
Estimating Improved % Defective

Once we determine the level at which we want to control our x, we can use the root mean square error (RMSE) and other regression results to estimate the % defective in the improved process.

Remember that by definition, the RMSE is the standard deviation of the improved process, with x's held at desired levels.

The *t distribution calculator* helps us calculate the future % defective.

Notes			



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Notes

Data sets \ production vs capacity.jmp.
In this process data, on 75% of the days production quantity fell below 3000.
Based on the best fit distribution, the Lognormal, the expected % of days that production quantity will fall below 3000 is 71.8%.
a) We found earlier that capacity utilization 52.1% gives a mean daily production quantity of 3500. The RMSE was 409.7, the error degrees of freedom was 34. Assuming 52.1% capacity utilization, use the <i>t distribution calculator</i> to find the predicted % of days on which production quantity will be less than 3000.
b) Save your scripts, close and save the data table.
Notes

Open Data sets \ outgassing process. Current (the Y variable) is the current required to heat a filament to a target temperature. Resist (the X variable) is the electrical resistance of the filament. Machine is the processing unit. This example shows how to reduce % defective by separate optimization of each machine.

- a) For this process, the % of *Current* data values that fall outside the interval (1.9, 2.1) is 8.87%.
- b) Fit a regression for *Current* as a function of *Resist*, using *Machine* as the *By variable*. For each machine, give the RMSE, the error degrees of freedom, and the resistance that predicts a mean current of 2.

Machine	RMSE	DF	Resistance	% Outside
A				
В				
C				

- c) Assuming we use the indicated resistance values, use the t distribution calculator to find for each machine the % of Current values predicted to fall outside the interval (1.9, 2.1).
- d) Save your scripts, close and save the data table.

Notes			

5 Multiple Regression

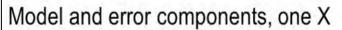
- Multiple regression model
- Examples
- Fitting regression models
- · Interactive effects
- · Predicted values and uncertainty
- Modeling and optimization

Notes			

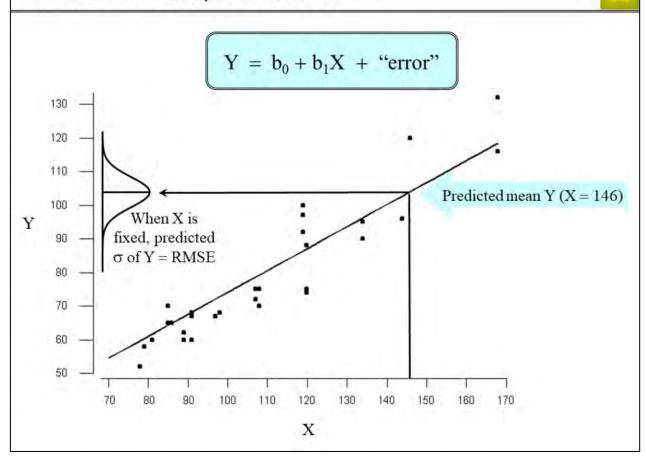
$$Y = b_0 + b_1 X_1 + b_2 X_2 + ... + b_k X_k + "error"$$

Y	X_1, X_2, \ldots, X_k	b_0	b_1, b_2, \ldots, b_k	"Error"
Dependent variable	Independent variables	Intercept	Regression coefficients	Residuals Mean = 0
Response variable	Explanatory variables	Parameter	Parameters	Standard deviation = σ (RMSE)
Output	Inputs			Distribution = Assumed to be Normal
	Predictors			
	Regressors			
	Factors (in DOE)			

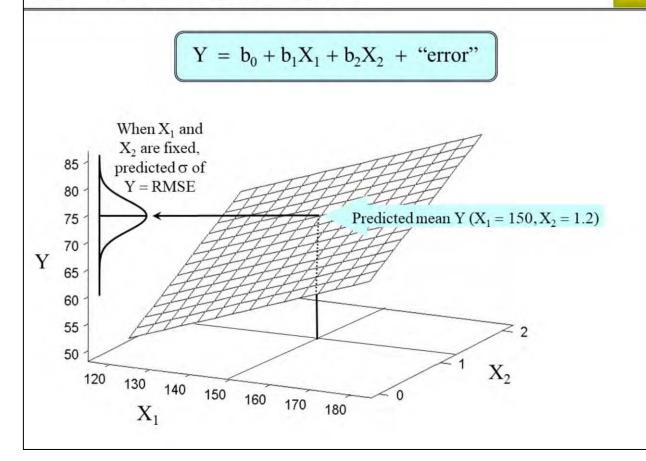
Notes			







Notes			



Notes			

Multiple regression examples

Y	X ₁	X ₂	X ₃	X ₄	X ₅
Life of cutting tool	RPM	Tool type	Material	Feed rate	
MPG	Displace- ment	Horsepower	Weight		
Salary	Education	Experience	Performance	Seniority	Gender
Vending machine service time	Amount of product stocked	Distance from truck to machine			

Fill in examples of interest to you

Notes			

Y	X ₁	X ₂	X ₃	X ₄	X ₅
MPG	Displacement (D)	Horsepower (H)	Weight (W)		

$$MPG = b_0 + b_1D + b_2H + b_3W + error$$

Y	X ₁	X ₂	X ₃	X_4	X ₅
Bond strength	Temperature (T)	Dwell time (D)	$T \times D$	T ²	D^2

Bond =
$$b_0 + b_1T + b_2D + b_3TD + b_4T^2 + b_5D^2 + \text{error}$$

Response surface model (RSM) with two continuous Xs.

TD is the interaction term for T and D, T^2 and D^2 show curvature.

Notes			

Nonlinear model	Equivalent linear model
$Y = b_0(X_1)^{b_1}(X_2)^{b_2}$	$log(Y) = log(b_0) + b_1 log(X_1) + b_2 log(X_2)$
$Y = b_0 (b_1)^{X_1} (b_2)^{X_2}$	$log(Y) = log(b_0) + log(b_1)X_1 + log(b_2)X_2$

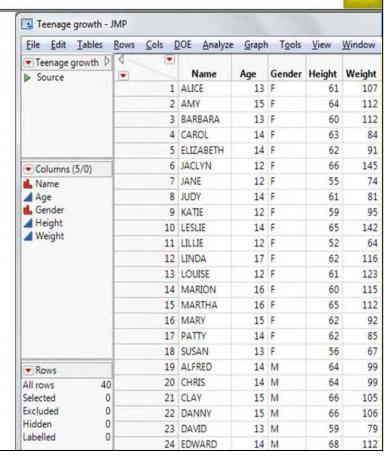
- In many cases, log(Y) transformations can successfully linearize nonlinear regression models
- This greatly extends the application of standard multiple regression models

_N	lotes			

Fitting regression models

Data sets \ teenage growth

Y	X_1	X_2
Height	Age	Gender
Weight	Age	Gender

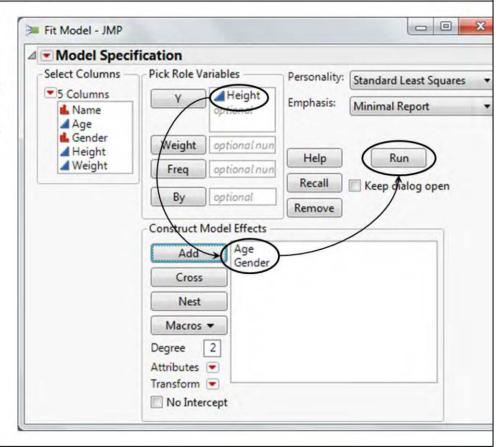


Notes				

Say we want to model *Height* as a function of *Age* and *Gender*

Analyze

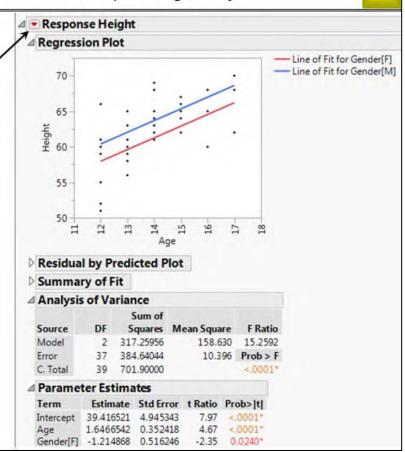
↓
Fit Model



Notes			

How to change options (for Fit Model) during analysis

- Alt-click on Response
 Height red triangle (This technique works for may JMP platforms)
- Set up as shown on next slide

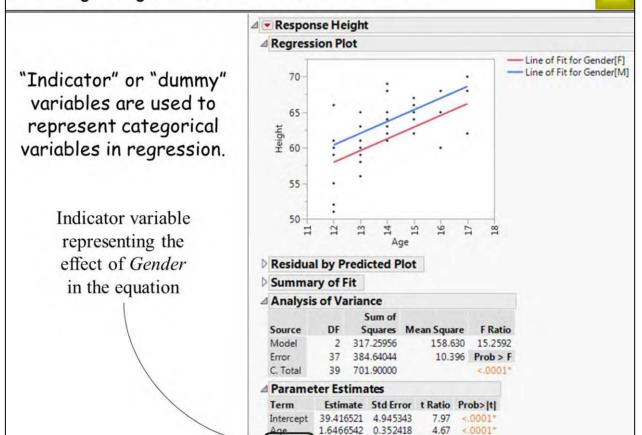


Notes			

Default options for Fit Model (cont'd)

Regression Reports	☐ Inverse Prediction	Row Diagnostics
✓ Summary of Fit	Parameter Power	✓ Plot Regression
✓ Analysis of Variance	Correlation of Estimates	✓ Plot Actual by Predicted
✓ Parameter Estimates	Effect Screening	☐ Plot Effect Leverage
✓ Effect Tests	Scaled Estimates	✓ Plot Residual by Predicted
✓ Effect Details	Normal Plot	☐ Plot Residual by Row
Lack of Fit	☐ Bayes Plot	✓ Plot Studentized Residuals
☐ Show All Confidence Intervals	Pareto Plot	✓ Plot Residual by Normal Quantile
☐ AICc	Factor Profiling	Press
Estimates	✓ Profiler	Durbin Watson Test
Show Prediction Expression	Cube Plots	
Sorted Estimates	☐ Box Cox Y Transformation	n .
Expanded Estimates	Surface Profiler	
☐ Indicator Parameterization Estima		
		In the last column on the
Sequential Tests	The state of the s	
☐ Sequential Tests ☐ Custom Test	The state of the s	right (not shown), select
	The state of the s	
Custom Test	The state of the s	right (not shown), select
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Custom Test Multiple Comparisons	The state of the s	right (not shown), select
Custom Test Multiple Comparisons	The state of the s	right (not shown), select
Custom Test Multiple Comparisons	The state of the s	right (not shown), select

Handling categorical X variables in the model



Gender[F]

Notes

-1.214868 0.516246 -2.35 0.0240*

110103			
-			
	-		

In JMP, two-level categorical factors are coded +1 and -1

Gender[F] =
$$\begin{cases} +1 & \text{if Gender is F} \\ -1 & \text{if Gender is M} \end{cases}$$

Height =
$$b_0 + b_1 Age + b_2 Gender[F]$$

=
$$\begin{cases} b_0 + b_2 + b_1 Age & \text{if Gender is F} \\ b_0 - b_2 + b_1 Age & \text{if Gender is M} \end{cases}$$

This results in one equation for Females and one equation for Males, with equal slopes (b_1) and different intercepts $(b_0 + b_2)$ and $(b_0 - b_2)$.

An additional indicator variable is added for each additional level of a categorical variable.

Notes			

Residual by Predicted Plot Summary of Fit Height = 39.42 + 1.65 Age -1.21 Gender[F]

Analysis of Variance

Sum of Source DF Squares Mean Square **FRatio** 17.25956 Model 158.630 15.2592 Error 37 384.64044 10.396 Prob > F 701.90000 C. Total 39 <.0001* Parameter E timates

Term Estimate Std Error t Ratio Prob>|t| 39.416521 4.945343 7.97 Intercept <.0001* 1.6466542 0.352418 4.67 <.0001* Age Gender -1.2148680.516246 -2.35 0.0240*

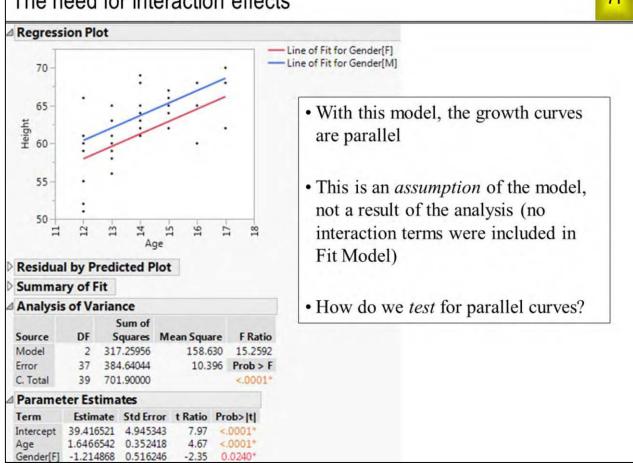
If you want to verify the equation:

▼ Response Y→ Estimates

→ Show Prediction Expression

Notes

The need for interaction effects



Notes				

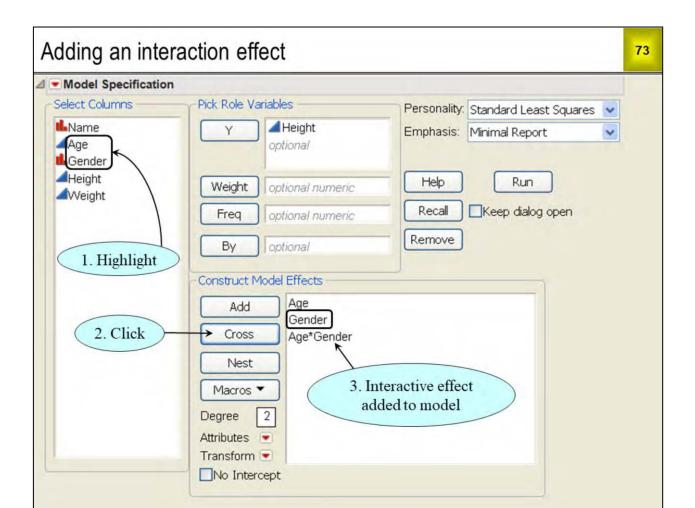
Height =
$$b_0 + b_1 Age + b_2 Gender[F]$$

+ $b_3 Age * Gender[F]$

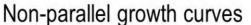


This product term allows different slopes for M and F

Notes			

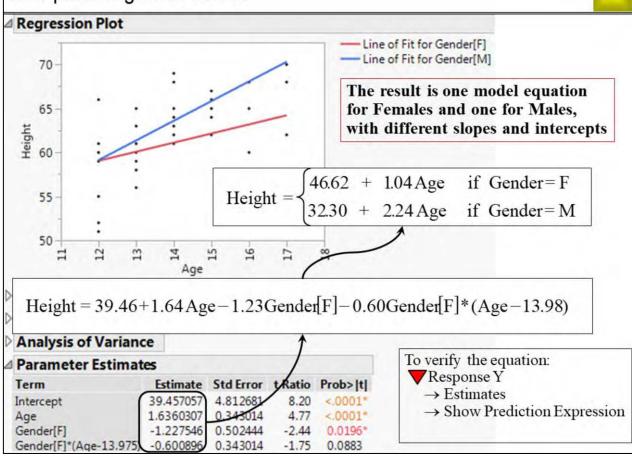


Notes				

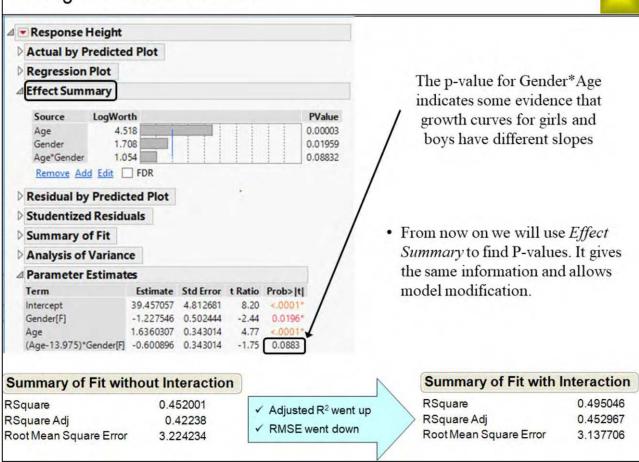


Notes

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Testing the interaction effect



Notes			

Residuals Review Predicted $Y = b_0 + b_1 X$ Residual (+) Predicted value Predicted value Residual (-) X

Notes			

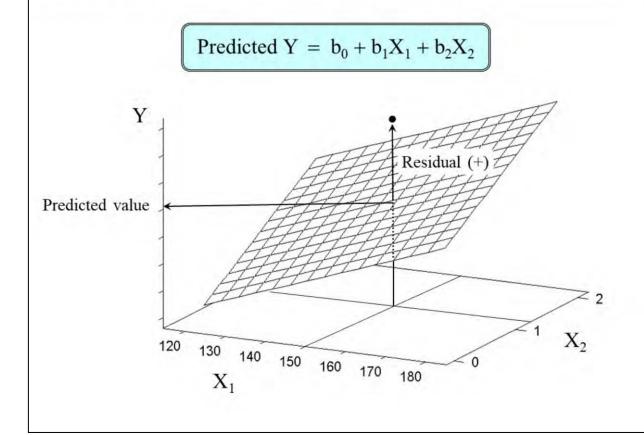
A fitted model, the equation generated during regression, gives the predicted mean value of the response variable as a function of the predictor variables. These predicted mean values are also called *predicted values*, or just *predicted* for short. The *residual value* is the data (observation) value minus the predicted value. Residual values are called *residuals* for short.

These terms are easiest to visualize in the simple linear model shown above. A predicted value is the fitted line evaluated at some X value. A residual is the difference between a measured (observed) Y value and the predicted value at the corresponding X.

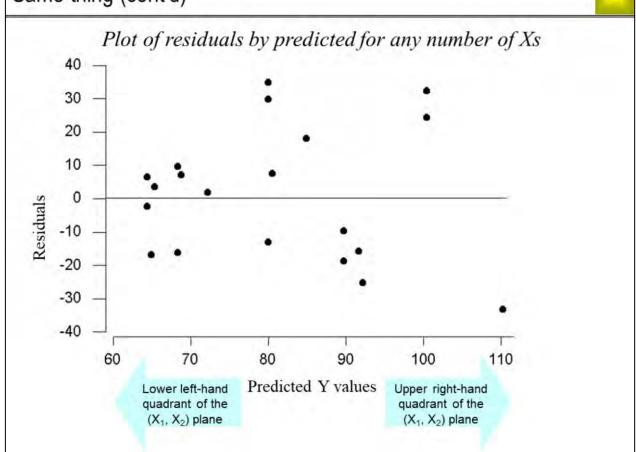
Residuals contain information about the magnitude and direction of variability in the data relative to the fitted model.

- An unusually large residual might signal a measurement error, data entry error or some other type of outlier.
- A systematic trend or pattern in the residuals might signal an inadequacy in the fitted model.

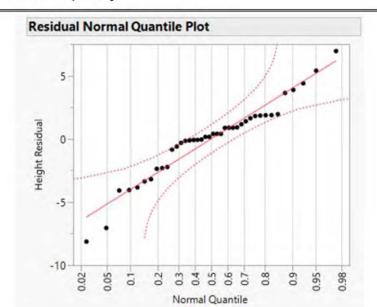
Notes			



Notes			

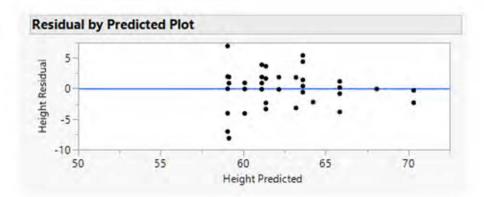


Notes			



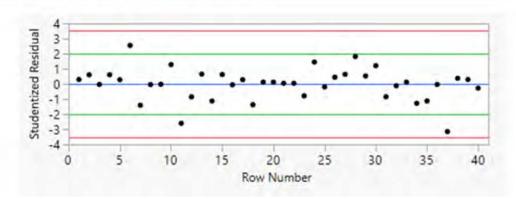
We can see points on the hyperbolic bands here, but there is not an obvious curve through the data. Given the small sample size, this is not too concerning.

Notes			



In this plot, we can see that the variance in the residuals is decreasing as height increases. This indicates the need for a transformation. We will see how to do this a little later in the course.

Notes			



There are no obvious patterns in residuals in run order, and they scatter about zero.

There is no concern here.

(Points outside the red limits are considered outliers, and should be investigated. Points outside the green limits but inside the red limits are possibly outliers, but with less certainty.)

Notes			

Variance Inflation Factor (VIF)

When historical or observational data is used to generate a regression model, an additional test is needed:

- The variance inflation factor (VIF) must be checked
- The VIF indicates whether the regressors (i.e. Xs or predictors) are correlated with each other
 - VIF = 1: regressor is independent of all other regressors
 - \succ 1 ≥ VIF ≥ 5: regressor is moderately correlated to other regressors
 - VIF > 5: regressor is highly correlated with other regressors
- VIFs in the final model need to be less than 5
 - When X variables are correlated (high VIFs), the analysis makes statistical determinations based on the noise between the correlated variables. This will often result in high R² values but insignificant p values.
 - VIFs are often lowered when insignificant terms are removed from the model, and terms should be removed one at a time. The first term removed should be the one with the highest p value unless theory implies removing a different one.
 - High VIFs are not an issue in designed experiments, as the designs prevent high correlation between terms/regressors

Notes		

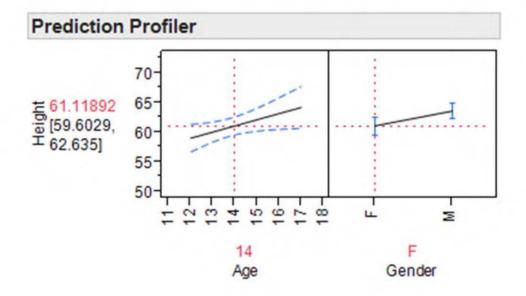
Parameter Estimates								
Term	Estimate	Std Error	t Ratio	Prob> t	VIF			
Intercept	39.457057	4.812681	8.20	<.0001*				
Gender[F]	-1.227546	0.502444	-2.44	0.0196*	1.0154192			
Age	1.6360307	0.343014	4.77	<.0001*	1.0155259			
(Age-13.975)*Gender[F]	-0.600896	0.343014	-1.75	0.0883	1.0004648			

The variance inflation factors for all terms in the model are below 5. There is no concerning level of correlation between model terms.

To display the VIFs, right click in the Parameter Estimates section, click Columns, then VIF.

Notes			

Predicted values and associated uncertainty



Predicted avg. height in the population of 14 year old girls	61.12
95% confidence interval for avg. height of 14 year old girls	[59.60, 62.64] 61.12 ± 1.52

Notes		

Steps in Multiple Regression (backward elimination method)

- 1. Run Analyze > Fit Model in JMP to investigate the relationship between y and x's. Use the Response Surface Model (all factors, all interactions, quadratic terms for continuous variables/factors)
- 2. Check model adequacy by reviewing the residuals plots:
 - Residual Normal Quantile Plot
 - Residual by Predicted Plot
 - Studentized Residuals (in run order)
- 3. Transform the data and resolve other issues, if needed.
- 4. Verify all VIFs < 5. Address the issue if any are over 5.
- 5. Remove insignificant terms from the model, that are not needed to maintain model hierarchy (main effects must be included if a higher order term of that variable remains in the model).
- 6. Use $Adjusted R^2$ to determine the amount of variation in Y that is explained by the model.

Notes			

Exercise 5.1

a) In the table below, record the Adjusted R² and RMSE from the analysis of *Height* in this section. Also, record the P-values from *Effects Tests*. Run the same analysis for *Weight* and record the corresponding results.

			P-values		
Response	Adj. R ²	RMSE	Age	Gender	Age*Gender
Height					
Weight					

- b) Which variable (*Height* or *Weight*) has the greater proportion of variation explained by *Age* and *Gender*?
- b) Explain why it wouldn't make sense to compare the two models in terms of RMSE.

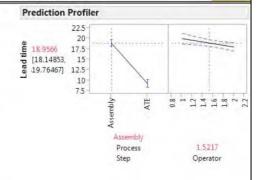
Notes			

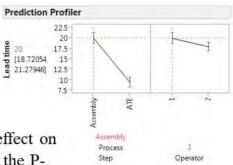
d)	Both Age and Gender were statistically significant for predicting Height. Is this true for Weight?
e)	For <i>Height</i> we found evidence that the growth curves for girls and boys have different slopes. Is this true for <i>Weight</i> as well? Give the P-value that is relevant to this question and explain what it means.
f)	Give the predicted average Weight in the population of 15-year-old boys. Give a 95% confidence interval for this average.
g)	Save your scripts, close and save the data table.
	Notes

Notes			

Data sets \ lead time 2.

- a) Fit a model for *Lead time* including the terms *Process Step*, *Operator*, and their interactive effect. **Be sure you have the correct modeling type for** *Operator*. (If you got the upper right profiler, the modeling type for Operator is not correct. The lower right profiler is correct.)
- b) Note anything concerning in the residuals plots.
- c) Remove terms under *Effect Summary* with P-values exceeding 0.15 (*Remove* button). Which terms are left? Any issues with VIFs?





- d) Based on the profiler, which factor has the larger effect on lead time (steeper slope)? Does this correlate with the Pvalues? Please explain.
- e) Save your script, close and save the data table.

Notes		

Data sets \ number and	d size of defects.jm	p.
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- a) Fit a model for *Max size* including the terms *Welder*, # *Defects*, their interactive effect, and the quadratic effect for # *Defects* (cross it with itself). This is the *Response Surface Model (RSM)* for one categorical factor and one continuous factor.
- b) Do you see anything concerning in the residuals plots?
- c) Using the Effect Summary, remove terms with P-values exceeding 0.15 (use the Remove button). Which terms are left in the model? Do all remaining terms have VIFs < 5?</p>
- d) Based on the profiler, which factor has the larger effect on Max size? Does this correlate with the P-values? Please explain.
- e) Save your script, close and save the data table.

Notes

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Exercise 5.4 [Instructor to demonstrate]

In this example you will analyze data from an optimization experiment concerning the removal of excess metal from castings by belt grinding.

The belt supplier had been recommending that belts be discarded when they are "50% used up." This rule was based on tests conducted by the supplier to define the usage point at which the total of labor and belt costs will be minimized. One of the grinders thought the supplier's rule caused grinders to discard belts too soon. Aside from being suspicious that the supplier just wanted to sell more belts, he argued that the supplier's tests did not take into account the time lost to belt changes.

This grinder developed a new standard under which belts would be discarded only after they were "75% used up." He wanted to do a comparative study to show that his method was cheaper overall. After he explains the study with his fellow grinders, 3 additional factors are added to the experiment.

Each casting in the experiment was weighed before and after the grinding operation. A technician kept track of how many belts were used and how long it took the grinder to complete each casting. From this information the total cost per unit of metal removed was calculated for each casting.

Data sets \ belt grinding.

Notes			

Exercise 5.4 (cont'd) [Instructor to demonstrate]

 Y variable: cost per unit of metal remove 	•	Y	variable:	cost	per	unit	of	metal	remove	d
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- X variables: > Contact wheel land-groove ratio (LGR): Low or High
 - Contact wheel material (MATL): Steel or Rubber
 - > Belt usage limit (USAGE): "50%" or "75%"
 - > Belt grit size (GRIT): 30 or 50
- Run the *Fit Model* script provided in the left panel, by clicking on the green triangle. This is the response surface model for 4 categorical X variables.
- · Check the residuals plots. Any problems?
- Using the Effect Summary, remove insignificant terms not needed to maintain model hierarchy, starting with the group of terms with P > 0.20, then one at a time. Which terms are left in the model?
- Use the Prediction Profiler to find the minimum cost factor settings.
- What do you expect the mean and standard deviation of Cost to be after implementing the optimal factor settings?
- · Save your script, close and save the data table.

Notes			

Exercise 5.5

In this example you will analyze data from an optimization experiment concerning the bond strength of potato chip bags.

Chips 'R' Us was receiving customer complaints about stale chips, especially from customers on airplanes. They traced the problem to the bag sealing process. The current process involved a temperature of 150°C, a pressure of 100 psi and a dwell time of 1.1 secs. The current average bond strength was about 85 psi.

Process Engineer Chip Kettle ran an experiment to increase the bond strength.

Production Manager Justin Thyme reminded Chip that he would very much like to avoid an increase in the dwell time.

Justin is able to free up a bag sealer for only so much time each shift. Chip realizes he will need two shifts to complete the experiment. He decides to include *Shift* as an additional variable in the analysis just in case there is an operator and/or equipment effect.

Data sets \ heat sealing 1.

Notes			

Exercise 5.5 (cont'd)

· Y variable: bond strength

· X variables and feasible ranges:

Temperature (TEMP): 120 to 180

Pressure (PRESS): 50 to 150

> Dwell time (DWELL): 0.2 to 2.0

Shift: 1 or 2

- Run the Fit Model script provided in the left panel. This is the response surface model (RSM) for 3 continuous X's. Is anything concerning in the residuals plots?
- Remove from the model insignificant terms that are not needed to maintain model hierarchy (P > 0.15), using the Effect Summary. Which terms are left?
- Use the Prediction Profiler to maximize the average bond strength. If your solution requires a long dwell time, manually move things around in the profiler to find another solution with a short dwell time.
- What do you expect the mean and standard deviation of bond to be after implementing the optimal factor settings?
- · Save your script, close and save the data table.

Notes			

Data sets \ outgassing process. Current (the Y variable) is the electrical current required to heat a filament to a specified temperature. Resist (one of the X variables) is the electrical resistance of the filament. Machine (the other X variable) identifies which of three processing units was used. We want to develop a model for Current as a function of Resist and Machine.

- a) Fit a response surface model for Current. (The terms will be Resist, Machine, the interaction term Resist*Machine, and the quadratic term Resist*Resist. To get the quadratic term, highlight Resist both under Select Columns and under Construct Model Effects, then click Cross.)
- b) Do you see anything concerning in the residuals plots?
- c) Remove any terms under *Effect Summary* with P value exceeding 0.15. (Use the *Remove* button.) Record the RMSE.
- d) Use the *Prediction Profiler* to find the predicted average *Current* for each machine if we always use filaments with resistance 52.

Notes				

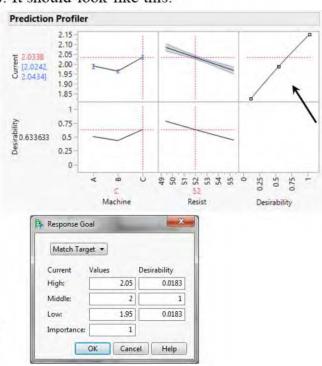
Exercise 5.6 (cont'd)

- e) The target value for *Current* is 2. For each machine, we want to find the resistance for which the average current is 2. On the *Prediction Profiler* red triangle, select *Desirability Functions*. It should look like this:
- f) Double click in the upper right hand panel of the profiler. (Try to avoid the plotted line.) You should get the dialog shown below.



g) Modify the dialog as shown to the right, then select OK. Proceed to the next slide.

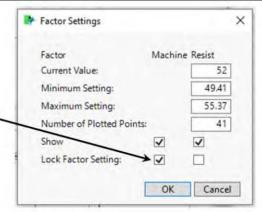
Notes



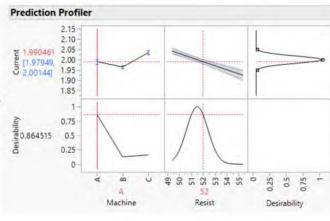
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Exercise 5.6 (cont'd)

h) On the *Prediction Profiler* red triangle, select *Reset Factor Grid*. We want to lock the factor setting for *Machine*, so check the *Lock Factor Setting* box as shown here.

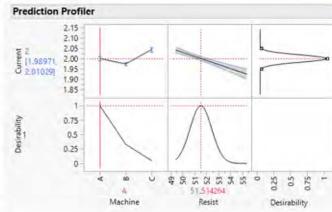


i) The vertical line for Machine should now be solid instead of dotted. This will hold the machine setting in place during Maximize Desirability, which allows you to optimize Resist separately for each machine. On the Prediction Profiler red triangle, select Maximize Desirability. Proceed to the next slide.



Notes			

j) The optimal resistance value for Machine A is 51.5. Drag the solid vertical line across to B, then click Maximize Desirability to find the optimal resistance value for Machine B. Do the same for Machine C.



- k) What will the average current be if we always use the optimal resistance values for each machine?
- What will the standard deviation of current be if we always use the optimal resistance values?
- m) Save your scripts, close and save the data table.

Notes			

6 Dealing with Model Adequacy Issues

In this section, we will cover the most common model adequacy issues:

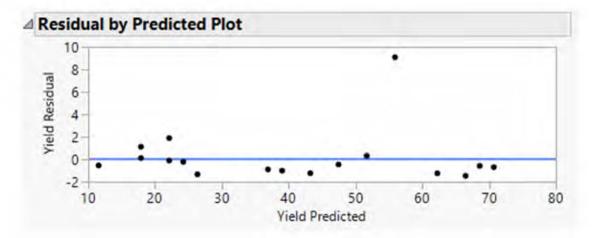
- Outliers
- · Pattern in run order plot of residuals
- Multicollinearity (VIFs over 5)
- · Unequal variance and non-normal residuals

Notes			

Issue: Outliers

Notes

Outliers can easily be seen on the Residual by Predicted and Studentized Residuals (residuals by run order) plots



Remember, healthy residuals look like random scatter about zero.

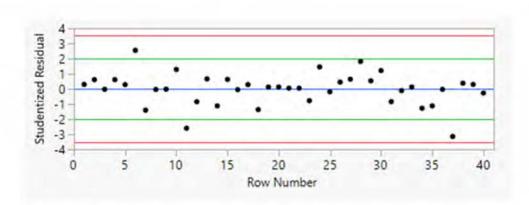
Here, it looks like there might be a suspicious data point.

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Issue: Outliers (cont'd)

- Investigate the data point.
 - o If it turns out to be just a data entry error, we simply enter the correct value, then all is well. Most of the time it's not that simple.
- If you have an outlier of unknown origin:
 - o Run the analysis with and without the questionable data point.
 - If you're lucky, the results will be pretty much the same both ways, hence no worries. Leave the data point in.
- If excluding the outlier does make a significant difference in the results, then you have a hard decision to make.
 - The official rule is: leave the data point in unless you can identify the cause. The idea is to throw it out only if you can demonstrate that it does not come from the population you want to study. This is the "pure" approach.
 - This should be tempered with the following practical consideration: you don't want your results to be unduly influenced by one extreme outlier, even if you can't explain it.

Notes			



Remember, healthy residuals look like random scatter about zero.

There are no patterns of concern here.

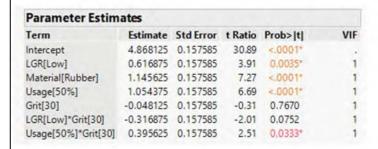
	Notes
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Issue: Pattern in run order of residuals (cont'd)

- Runs (points in a row) of positive-negative-negative-negative residuals indicate correlation between runs in an experiment.
 - o This implies that the assumption of independence has been violated.
 - Randomization of an experiment protects against this! Do it every time!
- This plot can show changes in variance over the time span of the experiment or data collection.
 - This could be due to increased skill as the experiment progresses, a process drift, operator fatigue, tool wear, etc.
 - This type of problem would show as an increase or decrease in spread or "scatter" of the residuals across the graph.
 - o If there is x data available to support it, one remedy is to add a factor (time since tool change, number of hours of operator work, etc.)
 - Increasing or decreasing variance can also indicate the need for a transformation.

Notes			

Issue: Multicollinearity (VIFs > 5)



Parameter Estimates							
Term	Estimate	Std Error	t Ratio	Prob> t	VIF		
Intercept	14.044944	0.291958	48.11	<.0001*			
Process Step[Assembly]	4.8792135	0.298829	16.33	<.0001*	1.0478749		
Operator[1]	0.6713483	0.296556	2.26	0.0349*	1.0478749		

Remember, VIF < 5 is not concerning.

- One aspect of factorial design experiments (often called DOEs) is that they are orthogonal designs. This results in the model terms being completely uncorrelated.
- Regressors that are completely uncorrelated with others have VIF = 1.
- High correlation is only a potential issue when using historical or observational data in regression analysis.

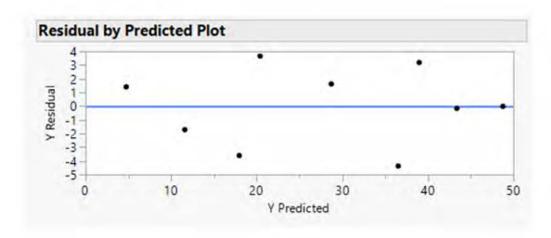
Notes			

Issue: Multicollinearity (cont'd)

Several strategies can be tried for resolving multicollinearity, but they may not be satisfactory, especially if the model will be used for prediction.

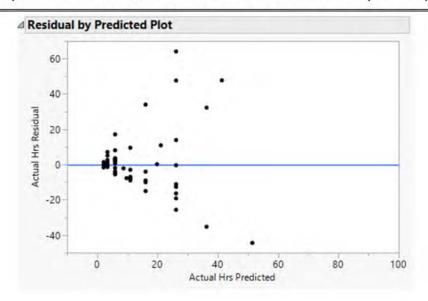
- Collect additional data in a way that breaks up the multicollinearity.
 - o Historical data may contain only certain combinations of x-variables, for example, only low levels of x_1 when x_2 is at a low level and only high levels of x_1 when x_2 is at a high level
 - Note: it may not be feasible or possible to collect this additional data.
 - In some cases, the factors (x's) are inherently correlated, for example as may be the case with household income and house size.
- · Respecifying the model, can help.
 - o If x_1 and x_2 are nearly linearly dependent, use one term, $x = x_1 + x_2$, which preserves the information content of the original variables
 - Try removing the term with the highest p-value, and look at that model. Then, replace it and remove the term with the highest VIF. See which gives the better model.
- Use ridge or principal-component regression (way beyond the scope of this course)

	Notes
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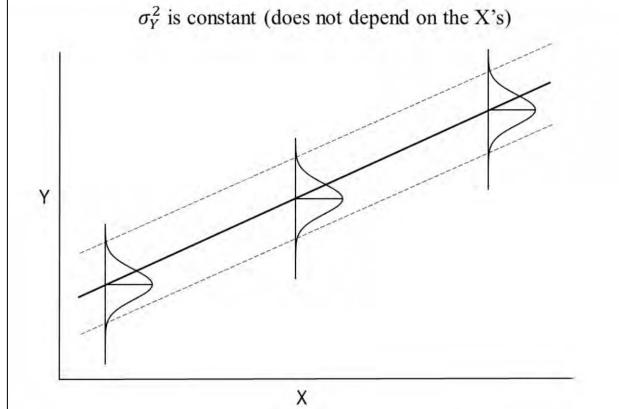
Remember, the variation in the residuals should be fairly constant across the Residual by Predicted Plot. There is no issue here.

Notes			

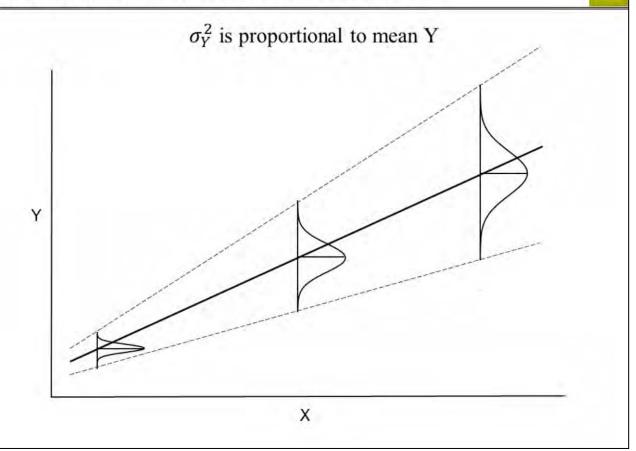


In this plot, we can see an issue. σ_Y^2 proportional to mean Y \rightarrow "sideways V"

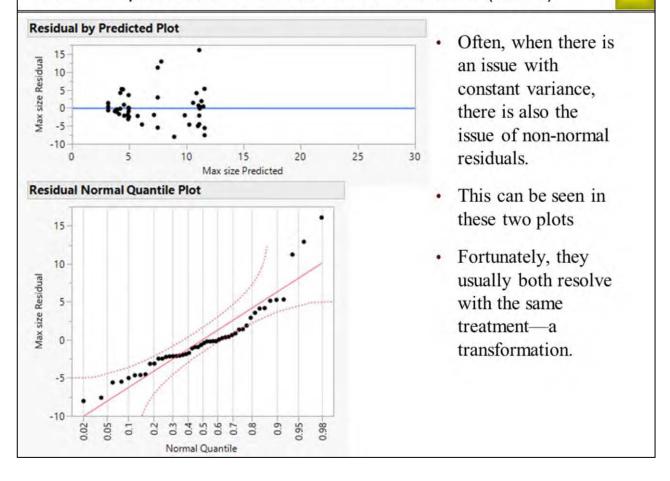
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Notes			



Issue: Unequal variance and non-normal residuals (cont'd)



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Notes

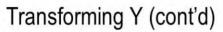
Notes 113
The standard assumption in all comparison and correlation analyses involving a quantitative Y variable is that the noise (unexplained/error/residual) variation follows a Normal distribution with mean 0 and a standard deviation that does not depend on the X variables.
This simple model has served us well. However, when Normality or constant σ is grossly violated, something must be done. The most common remedy is to use log(Y) or sqrt(Y) as the dependent variable instead of Y. This is a transformation. This "trick of the trade" is simple and, in most cases, effective.
Notes

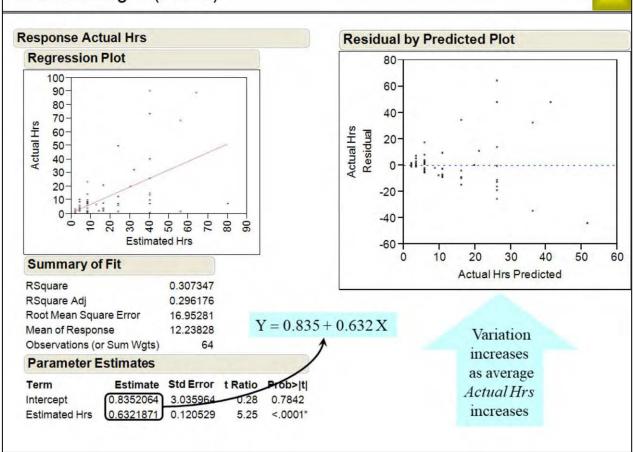
Data sets \ actual vs estimated

Fit Model We want to see **Model Specification** how accurately Select Columns Pick Role Variables Personality: Standard Least Squares > we can estimate **⊪**Task ▲ Actual Hrs Emphasis: Minimal Report ♣Resource the time it takes ♣Finish Date to do certain ■Estimated Hrs Help Run Model Weight optional numeric ▲Actual Hrs tasks Recall optional numeric Remove optional Construct Model Effects (Estimated Hrs) Analyze Add Cross Nest Fit Model Macros

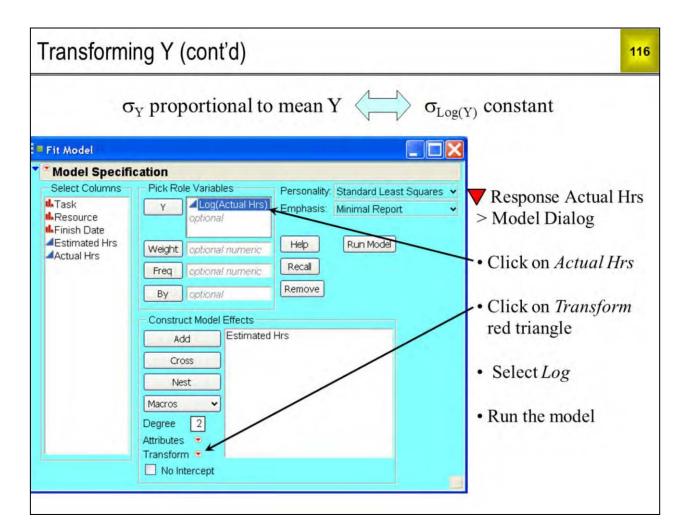
Degree 2
Attributes
Transform
No Intercept

Notes			





Notes			



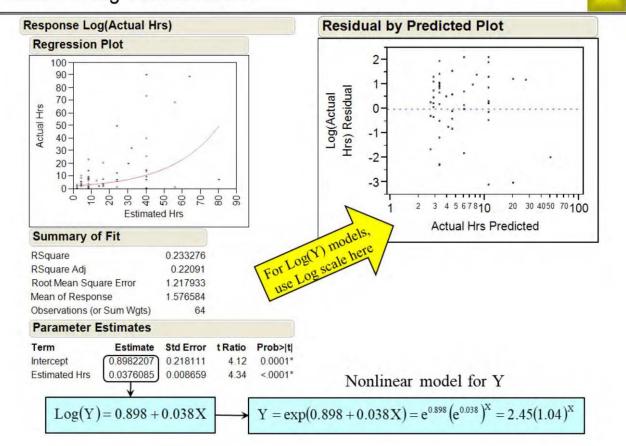
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Notes



Effects of log transformation

Notes



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Note on JMP notation, and impacts of the Log transformation

JMPs notation regarding Logs requires some clarification:

- Although JMP expresses the logarithm as "Log", it is actually base e, or the natural log, which is usually written as Ln. It is not a base 10 logarithm.
- However, the plots that use a log transformed X-axis display use base 10 log for the X-axis. This does not change the interpretation of the chart.

The impact of transformation on R² and p-values:

- In the previous example, a transformation was required because the residuals variance wasn't constant over the range of the predicted values.
- After the transformation, the R² value went down. This can lead to a belief that the non-transformed model was "better". However,
- Residuals showing this condition (heteroscedasticity) can cause p-values and R² to be over or under stated.
- When this condition occurs, the problem must be corrected. The resulting model, even if R² is lower or p-values are higher, is the more "real" model.

Notes			

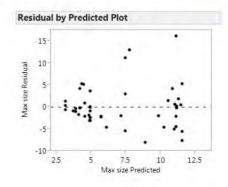
Steps in Multiple Regression (backward elimination method)

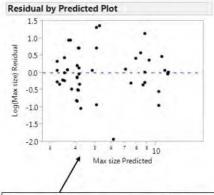
- Run Analyze > Fit Model in JMP to investigate the relationship between y and x's. Use the Response Surface Model (all factors, all interactions, quadratic terms for continuous variables/factors)
- 2. Check model adequacy by reviewing the residuals plots:
 - Residual Normal Quantile Plot
 - Residual by Predicted Plot
 - Studentized Residuals (in run order)
- 3. Transform the data and resolve other issues, if needed.
- 4. Verify all VIFs < 5. Address the issue if any are over 5.
- 5. Remove insignificant terms from the model, that are not needed to maintain model hierarchy (main effects must be included if a higher order term of that variable remains in the model).
- 6. Use $Adjusted R^2$ to determine the amount of variation in Y that is explained by the model.

Notes			

Data sets \ number and size of defects.jmp

- a) Fit a model for *Max size* including the terms *Welder*, # *Defects*, their interactive effect, and the quadratic effect for # *Defects* (response surface model for one continuous factor and one categorical factor). You should see a distinct sideways V. Do you see issues in any other residuals plots?
- b) Select Model Dialog on the Response red triangle menu, apply a Log transformation to Max size, re-run the model. The sideways V isn't completely gone, but close enough. Did other residuals plots improve?
- c) Use Effect Summary to remove terms with P > 0.15.



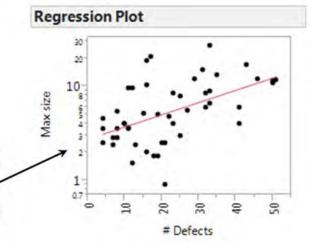


Remember to change the x-axis on the plot, as well.

Notes			

- d) Which terms are left in the model?
- e) Now we have a log-linear simple regression.

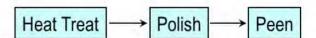
When you use a Log or square root transformation on Y, it is helpful to use same scale for the Y axes of the plots



f) Save your script, close and save the data table.

Notes			

An aerospace manufacturer uses integral castings as structural components of jet engines. Integral castings give design engineers more flexibility and simplify the assembly process. Defect-free castings are known to have long cycle fatigue life, but defects often arise in the casting process and must be weld repaired. The engine manufacturer's metallurgical team has proposed a finishing process of the following type to ensure adequate cycle fatigue life of weld-repaired castings:



The team wants to optimize the first two steps in this process to achieve maximum cycle fatigue life. Also, though other applications of similar processes have included peening, they would like to see if it can be omitted to reduce processing time and cost.

Due to project time constraints and limited availability of test fixtures, the team can perform at most 12 cycle fatigue tests for their experiment.

Notes			

Exercise 6.2 (cont'd)

	V	wariable.	Cualas	(to failure)	i
•	1	variable.	Cycles	(10 Ianuic)	1

• X variables: > Heat treat: Anneal or Solution/age

Polish: Chemical or Mechanical

> Peen: Yes or No

- Data sets \ weldment fatigue.jmp.
- Run the Model script provided in the left panel, run the model.
- Notice the extreme sideways V on the *Residual by Predicted Plot*. Are there issues in any of the other residuals plots? If yes, what are they?
- Rerun the model using a Log transformation on Cycles. Did residuals plots improve?
- Remove insignificant terms from the model (P > 0.15) that are not needed to maintain model heirarchy.
- Use the Prediction Profiler to maximize the cycle fatigue life.

Notes			

A Black Belt wants to minimize the *leak rate* in plastic containers ultrasonically welded together. The X variables and ranges are:

> Force: 70 to 150

> Energy: 275 to 325

> Amplitude: 70 to 90

- Data sets \ ultrasonic welding 1.jmp.
- Run the Model script provided in the left panel.
- · What problems do you see in the residuals plots?

Notes			

Exercise 6.3 (cont'd)

•	Rerun the model using the Log transformation on leak rate. (Be sure to change the
	x-scale to Log on the Residual by Predicted Plot.)

- Rerun the model using the Sqrt transformation on leak rate. (Be sure to change the x-scale to Sqrt on the Residual by Predicted Plot.)
- Which set of residuals plots looks better? Use whichever transformation looks like it worked better, going forward.
- Remove insignificant term(s) from the model (P > 0.15), while maintaining model hierarchy.
- Use the Prediction Profiler to minimize the leak rate.

Notes			

7 Simple Regression with Pass/Fail Y

When the response variable, Y, is binary (pass/fail, yes/no, success/failure, etc.), the regression model used for a continuous Y-variable *cannot* be used.

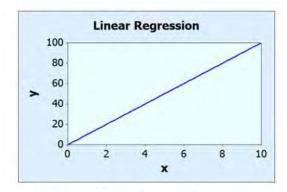
- A logistic response function must be used
- The resulting analysis yields an equation that allows us to calculate event probability:

$$P_{event} = f(x_1, x_2, \dots, x_n)$$

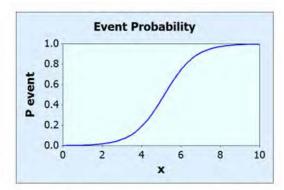
- This equation is used to answer questions such as:
 - What is the probability of being in spec (at various levels of x)?
 - What is the probability of getting the contract?
 - O What is the probability of a defect?

Notes			

This probability function, the *logistic response function*, has a much different behavior than a linear regression function:



 The y values of a linear regression can have any values



 The logistic response function is an S-shaped function that can only have values between 0 and 1

To be useful in prediction, the logistic response function must be transformed into an unbounded linear function

Notes			

The *logit transformation* is used to linearize the model:

$$logit(P_{event}) = \ln\left(\frac{P_{event}}{1 - P_{event}}\right) = b_0 + b_1 x_1 + \dots + b_n x_n$$

$$\frac{P_{event}}{1 - P_{event}} = e^{b_0 + b_1 x_1 + \dots + b_n x_n}$$

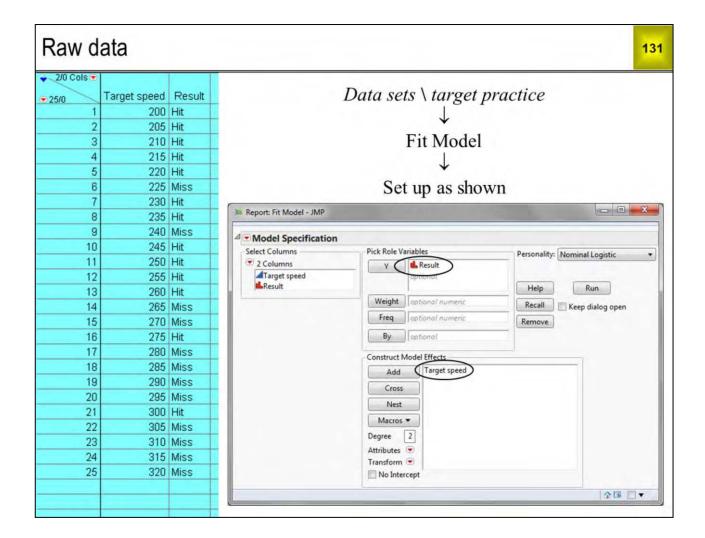
$$P_{event} = \frac{1}{1 + e^{-(b_0 + b_1 x_1 + \dots + b_n x_n)}}$$

- · This is the form of the final equation in the regression analysis
- The maximum likelihood method is used to estimate the parameters in this
 probability equation . . . JMP does this work for us
- We can use this equation (model) to predict the probability of an event for various levels of x₁, x₂,...,x_n

Notes			

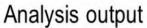
We will see how to use JMP do the regression analysis when we have:

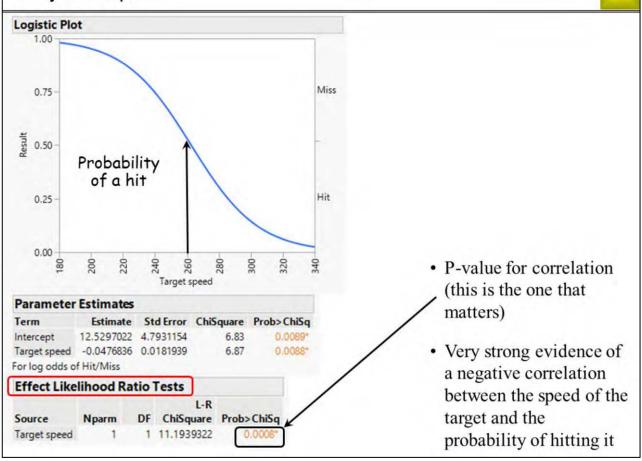
- a) Raw data each row represents one part or transaction
- Tabulated data each row represents multiple parts or transactions



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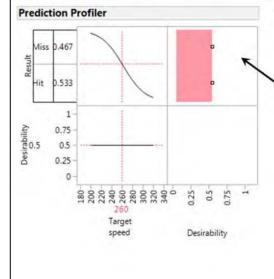
Notes





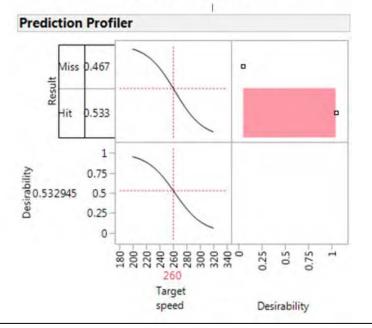
Notes			

The prediction profiler



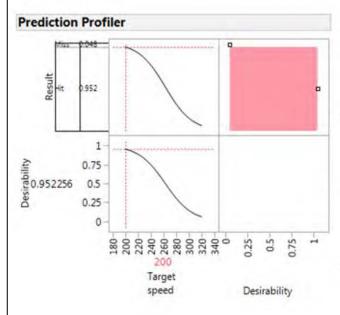
Notes

- Red Triangle → Profiler → Prediction Profiler red triangle → Optimization and Desirability → Desirability Functions
- Double-click in the blank area, enter 1 for *Hit* and 0 for $Miss \rightarrow OK \rightarrow OK \rightarrow next$ slide



Prediction profiler (cont'd)

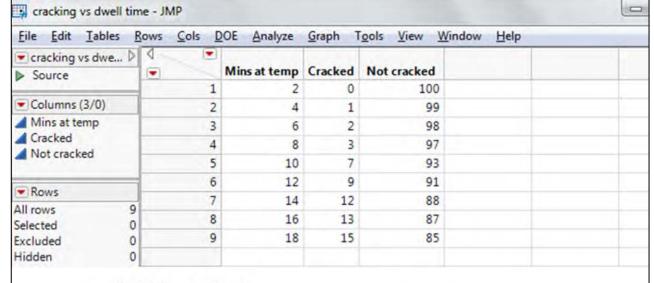
Prediction Profiler red triangle → Optimization and Desirability → Maximize Desirability



- The target speed of 200 produces the maximum hit probability of 0.952
- The corresponding miss probability is 0.048
- The target speed of 320 produces the minimum hit probability of 0.061
- The corresponding miss probability is 0.939

Open Data sets \ quotation process.jmp. a) Fit PO by TAT. Which P-value in the output is the most reliable? b) Does the PO hit rate increase or decrease as the TAT increases? c) Find the PO hit rates for 3 day and 15 day turnarounds. d) Save your script, close and save the data table. **Notes**

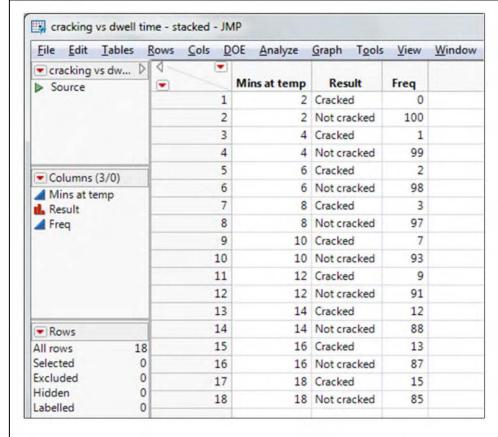
Data sets \ cracking vs dwell time



- 1) Tables → Stack
- 2) Use Cracked and Not cracked as the stack columns
- 3) Change Label to Result, change Data to Freq \rightarrow OK
- 4) Save as cracking vs dwell time stacked

Notes			

Stacked format



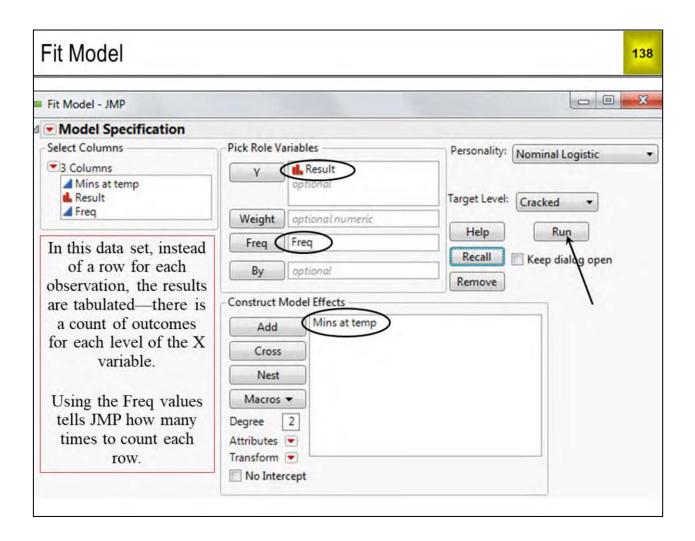
Analyze

↓
Fit Model

↓
See next slide

↓
Set up as shown

Notes			

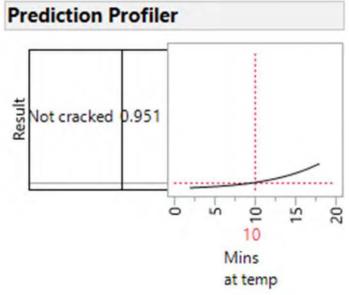


Notes			

Effect Likelihood Ratio Tests

			L-R	
Source	Nparm	DF	ChiSquare	Prob>ChiSq
Mins at temp	1	1	41.5372498	<.0001*

Very strong evidence of positive correlation between dwell time and probability of cracking



Dwell time (mins)	Probability of cracking
5	0.020
10	0.049
15	0.114

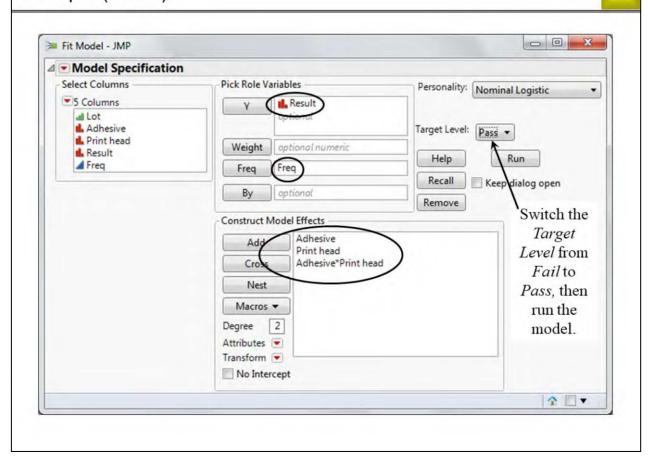
Notes			

8 Multiple Regression with Pass/Fail Y

	→ 5/0 Cols 💌					
• Project to reduce clogged nozzles	€ 32/0	Lot	Adhesive	Print head	Result	Freq
	1	1	A4	D2	Fail	2
in print heads	2	1	A4	D2	Pass	58
	3	2	A4	D1	Fail	-1
• Comparison of four types of	4	2	A4	D1	Pass	59
그리고 살아가면 하면 보다면 하면 살아 있는데 그렇게 하는 사람들이 되지 않아요.	5	3	A2	D2	Fail	13
adhesive and two print head	6	3	A2	D2	Pass	47
designs	7	4	A1	D2	Fail	11
	8	4	A1	D2	Pass	49
	9	5	A3	D2	Fail	4
• Each lot = 60 print cartridges	10	5	A3	D2	Pass	56
	11.	6	A4	D1	Fail	5
"D"	12	6	A4	D1	Pass	55
• "Pass" = no customer detectable	13	7	A1	D2	Fail	8
print defects	14	7	A1	D2	Pass	52
	15	8	A2	D1	Fail	3
D	16	8	A2	D1	Pass	57
 Data sets \ clogging pass-fail 	17	9	A3	D2	Fail	1
	18	9	A3	D2	Pass	59
• Run the Model script. If necessary,	19	10	A2	D2	Fail	13
HE HERE NOTE HERE NOTE HERE NOTE HERE NOTE HERE NOTE HERE NOTE HER NOTE HERE NOTE HERE NOTE HERE NOTE HERE NOT	20	10	A2	D2	Pass	47
bring the Model Specification to	21	11	A2	D1	Fail	1
the front.	22	11	A2	D1	Pass	59
	23	12	A1	D1	Fail	1
	24	12	A1	D1	Pass	59
	25	13	A3	D1	Fail	7

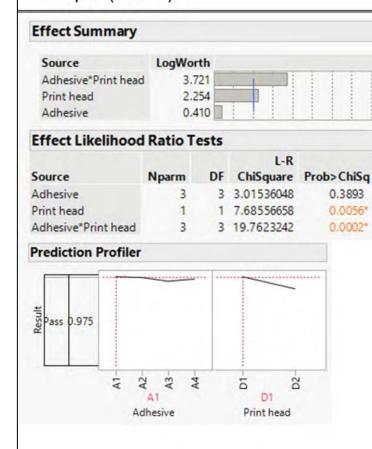
Notes			

Example (cont'd)



Notes		

Example (cont'd)



- The Adhesive factor was insignificant, but we left it in the model to preserve model hierarchy (Adhesive*Print head is significant)
- On the *Prediction Profiler* red triangle select *Optimization and Desirability* → *Desirability Functions*
- · See next slide

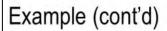
PValue

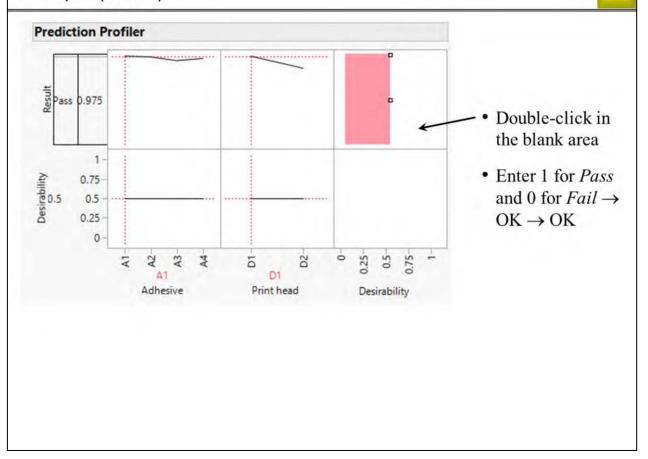
0.00019

0.00557 ^

0.38926 ^

Notes				

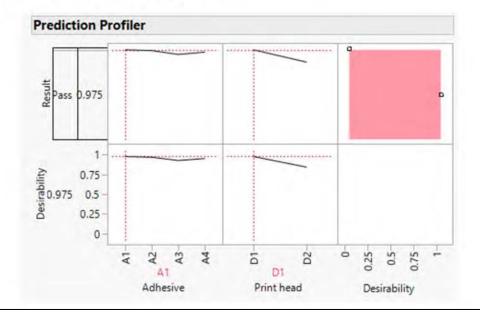




Notes			

Example (cont'd)

- Prediction Profiler red triangle → Optimization and Desirability → Maximize Desirability
- The failure rate predicted from the optimization was 0.025 or 2.5% (current state failure rate was 20% or more)
- · Best combination was D1 with A1



	Notes
_	
_	
_	
_	

A Black Belt wants to minimize the occurrence of bubbles and ripples in the urethane coating on truck nameplates. The X variables and ranges are:

Badge temp: 20 to 40

Mixing ratio: 92.6 to 94.6

Curing temp: 30 to 55

- Data sets \ urethane coating pass-fail
- Run the *Model* script in the left panel. In the *Model Specification*, switch the *Target Level* from *Fail* to *Pass*, then run the model.
- Remove insignificant terms from the *Effect Summary* (P > 0.15).
- Use the Prediction Profiler to find a factor combination that maximizes the yield.
- The current state yield was about 95%. What is the predicted yield for the improved process?

Notes			

Lean Six Sigma Black Belt Volume II

Tab 3 Design of Experiments

Presented by



Oregon: 503-484-5979 Washington: 360-681-2188 www.etigroupusa.com

1 Designed Experiments vs "File Cabinet" Data

All experiments are experiences, but not all experiences are experiments. — R. A. Fisher

	File cabinet data	DOE
Data sets	Larger, "messy"	Smaller, "clean"
Data collection	Routine operation	Controlled conditions
Information provided	Correlations	Cause and effect
Interactive effects?	Maybe	Definitely
Time period covered	Longer	Shorter

Notes			

Notes

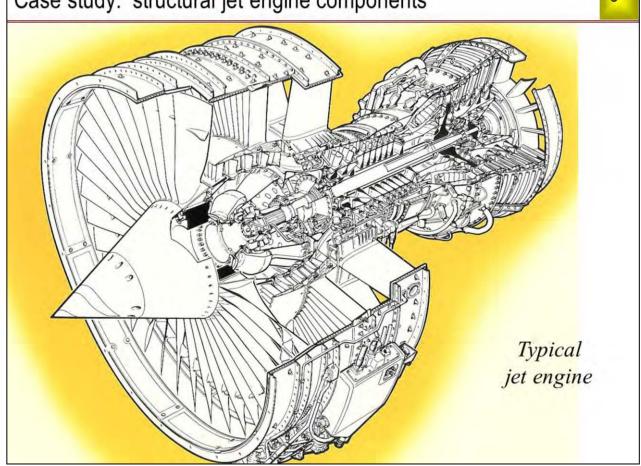
Ronald Fisher was an English geneticist and mathematician trying to increase crop yields in the 1920s. There were limited numbers of plots available for field trials, gradients in the soil, variable proximity to water sources, differing amounts of sunlight, and long lead times. To solve these problems, Fisher developed a body of statistical methods known as Design of Experiments (DOE).

During World War II, Fisher's techniques were extended and applied to military optimization problems. After the war, they were further extended and applied to industrial problems like improving the quality and reliability of manufactured products. For his lifelong contributions to science and statistics, Dr Ronald Fisher eventually became Sir Ronald Fisher.

The quote above was Fisher's way of emphasizing the difference between observational studies (analysis of "file cabinet" data) and designed experiments. This distinction is as important today in Six Sigma as it was a century ago in agriculture. After all, both are concerning with increasing yields!

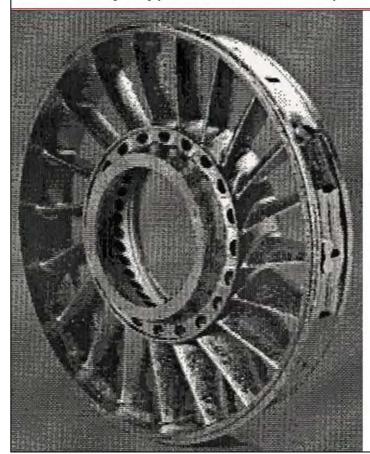
Notes			

Case study: structural jet engine components



Notes			

Case Study: Typical structural component of jet engine

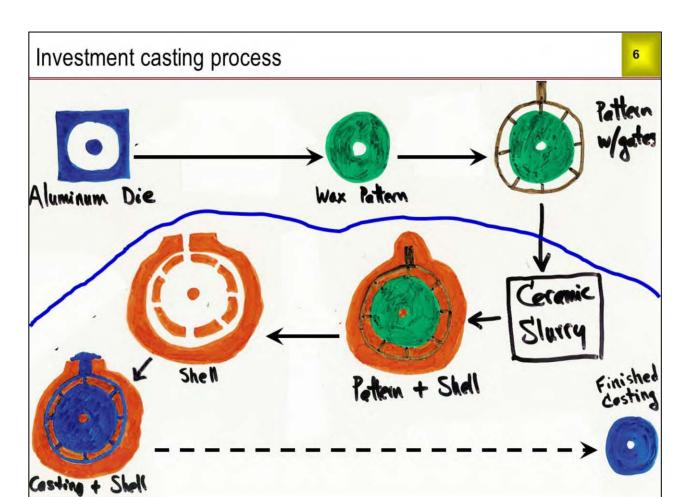


- Back in the day: many small pieces welded together
- · Now: one piece casting
- 3 to 6 feet in diameter
- Stainless steel, nickel alloys, titanium alloys

Notes			

- Value stream: investment casting of nickel alloy structural components
- · Process boundaries: shell making through backend processing
- Experiencing "orange peel" surface condition violating customer smoothness requirements
- 12% scrap rate (big parts → big \$\$)
- Y = f(X): analyze existing production data

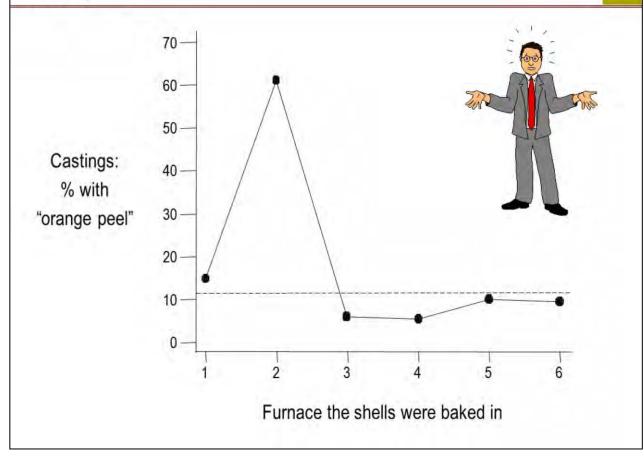
Notes			



Notes			



A big signal



Notes			

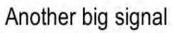
Notes

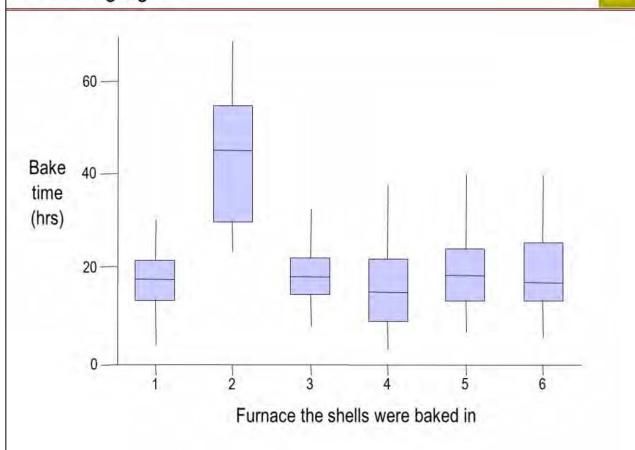
The strongest correlation in the database involved one of the pre-heat furnaces used to bake the ceramic shells before transfer to the casting furnace. Furnace 2 was new and had come online just about the same time orange peel started occurring. Almost everyone agreed the new furnace was the problem.

The casting area manager refused to take Furnace #2 off-line. He needed all six preheats to keep the casting furnace running nonstop so he could meet his production quotas.

Process Engineer Dave (shown above) was skeptical that Furnace 2 was causing the problem. For one thing, the other pre-heats were also producing scrap castings. Also, he had spent the better part of the past three months evaluating and qualifying the new furnace.

Notes			





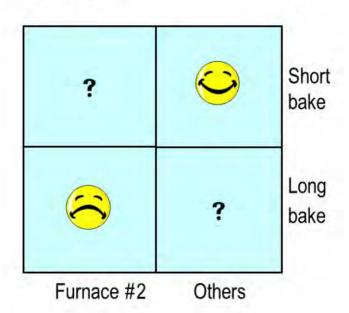
Notes		

Notes 10
Dave pointed out that the shell bake times were much longer for Furnace 2 than for the other furnaces. There was a minimum required bake time, but no upper limit. Dave's theory was that orange peel was caused by long bake times.
Why did shells stay longer in Furnace 2?
It turned out there wasn't room to put the new furnace next to the original five, so it had to be located further away from the casting furnace. The fork-lift operators wouldn't drive over there unless they had no shells ready from the closer furnaces, so shells tended to sit in Furnace 2 for a long time.

Notes			

Autopsy

- The file cabinet data suggested some plausible hypotheses
- · It could not establish the cause of the defect
- The quantity of data was not the problem
- The data lacked the structure required to determine cause and effect



<u>Notes</u>			

Notes
There was lots of data in the upper right-hand and lower left-hand cells in the table above, but virtually nothing in the other two cells. Making sure that data tables like the one above are completely filled out is one of the basic principles of experimental design.
Subsequently, engineers ran enough parts in the upper left-hand corner of the table to determine that long bakes were indeed causing the problem. An upper limit on the bake time was developed and put in place. Shells that exceeded this limit were scrapped. This cost the company much less than scrapping the resulting castings.
The new procedure made the fork-lift operators' job harder, but it made the orange peel problem go away.

Notes		

The Role of DOE in Process Improvement

Y = f(X) analysis

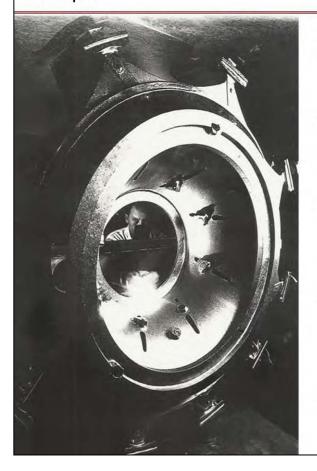
- DOE is an effective way to collect data for identifying critical x's, in a relatively short period of time
- In a Lean Six Sigma project, data collection in the Measure phase may have produced little or no useful information.

Developing the future state

- May have multiple potential improvement ideas on the table
- DOE is an effective way to evaluate these ideas prior to defining the future state

Notes			

Example



- Titanium castings → strong & light
- Ti develops surface oxidation during the cooling phase
- Large Ti castings were failing the customer O₂ requirement
- Analysis of file cabinet data yielded no significant correlations
- Engineers developed a list of factors for a DOE

Notes			

Example (cont'd)

Factor	Levels	Current state X variable	Possible future state solution
Slurry for shell	Batch 1 vs Batch 2	~	
Shell thickness	14 dips vs 18 dips		✓
Shell bake time	6 hrs vs 48 hrs	✓	
Shell bake temp	1950° vs 2050°		1
Alloy grade	Low \$ vs High \$		✓
Alloy status	New vs Revert	~	
Heat shield steel	Mild vs SS		*
Cooling fan speed	2400 vs 3200		~

Notes			

2 One Factor at a Time?

- In this approach, each factor is varied with all others held constant. This way, it is felt, we can see the "pure effect" of each factor.
- This is one way to apply the scientific method, but it is not the only way, and not the best way!
- For any proposed one at a time experiment, there is usually a multifactor experiment providing:
 - √ More information
 - √ Better results
 - √ Same (or possibly smaller) total sample size
- One at a time trials are useful for determining feasible ranges for factor in a DOE

Notes		

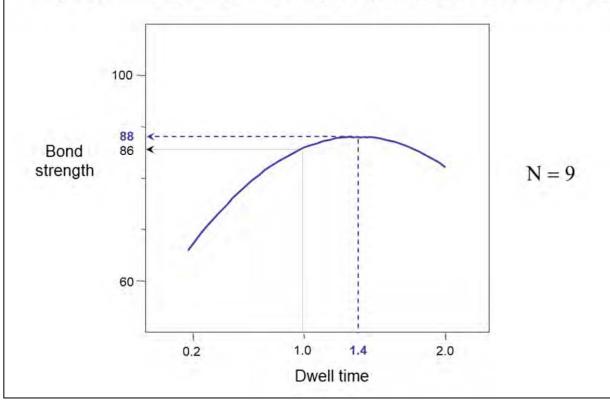
Example: potato chip bags

- The current average bond strength of our potato chip bags is 86 psi
- · Based on customer complaints, we need to increase the bond strength
- The most important control factors in the bag sealing operation are *temperature* and *dwell time* (see below)
- · Secondary objective: decrease the dwell time if possible

Factor	Current level	Feasible range
Temperature	150°	120 to 180
Dwell time	1.0 secs	0.2 to 2.0

Notes			

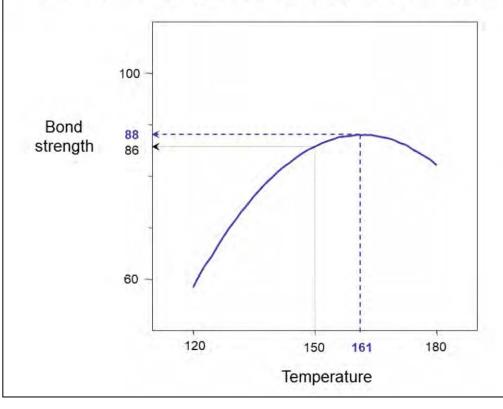
Vary dwell time over its feasible range while holding temperature at 150



_Notes			

Notes	20
Our process engineer Chip Kettle first studies the effect of dwell time while holding temperature constant. He seals and tests 9 bags using dwell times ranging from 0.2 to 2.0. Chip finds he can increase the bond strength by 2 psi by increasing the dwell time to 1.4.	
Our production manager Justin Thyme is not pleased with the prospect of a 40% increase in dwell time.	
Notes	_

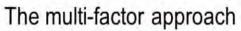
Vary temperature over its feasible range while holding dwell time at 1.0

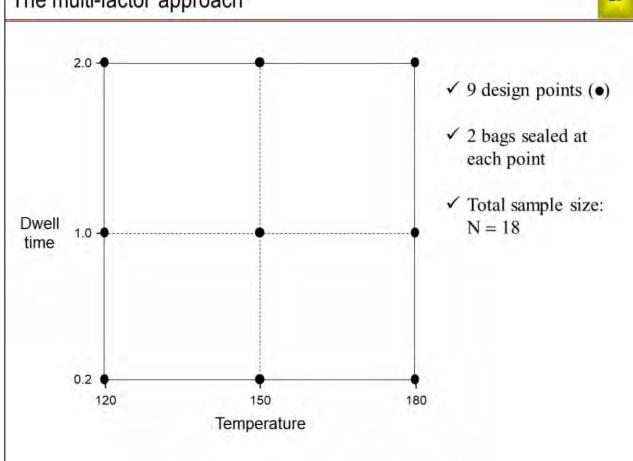


N = 9

Notes			

Notes
Chip now studies the effect of temperature while holding dwell time constant. He seals and tests 9 bags using temperatures ranging from 120 to 180. Chip finds he can increase the bond strength by 2 psi by increasing the temperature to 161.
Chip predicts that changing the dwell time to 1.4 and the temperature to 161 will increase the average bond strength by 4 psi $(2 + 2)$. However, it is highly likely that Justin will oppose the increase in dwell time, in which case the increase in average bond strength will be only 2 psi.
Notes

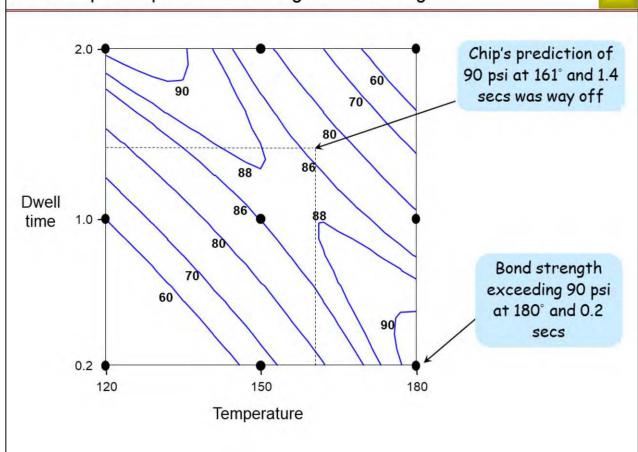




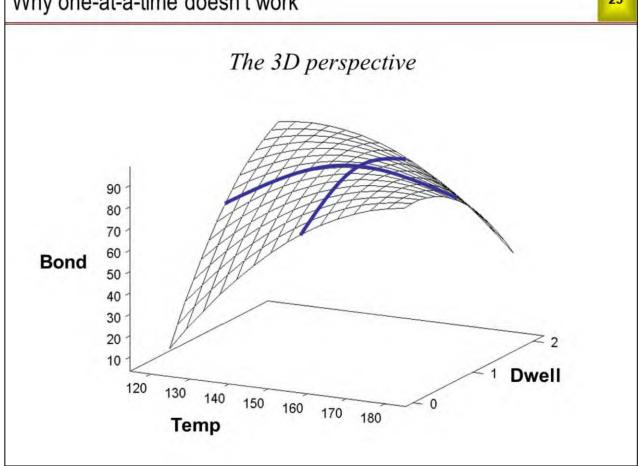
Notes			



Contour plot of predicted average bond strength



Notes			



Notes			

Notes

When we experiment with all factors, but one held constant, we optimize sequentially over one-dimensional profiles. The sequence of solutions generated by this process is highly dependent on the starting point. It has very little chance of finding a global optimum, and often fails to move a significant distance from the starting point.

Notes			

3 DOE Terminology

Experimental unit

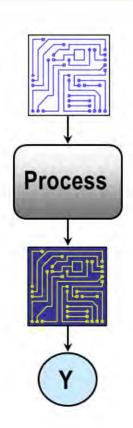
The outcome of a single application of the process being studied

Sample size

The total number of experimental units ("number of runs")

Response variable

A Y variable measured or inspected on each experimental unit



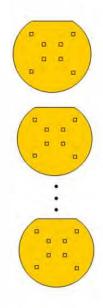
Notes			

Notes	20
The experimental unit is often a part, lot, batch or single transaction of some kind. It may also be a test specimen or sample of material. It is important to identify the experimental unit—it provides the basis for counting sample size, and sample size is critical in determining the statistical significance of the results.	
The experimental unit is determined by the process on which we are experimenting, not the measurement plan used to evaluate the results. For example, suppose we test 100 devices for product life. Suppose we measure a degradation parameter on each device every 10 hours until the end of the test at 100 hours. The sample size for the study is the number of units (100), not the number of measurements (1000).	
Notes	_

Example

- 11 silicon wafers were subjected to vapor deposition at various temperatures, pressures, and Argon flow rates
- · The thickness of the resulting layer was measured at 8 locations on each wafer
- What is the sample size?

Temp	Press	Flow	Thickness
180	0.3	30	
180	0.3	30	
180	0.3	30	
160	0.4	10	
160	0.4	50	
160	0.2	50	
160	0.2	10	
200	0.4	10	
200	0.2	10	
200	0.2	50	
200	0.4	50	



Notes			

Example (cont'd)

- The sample size is the number of experimental units, not the total number of measurements taken
- The response variables of interest may be statistical summaries of multiple measurements on each unit

Temp	Press	Flow	Avg.	Std. dev.
180	0.3	30	1	1
180	0.3	30		
180	0.3	30		
160	0.4	10		
160	0.4	50		
160	0.2	50		
160	0.2	10		
200	0.4	10		
200	0.2	10		
200	0.2	50		
200	0.4	50		

Notes			

Factor

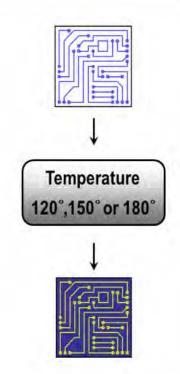
An X variable controlled in an experiment, varied on purpose to determine its effect on the responses

Level

A particular value or setting of a factor to be used in the experiment

Requirements

All levels of each factor must be logically and physically compatible with all levels of the other factors



Notes			

· ·
Variables used as factors in a designed experiment may or may not be controlled in the routine process. What matters is that they can be controlled for the purpose of experimentation.
Notes

T	7		Van de Carlos de		10	Contract of the Contract of th
Example	es	of	continue	ous i	tact	ors
		-,				~ . ~

Time Volume

Temperature Weight

Pressure Length

Energy Width

Voltage Density

Resistance Rate

Concentration RPM

Flow Intensity . . .

Notes			

Notes

- A factor is continuous if it can be varied within some range on a scale of measurement
- It is generally preferable to use 3 equally-spaced levels (low, medium, and high) for continuous factors
- Even though only two or three levels of a continuous factor will be used in an experiment, it is advantageous to identify it as continuous, rather than categorical
- Even when some levels of a continuous factor would not be applied to the process after the experiment, it is advantageous to still treat the factor as continuous in the experimental design and analysis
 - Example: After an experiment, we find that the optimal temperature setting is 117.13°. We may choose to set the temperature to 115° or 120°.
 We still treat temperature as a continuous factor in our experiment.
 - Example: We know that if we determine that the optimal Introductory Time Period for an offer is 3.37 months, it wouldn't make sense to offer that to our customers. We would offer them an Introductory Time Period of 3 months. We still treat this factor as continuous in our experiment.

Notes			

Examples of categorical factors

Method Old or New

Tool set 1, 2 or 3

Material A, B, C or D

Supplier X, Y or Z

Operator | Bob, Carol, Ted or Alice

Color | Cyan, Magenta or Yellow

Size | Small, Medium or Large

Notes			

Notes

- A factor is categorical if it is not <u>possible</u> to have it at all values on a measurement scale
- Treating a factor as continuous implies that any value in the range can be used in the process
- If the levels used in the experiment are the only <u>possible</u> values, even when the categories are described by numbers, the factor should be treated as categorical
 - Example: Pizza pan sizes of 10", 12", 14", 16" (10.26" doesn't exist)
 - Example: A control parameters for certain electron microscopes has to be a power of 2.
 - Some JMP DOE platforms now have the option of Discrete Numeric, in addition to continuous and categorical, to better handle these cases

Notes			

Categorical factors	Continuous factors
Any number of levels	Usually 2 - 3 levels
Discrete set of design points	Region in factor space
est for significant differences	Response surface modeling
Select best design point	Interpolate between design points

Notes			

Control factors	Noise factors
Can be controlled in the routine process Type of material Temperature Pressure Method Time :	Cannot be controlled in the routine process Ambient conditions Raw materials Operators Suppliers Batches Setups Shifts Lots :

Is it good	practice to include noise factors in experiments?
	Why or why not?

Notes			

Design point

A particular combination of levels of the factors.

Design matrix

The set and sequence of design points to be used in the experiment.

Full factorial

The set of all possible design points for a given set of factors and levels.

CO THE		
Temp	Press	
120	50	Expe
120	150	
180	50	iental u
180	150	units

- ✓ Full factorial
- ✓ 4 design points
- √ No repeats (replication)
- ✓ Sample size = 4

Notes			

Experimental units

DOE terminology (cont'd)

Replicate r	un
-------------	----

An experimental unit created independently of other units at the same design point

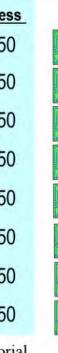
Replicate

A set of replicate runs, one for each unit in a given set (usually a replicate of a full factorial)

False repeat

- · Repeated or multiple measurements on one unit
- · Units in the same batch, when optimizing a batch process for which there is very little within-batch variation

Temp	Press	
120	50	
120	150	
180	50	
180	150	
120	50	
120	150	
180	50	
180	150	



- ✓ Full factorial
- ✓ 4 design points
- ✓ 1 replicate
- ✓ Sample size = 8

Notes			

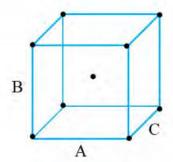
A bank wants to increase the yield of its credit card offers. It plans to collect VOC data by means of a DOE involving the factors in the table below. The bank plans to send out 1000 offers for each combination of the factor levels. Based on the data, they will determine the combination with the greatest % yield.
(a) What is the Y variable?
(b) What is the experimental unit? (Consider how Y will be measured)
(c) How many design points are in the full factorial?
(d) What is the sample size?
(e) For each factor, decide whether you would treat it as quantitative or categorical (give your answers and reasons in the table below).
Notes

Exercise 3.1 (cont'd)

Factor	Levels	Continuous or categorical?
Introductory APR	0, 2.5 or 5%	
Introductory time period	3, 6 or 9 months	
Gift	iPhone, iPad, microwave or espresso machine	

Notes			

4 The Full-Factorial Design



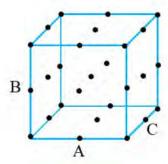
The full-factorial design contains all possible combinations of the specified factor settings

Above is an image of a 2³ full-factorial with center points (continuous factors)

- The full-factorial requires one run at each design point (8 for this 2³)
- 3-5 center points are recommended in a 2^k design
- Total runs required for this full-factorial are 11-13

A 2^k full-factorial design can estimate main effects and interactions

Full-Factorial Design (cont'd)

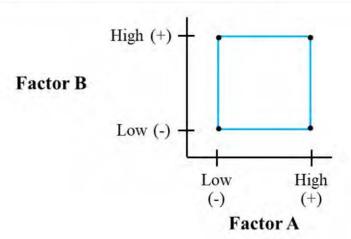


Above is an image of a 33 full-factorial

- · The full-factorial requires one run at each design point
- "Center points" are part of the design points (the middle level of the factors)
- Total runs required for this 3³ full-factorial is 27
- This type of design is useful when some factors are continuous, and some are categorical (there could be 3-level categorical factors in the picture above)

A three-level full-factorial (3^k) design can estimate main effects, interactions and quadratic effects, but is an inefficient design.

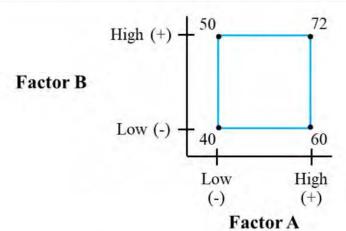
Notes			



 $Main\ Effect\ of\ A = Avg\ Response\ A\ (High) - Avg\ Response\ A\ (Low)$

Coefficient
$$A = \beta_1 = \frac{Main\ Effect\ A}{2}$$

Notes			

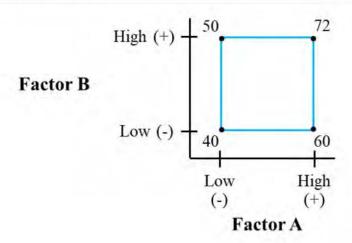


 $Main\ Effect\ of\ B = Avg\ Response\ B\ (High) - Avg\ Response\ B\ (Low)$

$$=\frac{50+72}{2}-\frac{40+60}{2}=\frac{122}{2}-\frac{100}{2}=11$$

What is the Main Effect of Factor A in this example?

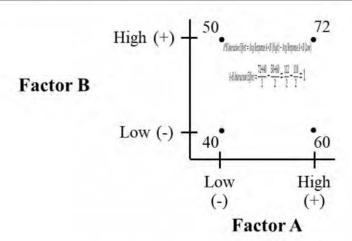
Notes			



Coefficient
$$B = \beta_1 = \frac{Main\ Effect\ B}{2} = \frac{11}{2} = 5.5$$

What is the coefficient for Factor A in this example?

Notes			



A*B Interaction Effect = Avg Response A*B (High) - Avg Response A*B (Low)

A-B Interaction Effect =
$$\frac{72+40}{2} - \frac{50+60}{2} = \frac{112}{2} - \frac{110}{2} = 1$$

Notes				

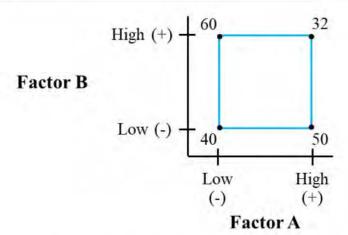
Example: Interaction Effect

To determine which values are for A*B High and Low, it can be helpful to refer to the experimental design matrix.

Multiply the + and - in the A and B columns in the design matrix to get the + and - for the A*B column.

	Fac	Factors			
Run	Α	В	A*B	Response	
1		34	+	40	
2		+		50	
3	+	- 1		60	
4	+	+		72	

Notes			

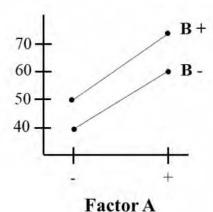


What is the A-B Interaction Effect in this example?

	Fac	tors		
Run	Α	В	A*B	Response
1			in T	
2	-	+		
3	+			
4	+	+		

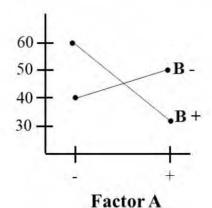
Notes			

Interaction Plots graphically show interaction



Interaction Plot for the first example

No interaction—slopes of lines are approximately equal



Interaction Plot for the data on the previous slide

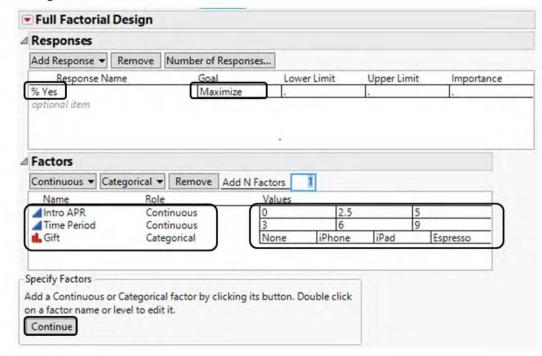
Interaction present—lines have different slopes

Notes			

Creating a Full Factorial Design

DOE → Classical → Full Factorial Design

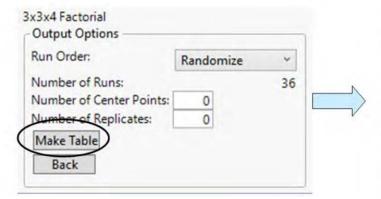
1. Define responses, factors, numerical ranges for continuous factors, and levels for categorical factors.



Notes			

Creating a full factorial (cont'd)

2. If desired, add extra center points*, request one or more replicates** and/or pre-sort the matrix. For a 2^k full-factorial, center runs are recommended. When you are ready, click *Make Table*.



*Each center point = one additional row (run)

**Each "replicate" = one additional set of 36 rows

4					
•			Time Period	Gift	% Yes
1	312	5	3	iPhone	
2	112	0	3	iPhone	
3	124	0	6	Espresso	
4	113	0	3	iPad	
5	232	2.5	9	iPhone	
6		2.5	9	None	
7	134	0	9	Espresso	
8	322	5	6	iPhone	
9	332	5	9	iPhone	
10	214	2.5	3	Espresso	
11	331	5	9	None	
12	121	0	6	None	
13	223	2,5	6	iPad	
14	314	5	3	Espresso	
15	323	5	6	iPad	
16	321	5	6	None	
17	123	0	6	iPad	
18	324	5	6	Espresso	
19	132	0	9	iPhone	
20	211	2.5	3	None	
21	222	2.5	6	iPhone	
22	311	5	3	None	
23	213	2.5	3	iPad	
24	333	5	9	iPad	
25	111	0	3	None	
26	221	2.5	6	None	
27	212	2.5	3	iPhone	
28	224	2.5	6	Espresso	
29	313	5	3	iPad	
30	334	5	9	Espresso	
31	233	2.5	9	iPad	
32	114	0	3	Espresso	
33	133	0	9	iPad	
34	234	2.5	9	Espresso	
35	122	0	6	iPhone	
36	131	0	9	None	

Notes			

Simulating response data (so we can see how analysis works)

3. Create two new columns called Pattern Intro APR Time Period Gift % Yes 1 312 3 iPhone Sent and Returned. 2 112 3 iPhone 1000 3 124 6 Espresso 1000 4 113 3 iPad 0 1000 4. Click on the Sent header \rightarrow 5 232 2.5 9 iPhone 1000 6 231 2.5 9 None 1000 double-click on the Sent header 7 134 9 Espresso 8 322 5 6 iPhone 1000 Column Properties→ select 9 332 9 iPhone 10 214 2.5 3 Espresso 1000 $Formula \rightarrow enter$ the value 1000 11 331 9 None 0 in the little box \rightarrow OK \rightarrow OK 12 121 6 None 1000 13 223 2,5 6 iPad 1000 14 314 3 Espresso 1000 15 323 6 iPad 5. The Returned column is where we 16 321 5 6 None 1000 17 123 0 6 iPad 1000 would enter the number of offers 18 324 5 6 Espresso 1000 19 132 0 9 iPhone 1000 accepted. To simulate the data, 20 211 2.5 3 None 1000 21 222 2.5 6 iPhone 1000 double-click on the header and 22 311 3 None 1000 5 name the column $\rightarrow Column$ 23 213 2.5 3 iPad 1000 24 333 5 9 iPad 1000 25 111 0 3 None 1000 $Properties \rightarrow Formula \rightarrow Edit$ 2.5 6 None 1000 26 221 Formula 27 212 2.5 3 iPhone 1000 28 224 2.5 6 Espresso 1000 29 313 5 3 iPad 1000 30 334 9 Espresso 1000 6. Enter the commands shown on 31 233 2.5 9 iPad 1000 32 114 0 3 Espresso 1000 the next slide, then click OK.

33 133

34 234

35 122

36 131

0

0

0

2.5

9 iPad

9 Espresso

6 iPhone

9 None

1000

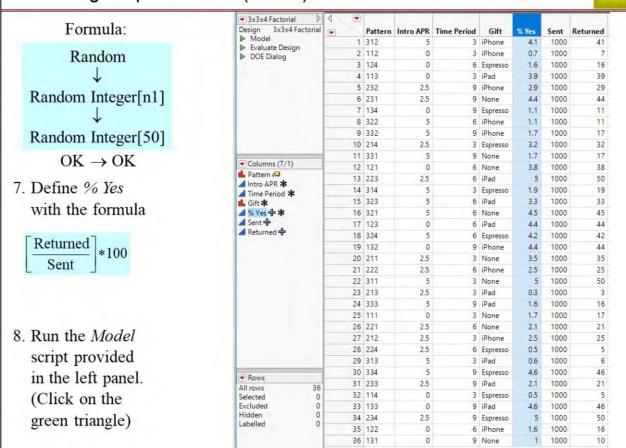
1000

1000

1000

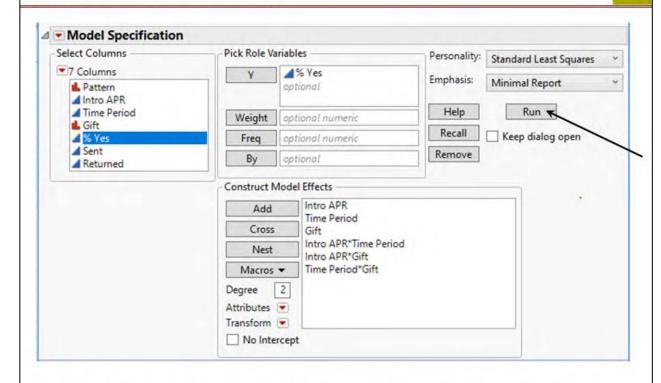
Notes			

Simulating response data (cont'd)



Notes			

Analyzing the simulated data

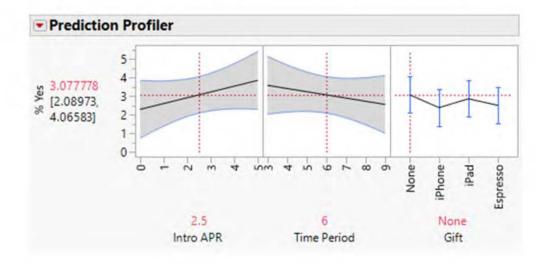


When you click Run, JMP will use regression to create a "model" for the process, that includes the terms under *Construct Model Effects*.

Notes			

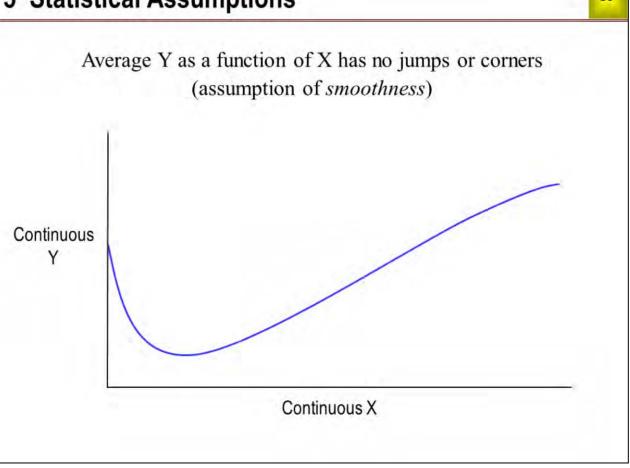
Getting to "yes"

- Point and click to find the combination with the highest % Yes
- Because it is simulated data:
 - o your profiler won't look exactly like this one
 - o don't be alarmed if your "best" combination doesn't make sense



Notes			

5 Statistical Assumptions



Notes			

A hypothetical smooth response function.

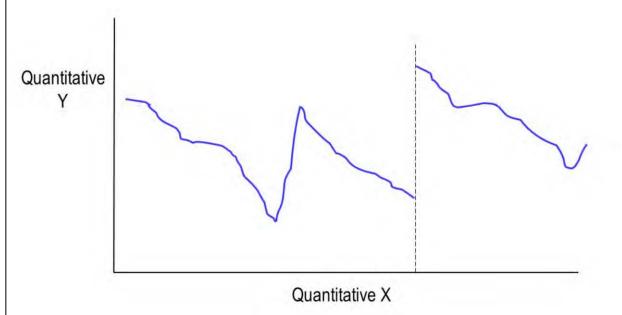
We never know the true response function, but often we have information about its general properties. For continuous X and Y, smoothness of the Y = f(X) relationship is one such property. It means the function can be well approximated over sufficiently short intervals by a polynomial, usually linear or quadratic. This is necessary in optimization experiments where we want to interpolate between the experimental design points.

These experiments are designed for continuous Y response. If you have a passfail response, see if you can turn it into a continuous response. Here are a few ideas:

- If you measure something on a continuous scale, but only record whether it
 passed or failed in your normal operation, record the actual measurement
 during the experiment.
- If you typically use a go-no go gauge, actually measure the part during the experiment.
- Record the size of defect instead of whether there is or is not a defect.
- Other ideas?

Notes			

Average Y as a function of X has jumps and/or corners



Notes			

A hypothetical non-smooth response function.

A function with jumps or sharp corners will not be well approximated by low-order polynomials in neighborhoods of the associated X values. This is a problem in optimization experiments because we want to interpolate.

It may or may not be a problem in screening experiments, because there we are merely trying to identify factors with large first-order effects. Accurate approximation throughout the X range is not required, although we may not be able to see the impact of the factor under certain circumstances. (You can see in the picture above that the response, Y, is at nearly the same level across various X values.)

Jumps and sharp corners often occur outside the feasible operating range of the process. In fact, such discontinuities often *define* the feasible operating range. A smooth response function is usually a safe assumption as long as we are not operating too close to a "cliff."

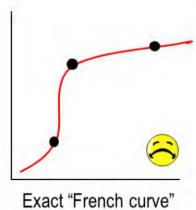
Notes			

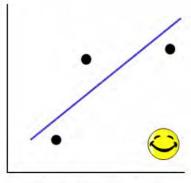
Occam's razor

"One should not increase, beyond what is necessary, the number of entities required to explain something."

-William of Occam, medieval philosopher







Linear plus noise

Notes			

Occam's razor represents a preference for simple explanations over complex ones. This reflects a belief that simple hypotheses are more likely to be true than complex ones. This belief is not always justified, but it is efficient in that it leads to models with just enough complexity to explain a given set of observations.

We can always find a sufficiently complex curve passing exactly through any given set of data points. The predictive ability of this "over-fitting" method is notoriously poor. The more successful "Occam" strategy is illustrated by random variation superimposed on a simple linear model.

Notes			

$$\vee$$
 Y = $f(X_1, X_2, X_3, ...) + error$

- \checkmark Can't assume f(X) explains everything (hence the error term)
- ✓ Can't assume f(X) is linear, but quadratic model is almost always sufficient
 - f(X) may include second order interactive effects
 - f(X) may include quadratic effects
- ✓ Don't need cubic or higher order models
 - · Don't need higher order interactive effects

Notes			

For each of 18 potato chip bags, we have data on

T = bonding temperature

D = bonding time (duration)

Y = bond strength

The best fitting response surface model (RSM) is the one whose parameters

$$b_0, b_1, b_2, b_3, b_4, b_5$$

minimize the sum of squared residuals:

$$\sum_{\{18 \text{ bags}\}} \left[Y - \left(b_0 + b_1 T + b_2 D + b_3 T D + b_4 T^2 + b_5 D^2 \right) \right]^2$$

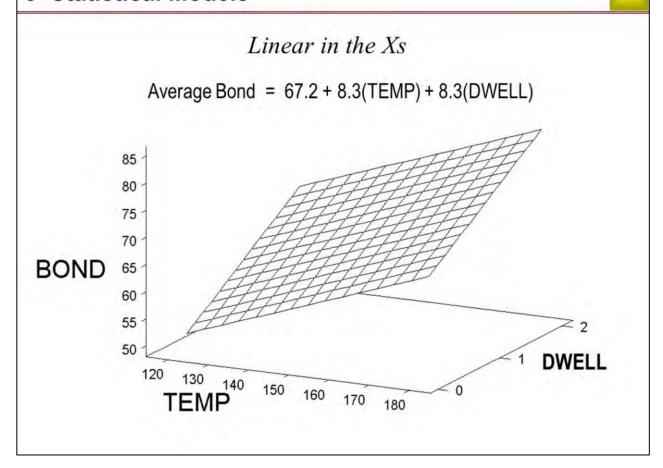
Notes			

Avg.
$$Y = 87.2 + 8.3(T) + 7.7(D) - 31.8(TD) - 16.1(T^2) - 13.2(D^2)$$

-1	Α	В	С	D E F	G	
1	TEMP	DWELL	BOND	Prediction	Noise	
2	-1	-1	11.0	10.08	0.92	
3	-1	-1	8.9	10.08	-1.18	
4	-1	0	63.9	62.80	1.10	
5	-1	0	60.4	62.80	-2.40	
6	-1	1	93.2	89.07	4.13	
7	-1	1	86.5	89.07	-2.57	
8	0	-1	65.7	66.30	-0.60	
9	0	-1	67.7	66.30	1.40	least squares
10	0	0	88.4	87.20	1.20	
11	0	0	88.0	87.20	0.80	modeling.xls
12	0	1	82.0	81.65	0.35	8
13	0	1	78.5	81.65	-3.15	
14	1	-1	88.1	90.37	-2.27	
15	1	-1	92.1	90.37	1.73	
16	1	0	77.2	79.45	-2.25	
17	1	0	81.0	79.45	1.55	
18	1	1	39.5	42.08	-2.58	6 terms in model
19	1	1	45.9	42.08	3.82	(equation shown above
20	Sum of	squares (SS)	93876.58	= 93792.35 +	84.18	
21	Degrees of	freedom (DF)	18	= 6 +	12	2.65 /04.40.442
22		RMSE	Square root	of noise (SS/DF)	2.65	$2.65 = \sqrt{84.18/12}$
23						

Notes			

6 Statistical Models



Notes			

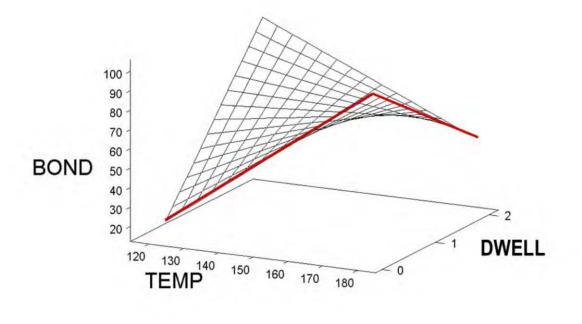
Response surface: tilted plane.

Simple linear models like the one shown above are used in screening designs. In many cases, simple linear models fit the data poorly, and do not give accurate predictions. They should not be used for optimization experiments.

Simple linear model: $Y = b_0 + b_1 x_1 + b_2 x_2 + \dots + b_k x_k$

Notes			

Avg. BOND = 67.2 + 8.3(TEMP) + 8.3(DWELL) - 31.5(TEMP \times DWELL)



_Notes			

Response surface: saddle.

Linear interaction models like the one shown above usually fit the data much better than simple linear models.

They include all main effects and all interaction effects.

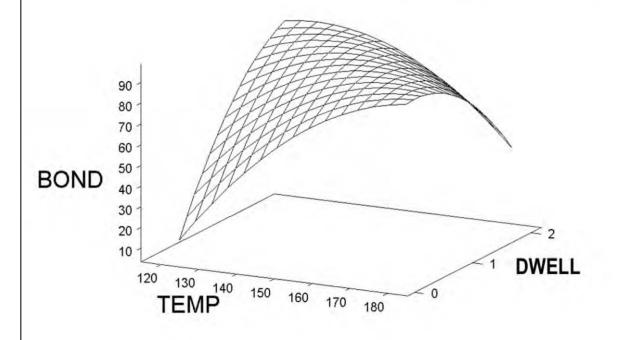
They are good for optimization experiments where all factors are categorical, but they should not be used for optimization experiments involving quantitative factors.

Linear interaction model:

$$Y = b_0 + b_1 x_1 + b_2 x_2 + \dots + b_i x_i + b_{12} x_1 x_2 + b_{13} x_1 x_3 + \dots + b_{ij} x_i x_j$$

Notes			

Avg. BOND = $86.8 + 8.3(TEMP) + 8.1(DWELL) - 32.4(TEMP \times DWELL)$ - $15.5(TEMP \times TEMP) - 12.9(DWELL \times DWELL)$



Notes			
·			

Response surface: ridge.

The response surface model (RSM) shown above is the <u>standard model for</u> optimization experiments.

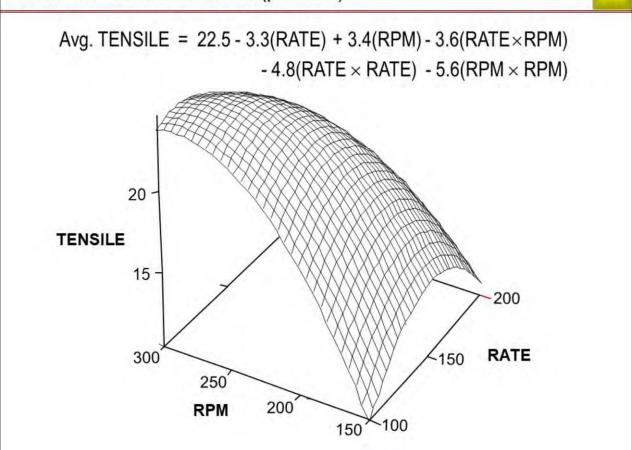
It differs from the linear interaction model in that it includes quadratic (squared) terms for all <u>continuous</u> factors, in addition to all main effects and interactions. Quadratic terms are never used with categorical factors.

In experiments involving continuous factors, the RSM may fit the data much better than the linear interaction model. In other words, the response surface model may be a better model of the process.

Response Surface Model RSM):

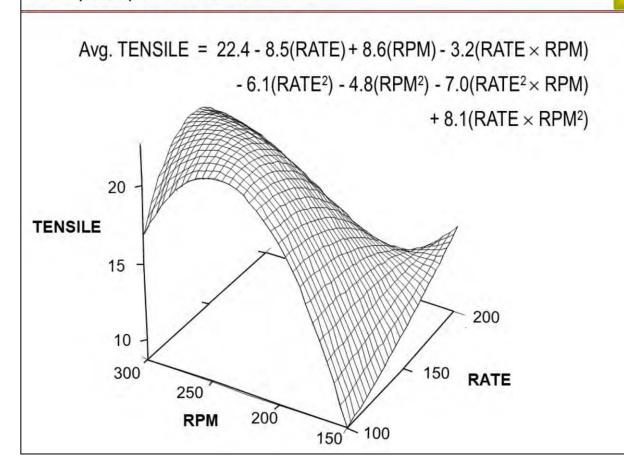
$$Y = b_0 + b_1 x_1 + b_2 x_2 + \dots + b_i x_i + b_{12} x_1 x_2 + b_{13} x_1 x_3 + \dots + b_{ij} x_i x_j + b_{11} x_1^2 + b_{22} x_2^2 + \dots + b_{ii} x_i^2$$

Notes			



Notes			

Notes	7
Response surface: hilltop.	
Other response surface shapes include inverted saddles, inverted ridges, a	nd bowls.
You can't tell from the plot alone, but in this example the RSM model doe data very well.	es not fit the
Notes	



<u>Notes</u>			

The s	shows a more	complicated	quadratic	model	fit to	the sa	me data	as on	the	previou	S
page.	This model	turns out to fi	t the data	well.							

Model terms like

RATE × RATE × RPM

 $RATE \times RPM \times RPM$

 $RATE \times RATE \times RPM \times RPM$

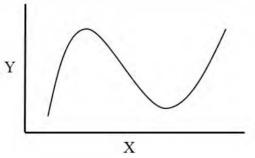
are called *quadratic interactions*. Adding one or more quadratic interactions is a good thing to try when an RSM model does not fit.

It is also possible to add other higher-level terms (cubic, three-way interactions), if the sample size is large enough to support the extra terms . . .

Notes			

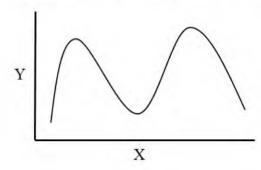
3rd order polynomial (cubic)

Avg.
$$Y = b_0 + b_1 X + b_2 X^2 + b_3 X^3$$



4th order polynomial (quartic)

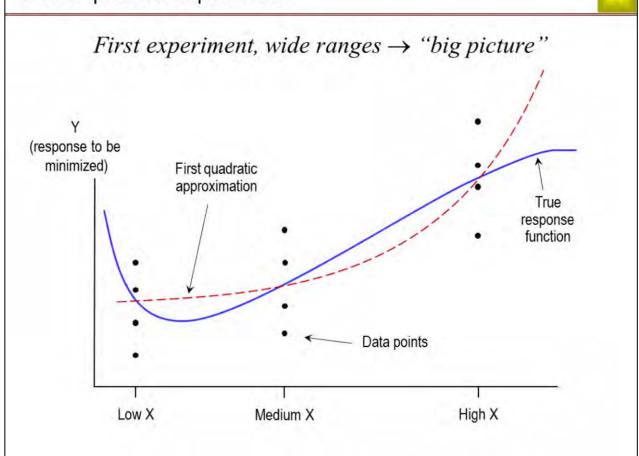
Avg.
$$Y = b_0 + b_1 X + b_2 X^2 + b_3 X^3 + b_4 X^4$$



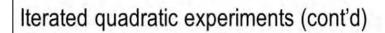
Notes			

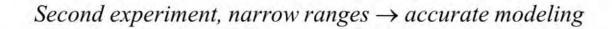
Notes
Even though third- or higher-order models may fit the data better than quadratic (second-order) models, they are rarely used in DOE. Why? They require much larger samples sizes for any given set of factors.
It is much more common to use quadratic models in an iterative fashion. A quadratic model may not fit the data well over a large initial factor space, but it almost always tells us which subset of the initial factor space is most likely to give the results we are looking for. The next step is to run another quadratric experiment in the smaller region. The smaller the factor space, the better the quadratic model will fit the data. This concept is illustrated on the next page.

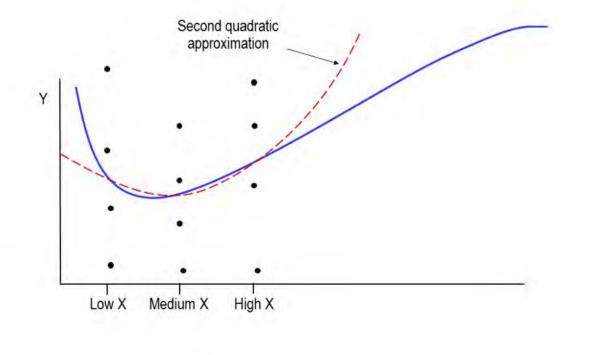
Notes			



Notes			





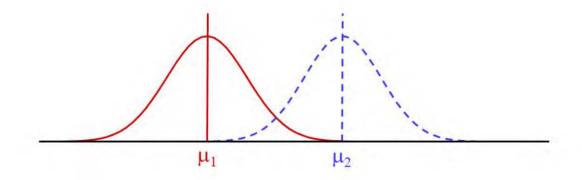


Notes			

Two-level categorical factor

MATL = Steel or Rubber

$$Average\ COST\ = \left\{ \begin{aligned} \mu_1 & \quad \text{if}\ \ MATL = Steel} \\ \mu_2 & \quad \text{if}\ \ MATL = Rubber} \end{aligned} \right.$$



Notes			

Categorical factors are represented by *indicator* variables (also known as *dummy* variables)

Average COST =
$$b_0 + b_1 MATL[Steel]$$

$$MATL[Steel] \ = \ \begin{cases} 1 & if \ MATL = Steel \\ -1 & if \ MATL = Rubber \end{cases}$$

Notes			

Simple linear model with all factors categorical

```
Avg. COST = b_0
                                         4.868125
                                                        "High" ⇒ -0.616875
               + b_1 LGR[Low]
                                         + Match [LGR]
                                                        "Low" ⇒ 0.616875
                                                        else
               + b<sub>2</sub> MATL[Steel]
                                                         "Rubber" ⇒ 1.145625
               + b<sub>3</sub> USAGE[50%]
                                        + Match MATL
                                                         "Steel"
                                                                  ⇒-1.145625
                                                         else
               + b_4 GRIT[30]
                                                           "50%" ⇒ 1.054375
                                        + Match USAGE
                                                           "75%" ⇒ -1.054375
                                                           else
· Analogy: blue book pricing of used cars
                                                         "30" ⇒ -0.048125
· Base price + extra for power windows
                                        + Match GRIT
                                                         "50" ⇒ 0.048125
           + extra for air conditioning
           + extra for cruise control
                                                         else ⇒.
           etc.
```

Notes			

Categorical interaction model

Avg.	COST	=	b_0

+ b₁LGR[Low]

+ b₂ MATL[Steel]

+ b₃ USAGE[50%]

# Factors	4	5	6
Full factorial (FF)	16	32	64
Min. sample size	11	16	22
% of FF	69	50	34

- $+ b_4 GRIT[30]$
- + $b_5 LGR[Low] \times MATL[Steel]$
- + $b_6 LGR[Low] \times USAGE[50\%]$
- + $b_7 LGR[Low] \times GRIT[30]$
- + b_8 MATL[Steel] × USAGE[50%]
- + b_9 MATL[Steel] × GRIT[30]
- + b_{10} USAGE[50%] × GRIT[30]

Notes			

7 Design Principles

- Bold strategy
- · "Control group"
- Replication
- · Randomization
- · "Blocking"

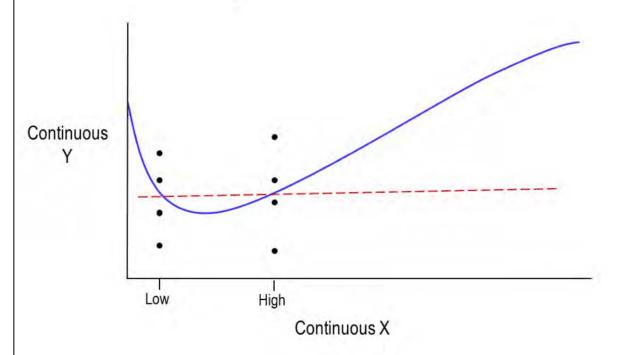
Notes			

Bold strategy

Continuous Y Linear approximation True response function (X, Y) data points Continuous X High

Notes			

- Low and high levels of X are too close together
- We mistakenly conclude that X has no effect on Y



Notes			

For each factor, one of the levels should match the current process

- Ideally, this is the middle level for continuous factors
- At least one run in the experiment should match the current process settings, for a "sanity check"
- In these types of designs, we don't usually refer to this as a "control group"

Temp	Press	Dwell	Mat'l
120	50	0.2	A
120	100	1.1	В
120	150	2.0	C
150	50	1.1	C
150	100	2.0	$\left(A\right)$
150	150	0.2	В
180	50	2.0	В
180	100	0.2	С
180	150	1.1	A

Notes				

Notes
The units involved in a DOE may turn out to be uniformly different from those in current production – either better or worse. This can be due to the effects of noise variables on production units, or to special circumstances surrounding the creation and handling of experimental units.
For each factor, one of the DOE levels should match the current state value of that factor. This allows valid comparisons between current state and experimental process settings. This is especially important when non-routine measurements, tests or inspections are applied to experimental units.
Notes

Notes			

Replication

		E	xperimental
Usa a vanliaata ov a	Temp	Press	units
Use a replicate or a replicate run to	120	50	1
quantify the error	120	50	2
in the experiment.	120	150	3
	120	150	4
This improves estimates	180	50	5
of coefficients and	180	50	6
precision in determining factor significance.	180	150	7
jacior significance.	180	150	8

Notes			

Notes

Replication forces redundancy into the experiment. This is necessary for two reasons:

- To quantify the magnitude of error in the experimental data differences between units at the same design point are, by definition, due to error (variation in the process that is not accounted for in the factors).
- To reduce the influence of error on the experimental results by estimating "pure error." This increases the signal-to-noise ratios.

Assume that you are the person responsible for running the experiment and for the validity of the results. Is there anything about the run order shown above that makes you nervous? Please explain.

Notes			

Randomization

		E	xperimental
	Temp	Press	units
Use a random number	120	150	1
generator to determine	180	50	2
the sequence in which experimental units are	180	50	3
created and tested	120	150	4
(JMP does this for you.)	180	50	5
	120	150	6
	180	150	7
	120	50	8

Notes			

Randomization

Benefits

- Reduces the chance of biased results due to nuisance variables (factors not included in the experiment that may be changing while the experiment is being conducted)
- •Doesn't require control of nuisance variables, which may be unknown or uncontrollable
- ·Results are more convincing to skeptics

What happens if you don't randomize?

- · Nuisance (noise) variables may be changing during your experiment
- This increases the chance of drawing the wrong conclusions from your experiment (significant factors, best levels, etc.)
- · Randomization guards against this

Drawbacks

- · Impractical when some of the factors are hard to change
- ·We'll see what to do about this later

Notes		

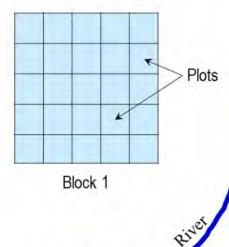
Blocking

		E	xperiment	al
	Temp	Press	units	
Blocking allows you to	120	50	1	Block_1
account for some nuisance variables	120	150	2	Operator Bob Shift 1
	180	150	3	Machine A Material Lot 6
 Nuisance variables or factors are used to divide the experiment into 	180	50	4	
homogeneous "blocks"	180	150	5	Block 2
 Effects of nuisance factors are separated from effects 	180	50	6	Operator Carol Shift 2
of other factors, for more accurate analysis of factor	120	50	7	Machine B Material Lot 7
significance	120	150	8	

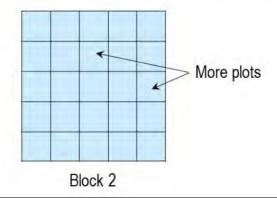
Notes			

Agricultural origin of "blocking"

- · Want to increase crop yields
- · Experimental units are plots of land in a field
- · Compare varieties, fertilizers, etc.



- Need 50 plots (runs), not 25
- · Have to use a second field
- Differences in the soil will cause differences in yields



Notes		

Why use blocking?

- Use blocking when experimental runs cannot be completed within a timeframe (shift, time allotted on a machine, etc.) or some other constraint (batch of material, space, etc.)
- Blocking systematically eliminates the effect of known, controllable nuisance (noise) factors
 - o Makes predictions more reliable
 - Quantifies the effects of nuisance variables
- Improves precision with which treatment means are compared, without increasing sample size
 - Makes identification of important (significant) factors more reliable
- Protects against variation due to known factors not included in the experiment

Notes			

8 The Custom Design Process

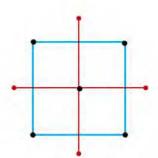
We saw the Full-Factorial Design earlier, and learned:

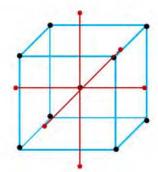
- A 2^k full-factorial design can estimate main effects and interactions, but cannot estimate quadratic terms
- A three level full-factorial (3^k) design can estimate main effects, interactions and quadratic effects, but is an inefficient design.

Let's look at some other designs.

Notes			

Response Surface Designs





The central composite design (CCD) is a 2^k factorial with added axial or star runs.

It is (was) the most used response surface design when all factors are continuous

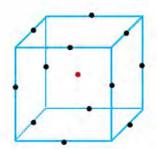
Above are images of two and three factor CCDs

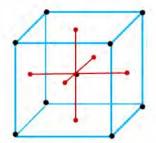
- The CCD requires two axial runs for each factor, plus the 2^k design runs
- 3-5 center points are recommended
- Total runs required for the 3-factor CCD are 8 + 6 + center points = 17-19.

A Response Surface Design can estimate main effects, 2-factor interactions and quadratic effects, with more efficiency than the 3^k full-factorial.

Notes			

Response Surface Designs (cont'd)





Box-Behnken designs (left) are spherical, and do not have any points on the corners of the "cube" contained by the limits of the factors.

The face-centered cube (right) is a variation on the Central Composite Design, with axial points on the centers of the faces of the cube (for k=3).

- 3 5 center points are recommended for each of these designs
- Total runs required for the 3-factor Box-Behnken design is 15-17.
- Total runs required for the face-centered cube is the same as the CCD (17-19).

As Response Surface Designs, these can estimate main effects, 2-factor interactions and quadratic effects.

Notes			

Custom Designs

JMP's Custom Design platform uses modern computing power to employ a coordinate-exchange algorithm for determining the best set of points to use in a Response Surface Design, creating an "optimal design."

Often, fewer runs are required than the classical designs just presented.

When you look at the points chosen for your experiment, you may notice:

- · Center points--all continuous factors at the middle level of the range given
- · Points at the corners of the "cube"--all factors at high or low levels
- Points in the centers of the "cube" edges (Box-Behnken) or faces (face-centered cube)—some factors at the middle level, others at high or low levels
- · You will not see axial runs extending beyond the "cube," as in the original CCD

Because fewer runs are used in these designs, there will be some correlations and aliasing between terms.

(See Design Evaluation > Color Map on Correlations)

Notes			

Steps for Creating a Custom Design

- 1. Specify the Responses and general goals (maximize, minimize, or match target).
- 2. Specify the Factors.
 - For continuous factors, specify the high and low levels.
 - · For categorical factors, specify each level to be included in the experiment.
- 3. Specify the statistical Model (usually RSM).
- 4. Specify the blocking factor, if blocking is needed. (Click RSM again)
 - Enter the maximum number of runs that can be completed in one block (timeframe, batch of material, etc.).
 - JMP will evenly split required runs into blocks no larger than the number specified
- 5. Create the design matrix. (Make Design)
- 6. If desired, use *Design Evaluation* > *Power Analysis* to determine sample size.
- 7. Back up to make changes (Back), or create the data table (Make Table).
- 8. Save the table.

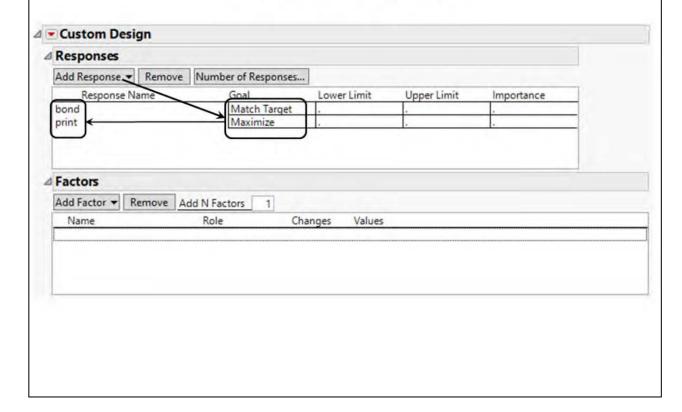
Later: Run the experiment in the order given. Enter results into table.

Notes			

1. Specify the Responses and general goals

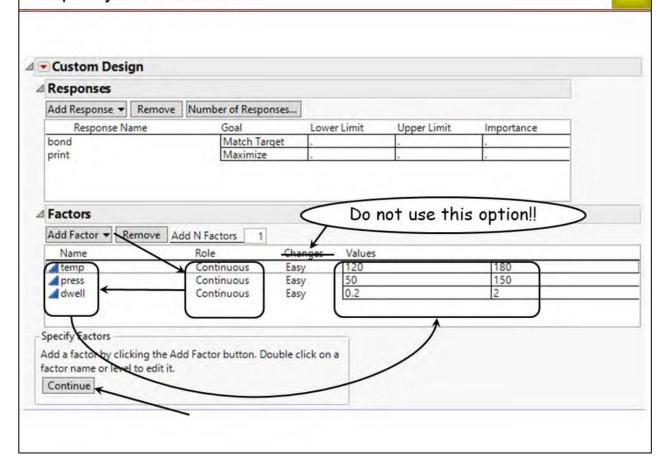


DOE → Custom Design

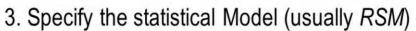


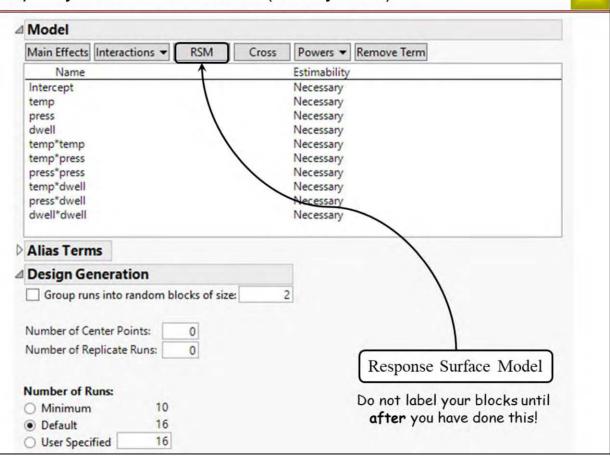
Notes			

2. Specify the Factors



Notes			





Notes			

4. Specify the blocking factor, if blocking is needed.

Once you specify the Model, the Default and Minimum Number of Runs are displayed.

Use this information, or User Specified Number of Runs (another sample size you've determined), to decide whether Blocking is needed.

It's not a bad idea to split your experiment into blocks just in case, if it is likely to take several hours or more to complete. For example, you may have a block size equal to half of a shift, just in case there's an evacuation, or the machine goes down, or you get called away urgently, and cannot complete the experiment all at one time.

If Blocking is needed:

- Click User Specified Number of Runs, even if you want to use the Default (this prevents JMP from increasing the sample size to a multiple of the block size),
- 2. Go back up to Factors to enter a Blocking factor,
- 3. Specify Model (click RSM) again.

Notes			

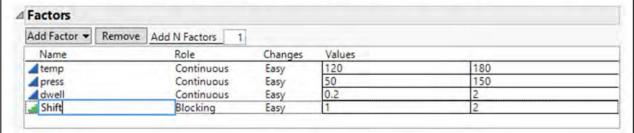
4. Specify the blocking factor, if blocking is needed. (cont'd)

Select User Specified Number of Runs to prevent an increase due to blocking △ Design Generation Group runs into random blocks of size: Number of Center Points: Number of Replicate Runs: Number of Runs: 10 O Minimum O Default User Specified Make Design Go back up to factor specification: Add Factor > Blocking > Select the maximum runs possible per block If your maximum is not listed, select Other... to Specify Number of Runs per Block Please Enter a Number × 16 Specify Number of Runs per Block OK Cancel

Notes			
_			

4. Specify the blocking factor, if blocking is needed. (cont'd)

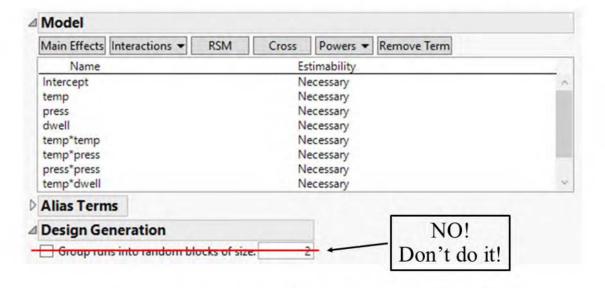
· Name the Blocking factor, so you will recognize it in the Design Matrix and Table:



- You do not need to be concerned about how many "levels" are shown under "Values." JMP will handle this when it creates the design.
- Re-specify the Model. (Click RSM again.) Click through JMP comments about categorical and blocking factors in RSM models.

Notes			

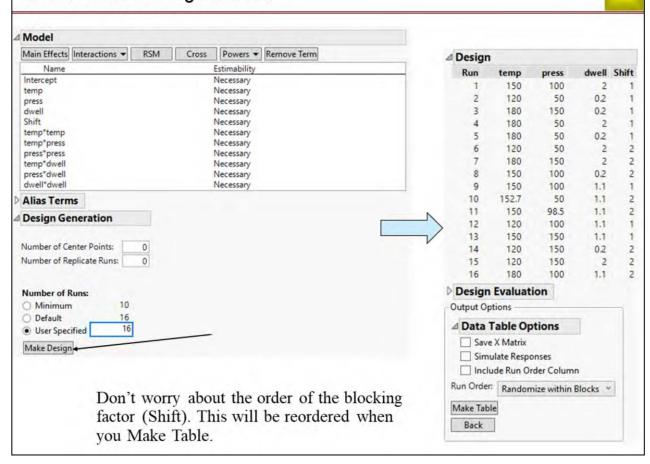
DO NOT use this option for setting up a blocking factor!



JMP will generate uneven block sizes, if this option is used.

Notes			

5. Create the Design Matrix.



Notes			

6. If desired, use Power Analysis* to determine sample size.

Design Evaluation > Power Analysis

Power An	alysi	s	
Significance	Level	0.05	
Anticipated I	RMSE	1	
Term		ipated ficient	Power
Intercept		1	0.402
temp		1	0.706
press		1	0.706
dwell		1	0.705
Shift		1	0.865
temp*temp		1	0.262
temp*press		1	0.623
press*press		1	0.262
temp*dwell		1	0.623
press*dwell		1	0.623
dwell*dwell		1	0.263

* Details of this procedure are presented later, in the Determining Sample Size section.

Notes			

7. Back up to make changes or create the data table.

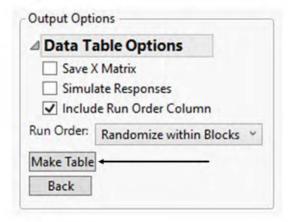
- Click Back to back up and adjust sample size.
- Adjust User Specified Number of Runs
- Click Make Design



Once the design is as needed:

- Check Include Run Order Column
- · click Make Table

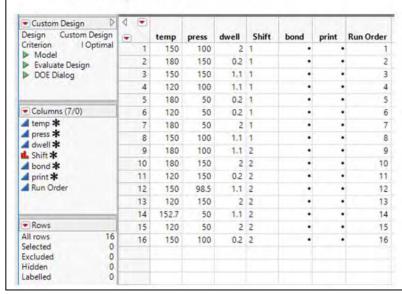
JMP creates an editable table.



Notes			

8. Save the table.

- You can reorder columns and adjust any odd factor levels by entering the desired value
 - o Odd levels are an artifact of the procedure JMP uses to create custom designs
 - Before creating the table, you can also back up to create another design, and see if that takes care of it
 - In this example, temp of 152.7 would be changed to 150, press of 98.5 would be changed to 100



- Run your experiment in the order specified and enter data into this table.
- If data is entered directly into the table as the experiment is performed, it's not a bad idea to print a copy of the table and keep a hard copy also, as you go . . . just in case.

Notes			

Exercises

Use the (Custom	Design	process	described	on the pre	evious	slides to	create Respo	nse
Surface of	designs	for the	exercises	on the fo	llowing pa	ages. In	addition	to special	
instructio	ons give	n in eac	h case,	follow the	se general	instruc	ctions:		

- Determine whether each factor is continuous or categorical
- Use the sample size given to determine if blocking is needed.
- For each exercise, have the instructor review your matrix when you are finished.
- · Make and save each design table.

Notes			

Control factors	Levels		
Heat treat	Anneal	Solution/age	
Polish	Chemical	Mechanical	
Peen	Yes	No	

• Response variable: Cycles to failure

· Blocking factor: none

• Experimental unit: one small test piece

• Sample size: 12 (constraint due to availability of test fixtures)

Notes			

Exercise 8.2

Control factors	Lev	vels
Contact wheel land-groove ratio (LGR)	Low	High
Contact wheel material (Material)	Steel	Rubber
Belt usage limit (Usage)	50%	80%
Belt grit size (Grit)	"30"	"50"

- · Response variable: Cost
- Blocking: At most, 10 runs can be completed in a morning or an afternoon. You want to split the runs evenly between two blocks.
- Blocking factor: Time of day (morning vs. afternoon)
- · Experimental unit: one large casting
- Sample size: Use the default sample size. Enter it here _______

Notes			

Exercise 8.3

Control factors	Ranges	
Force	70 to 150	
Energy	275 to 325	
Amplitude	70 to 90	

- · Response variable: Leak rate
- Blocking constraint: Due to production needs, a maximum of 20 containers can be molded in each tool cavity
- Blocking factor: Cavity (parts are molded from 4 tool cavities)
- · Experimental unit: one welded plastic container
- Sample size for experiment: 68

Notes			

9 Determining Sample Size for an Experiment

Sampl	e size.	N.	is	the	total	number	of	"runs"	in	the	experiment.
		7	100				-				

How should sample size be determined?

- First, you must have <u>at least</u> one run for each model term.
 More factors and more complex model → more terms and more runs
- Second, your purpose must be clear for a given experiment.

Process optimization with RSM require more runs for each factor than experiments for screening for important factors

Less ambiguity in results → more runs

 Beyond that, there are several answers to the question of how to determine sample size. Two are presented on the following slides.

Notes			

How should sample size be determined? (cont'd)

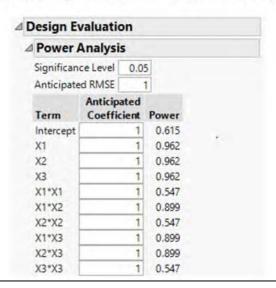
- The quickest answer that most statisticians experienced in experimentation give, is that the sample size depends on your budget. Run the best designed experiment you can, within your budgetary constraints.
 - Think through your experimental strategy before running your first experiment
 - Don't use more than about 25% of your entire budget on your first experiment
 - Compare potential designs with Design Diagnostics > Compare Designs
 - Fraction of Design Space Plot, when prediction using the model, is a goal
 - Color Map on Correlations, whenever less than a full-factorial is used

Notes			

How should sample size be determined? (cont'd)

2. Use JMP's Design Evaluation > Power Analysis to ensure that:

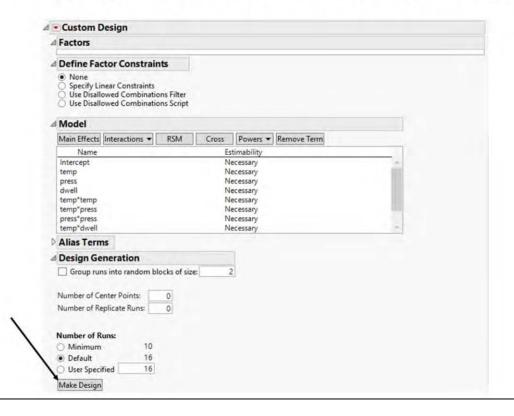
- Main Effects (e.g. Temp, Dwell, X1) have a Power of 0.9 to 0.8
- Interactions (e.g. Temp x Dwell, X1*X2) have a Power of about 0.8
- Quadratic Terms (e.g. Temp x Temp, X1*X1) have a Power of about 0.5
- Use the Power Analysis as it is when you open it, without changing Anticipated RMSE or Coefficients (this allows good detection of effects with $\beta_n \ge \text{RMSE}$)
- Adjust Power by going Back and changing the User Specified Number of Runs



Notes			

Example: Using Power Analysis to Determine Sample Size

Set up Responses, Factors and Model, then click Make Design



Notes			

Example: Using Power Analysis to Determine Sample Size (cont'd)

Click on the triangle next to Design Evaluation, then on the triangle next to Power Analysis to open the Power Analysis report:

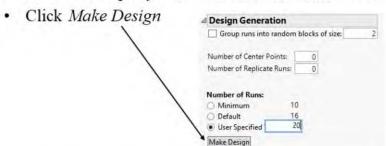
n		△ Design Eva	uation	
K	eview the Power Analysis to	△ Power An	alysis	
le	termine if all:	Significance Anticipated F	4.15	
	Main Effects (e.g. temp, dwell, X1) have a Power of 0.9 to 0.8	Term	Anticipated Coefficient	Power
	have a Power of 0.9 to 0.8	Intercept	1	0.427
	T-4	temp	. 1	0.75
	Interactions (e.g. temp*dwell,	press	1	0.75
	X1*X2) have a Power of about 0.8	dwell	1	0.75
		temp*temp	1	0.278
	Quadratic Terms (e.g. dwell*dwell,	temp*press	1	0.657
		press*press	. 1	0.278
	X1*X1) have a Power of about 0.5	temp*dwell	1	0.657
		press*dwell	1	0.657
		dwell*dwell	1	0.278

In this example, all Power values are too low. The sample size needs to be increased.

Notes			

Example: Using Power Analysis to Determine Sample Size (cont'd)

- · Click Back.
- · Select User Specified and increase the Number of Runs.



- Review the Power Analysis report again, to determine whether the power levels meet the requirements.
 - o This may require several iterations
 - o If you overshoot, go back and reduce the number of runs

Notes			

Example: Using Power Analysis to Determine Sample Size (cont'd)

It took 25 runs for all model terms to exceed the desired power.

(Because every design is a little different, it's possible that a design of 24 or 26 runs could (eventually) be generated that exceed the desired power levels.)

An experimenter may choose a slightly smaller sample size, as the desired power levels are approximate ("about 0.8") and are usually conservative.

esign Eva	luatio	on	
Power An	alysi	s	
Significance	Level	0.05	
Anticipated F	RMSE	1	
Term		ipated ficient	Power
Intercept		1	0.615
temp		1	0.962
press		1	0.962
dwell		1	0.962
temp*temp		1	0.547
temp*press		1	0.899
press*press		1	0.547
temp*dwell		1	0.899
press*dwell		1	0.899
dwell*dwell		1	0.547

Notes			

Power Analysis with Categorical Factors at more than 2 Levels

When categorical factors are at more than two levels, the Power Analysis report gets a little messy.

	△ Design Evaluation				
	△ Power Analysis				
	Significance Level 0.05 Anticipated RMSE 1				
Use the upper part of the Power Analysis, as before, for all continuous factor: o main effects o interactions o quadratic terms		Anticipated Coefficient	Power 0.442 0.882 0.877 0.575 0.631 0.575 0.297 0.838		
The decline which halos for all consider for all	Time Period*Time Period Intro APR*Gift 1 Intro APR*Gift 2 Intro APR*Gift 3 Time Period*Gift 1 Time Period*Gift 2 Time Period*Gift 3	1 -1 1 1 -1	0.307 0.477 0.477 0.477 0.476 0.476 0.476		
Use the little table below for all categorical factor: o main effects o interactions that include categorical factors	Apply Changes to Anticipal Effect Power → Gift 0.763 → Intro APR*Gift 0.633 Time Period*Gift 0.629	ted Coefficier	nts		

Notes			

Exercise 9.1

We are planning an experiment to optimize a monofilament extrusion process with 4 continuous factors X1 to X4. The response variable is *tensile strength*.

- Optimization experiment = Response Surface Model needed
- Use the Custom Design platform to design this experiment
- Using the Power Analysis method, determine the sample size (number of runs)
 required in this experiment [For consistency among class participants, find the
 smallest sample size that puts all factors over the recommended power levels.]

Notes			

We are planning an experiment to optimize an ultrasonic welding process with 3 continuous factors and a 4-level categorical factor. The response variable is the *weld depth*.

- Optimization experiment = Response Surface Model needed
- Use the Custom Design platform to design this experiment
- Using the Power Analysis method, determine the sample size (number of runs)
 required in this experiment [For consistency among class participants, find the
 smallest sample size that puts all factors over the recommended power levels.]

Notes			

10 DOE Workshop	11
Notes	
Notes	

11 Experiments with Hard-to-Change Factors

Sometimes it's not feasible to completely randomize, because a factor is hard-to-change

There are many situations when this is the case. Here are a few examples:

- Temperature in a furnace <u>takes a very long time</u> (hours) to stabilize after changing
- Special material needed (a factor) are made in <u>large batches</u> and cannot be stored, or it is run in a continuous flow through the process
- Material or part used in a machine is <u>difficult to change</u>, requiring a complete breakdown and cleaning
- Type of irrigation on a plot of land is very difficult and costly to change (an example of the origin of split-plot designs)

What are examples in your workplace?

Notes			

Experiments with Hard-to-change factors (cont'd)

When you have hard-to-change factors that cannot be randomized, you need to create and analyze your experiment as a "split-plot" design

If you don't do this (if you design and analyze as usual), you are more likely to:

- · Conclude that unimportant factors are important among the hard-to-change factors
 - o You think that a factor (X) is impacting your response (Y), when it is not
 - o This is a Type I error
 - Hard-to-change factors are those in the "Whole Plots" or main treatments, that were not randomized
- · Fail to recognize factors that are significant among the easy-to-change factors
 - You think that a factor (X) is NOT impacting your response (Y), when it is
 - o This is a Type II error
 - Easy-to-change factors are those in the "Subplots" or split-plots, that were randomized

Notes			

Experiments with Hard-to-change factors (cont'd)

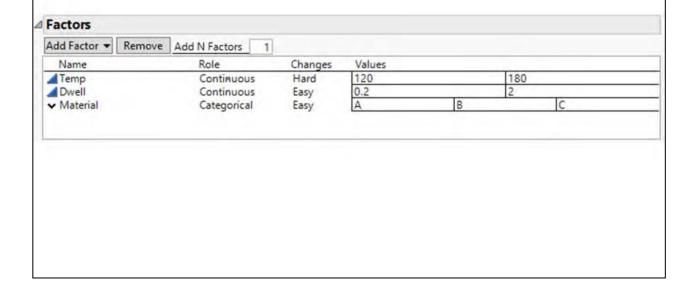
The decision to consider a factor as "hard-to-change" should not be taken lightly

- Subplot (easy-to-change) factors are compared with higher precision
 - O Usually, subplot error is smaller than whole-plot error
 - Whenever possible, the treatment(s) or factors we are most interested in should be assigned to the subplots
- To increase the precision of the test on whole-plot (hard-to-change) factors, additional replicates of the experiment or additional whole-plots are needed
 - Clearly, this takes more time and resources
 - Several (3-6) replicates could be needed to gain an adequate level of precision
 - o So, you could be back to changing that hard-to-change factor many times

Notes			

Creating a Split-Plot Design

- DOE > Custom Design
- Enter the factors as usual, except double-click on "Changes" and change to Hard for the hard to change factor
- · Click Continue

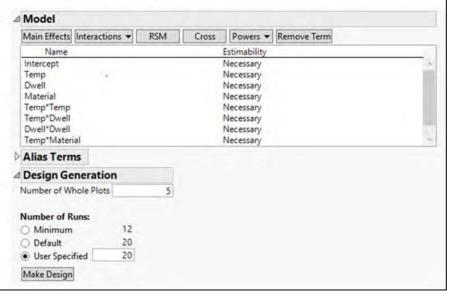


Notes			

Creating a Split-Plot Design (cont'd)

- Click on RSM.
- JMP will suggest a reasonable number of Whole Plots for the number of factors and levels entered
- The number of Whole Plots shows the number of times the hard-to-change factor will need to be changed in the experiment
- Click Make Design

 Model



Notes			

Creating a Split-Plot Design (cont'd)

- The design is presented.
- As before, click Back to make adjustments. Click Make Table.
- Run the experiment in the order shown in the table.

Desig	ın			
Run	Whole Plots	Temp	Dwell	Material
1	1	150	1.1	Д
2	1	150	0.2	C
3	1	150	0.2	В
4	1	150	2	Е
5	2	180	0.2	Д
6	2	180	1.1	(
7	2	180	1.1	E
8	2	180	2	A
9	3	120	0.2	A
10	3	120	1.1	(
11	3	120	2	A
12	3	120	1.1	E
13	4	150	1.1	E
14	4	150	0.2	(
15	4	150	2	(
16	4	150	1.1	A
17	5	150	0.2	E
18	5	150	1.1	A
19	5	150	2	E
20	5	150	2	0

Table:

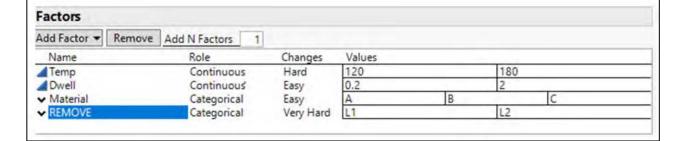
Whole Plots	Temp	Dwell	Material	Y1
1	150	1.1	A	
1	150	0.2	C	
1	150	0.2	В	•
1	150	2	В	
2	180	0.2	A	
2	180	1.1	С	
2	180	1.1	В	
2	180	2	A	
3	120	0.2	A	
3	120	1.1	C	
3	120	2	A	
3	120	1.1	В	
4	150	1.1	В	
4	150	0.2	C	
4	150	2	C	
4	150	1.1	A	
5	150	0.2	В	
5	150	1.1	A	
5	150	2	В	
5	150	2	C	

Notes			

Blocking in a Split-Plot Design

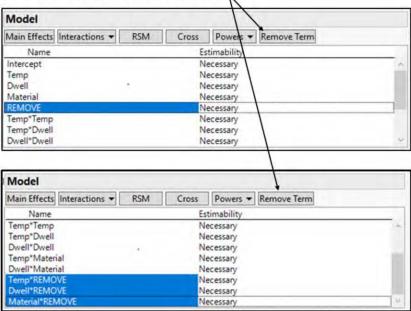
What if there are too many runs to complete in one day (or lot of material, or by one tester, etc.)?

- Once you see that there are too many runs, click Back (before making the table)
- Add a Categorical Factor with the number of levels as the number of batches or days or shifts, etc. needed for the experiment (In this example, two days will be needed to run the experiment, so a 2-Level Categorical Factor was added.)
- Name the factor something that you can easily pick out of the lists of terms (Here it is named REMOVE.)
- · Set Changes for this factor to Very Hard
- · Click Continue



Notes			

- Click RSM
- Remove from the Model every term that contains the Categorical factor that you added
 - Highlight the term then click Remove Term



Notes			

- Change the number of Whole Plots to the number of levels of the Categorical Factor
 - · In this example, two days were needed
 - · So, a 2-Level Categorical Factor called REMOVE was added
 - Now, the Number of Whole Plots is changed to 2
- Click make Design

Design Generation	n				
☐ Hard to change fact	ors can va	ry indeper	ndently of	Very Hard	to change factors.
Number of Whole Plots		2			
Number of Subplots		6			
	1.0				
Number of Runs:					
○ Minimum	12				
Default	18				
O User Specified	18				
Make Design					

Notes			

- · The Design is developed
- · Whole Plots show the number of days required
- REMOVE is still in the table, as it was entered as a factor
- Click Make Table

Desig	jn .					
Run	Whole Plots	Subplots	Temp	Dwell	Material	REMOVE
1	1	1	120	0.2	C	L1
2	1	1	120	2	A	LI
3	1	1	120	1.1	В	Li
4	1	2	180	2	C	LI
5	1	2	180	0.2	A	LI
6	1	2	180	1.1	В	L
7	1	3	150	1.1	C	Li
8	1	3	150	1.1	A	L
9	1	3	150	2	В	L
10	2	4	120	1.1	В	LI
11	2	4	120	0.2	A	L
12	2	4	120	2	C	Li
13	2	5	150	0.2	В	L
14	2	5	150	1.1	C	L
15	2	5	150	1.1	A	L
16	2	6	180	1.1	В	LI
17	2	6	180	2	A	L
18	2	6	180	0.2	C	L1

If you get this warning, it's okay to ignore it, IN THIS CASE, because you are not trying to estimate effects of the whole plot

At least one more whole plot is strongly recommended. This design does not have enough whole plots to estimate the whole plot variance. The whole plot effects are not testable.

Notes			

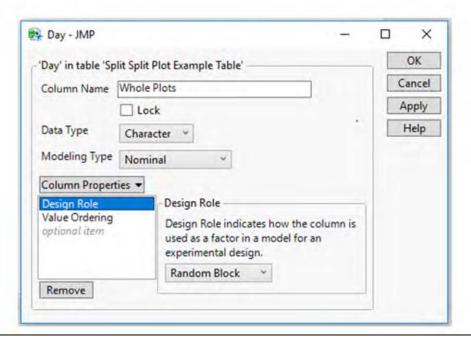
- The table is generated
- Click on the column of the Categorical Factor ("REMOVE" in this example).
- Cols > Delete Columns to delete the column from the table

Whole Plots	Subplots	Temp	Dwell	Material	REMOVE	Y1
1	1	120	0.2	C	L1	
1	1	120	2	A	L1	
1	1	120	1.1	В	L1	
1	2	180	2	C	L1	
1	2	180	0.2	A	L1	
1	2	180	1.1	В	L1	
1	3	150	1.1	C	L1	
1	3	150	1.1	A	L1	
1	3	150	2	В	L1	
2	4	120	1.1	В	L1	
2	4	120	0.2	A	L1	
2	4	120	2	C	L1	
2	5	150	0.2	В	L1	
2	5	150	1.1	C	L1	
2	5	150	1.1	A	L1	
2	6	180	1.1	В	L1	
2	6	180	2	A	L1	
2	6	180	0.2	C	L1	

Whole Plots	Subplots	Temp	Dwell	Material	REMOVE	Y1
1	1	120	0.2	C	L1	
1	1	120	2	Α	L1	
1	1	120	1.1	В	L1	
1	2	180	2	C	L1	
1	2	180	0.2	A	L1	
1	2	180	1.1	В	L1	
1	3	150	1.1	C	L1	
1	3	150	1.1	A	L1	
1	3	150	2	В	L1	
2	4	120	1.1	В	L1	
2	4	120	0.2	A	L1	
2	4	120	2	C	L1	
2	5	150	0.2	В	L1	
2	5	150	1.1	C	L1	
2	5	150	1.1	A	L1	
2	6	180	1.1	В	L1	
2	6	180	2	A	L1	
2	6	180	0.2	C	L1	

Notes			

- If you open the Column Info for Whole Plots, you'll see that the Design Role is Random Block (JMP is pretty smart!)
- · Rename the Whole Plots column with the name of your block



Notes			

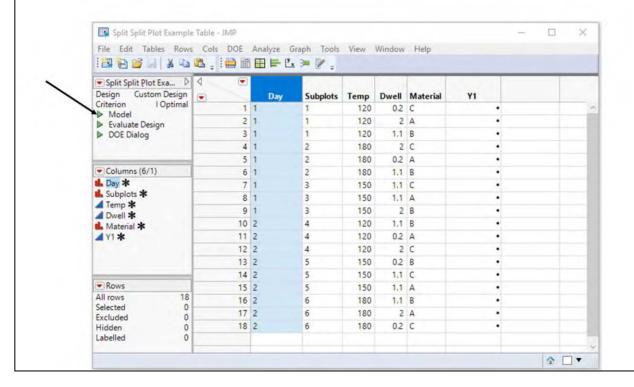
- This shows the final table, with Whole Plots renamed to Day
- · This experiment is designed to be run in two days
- What you actually have now is a split-split-plot design

Day	Subplots	Temp	Dwell	Material	Y1
1	1	120	0.2	C	
1	1	120	2	A	
1	1	120	1.1	В	
1	2	180	2	C	
1	2	180	0.2	A	
1	2	180	1.1	В	
1	3	150	• 1.1	C	
1	3	150	1.1	A	
1	3	150	2	В	
2	4	120	1.1	В	
2	4	120	0.2	A	
2	4	120	2	C	
2	5	150	0.2	В	
2	5	150	1.1	C	
2	5	150	1.1	A	
2	6	180	1.1	В	
2	6	180	2	A	
2	6	180	0.2	C	

Notes			

Analyzing the Split-Plot Design

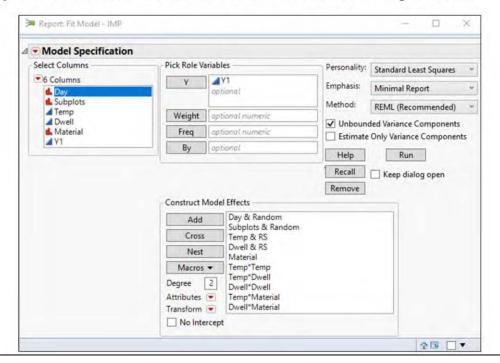
 For the Split-Plot or the Split-Split Plot design, click on the green triangle next to Model after entering data into the table.



Notes			

Analyzing the Split-Plot Design

- The Fit Model window will look a little different. Leave as is!
- · Click Run
- Analyze the residuals and remove terms as with other experiments



Notes			

12 Multiple Response Optimization

- Experiments may have more than one response variable
- · You can optimize each response separately . . .
- ... but you will get different answers for each response!

Notes			

It is not uncommon to have multiple response variables in a DOE. If you think you have just one, you might want to solicit feedback from one or more knowledgeable colleagues.	
In this section we introduce and illustrate the most widely used technique for joint optimization of multiple responses.	
Notes	
	_
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	—

Example 1: heat sealing process

- DOE Participant Files \ heat sealing 2.jmp
- Run the Model script
- · Response variables:
 - ✓ *Bond* (bond strength)
 - ✓ *Print* (higher-isbetter cosmetic quality rating)
- *Shift* is the only factor we can eliminate
- All other factors are significant for at least one response

Effect Tests									
Source	Nparm	DF	Sum of Squares	F Ratio	Prob > F				
Shift	1	1	3.578	0.8499	0.3671				
Temp(120,180)	1	1	1540.835	366.0070	<.0001*				
Press(50,150)	1	1	8.439	2.0046	0.1715				
Dwell(0.2,2)	1	1	1606.813	381.6793	<.0001*				
Temp*Temp	1	1	1363.630	323.9142	<.0001*				
Temp*Press	1	1	14.607	3.4697	0.0766				
Press*Press	1	1	1 385	0.3290	0.5724				

1

0.759

715.715 170.0096

0.1804

Dwell*Dwell Response Print

Temp*Dwell Press*Dwell

Response Bond

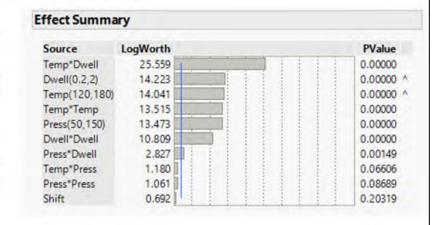
Effect Tests

Source	Nparm	DF	Sum of Squares	F Ratio	Prob > F
Shift	1	1	0.137812	1.7253	0.2032
Temp(120,180)	1	1	6.821113	85.3929	<.0001"
Press(50,150)	1	1	25.625986	320.8095	<.0001*
Dwell(0.2,2)	1	1	2.121674	26.5611	<.0001*
Temp*Temp	1	1	2.148242	26.8937	<.0001*
Temp*Press	1	1	0.300304	3.7595	0.0661
Press*Press	1	1	0.257674	3.2258	0.0869
Temp*Dwell	1	1	1.613751	20.2024	0.0002*
Press*Dwell	1	1	1.065140	13.3344	0.0015*
Dwell*Dwell	1	1	1.372401	17.1810	0.0005*

Notes			

Example 1 (cont'd)

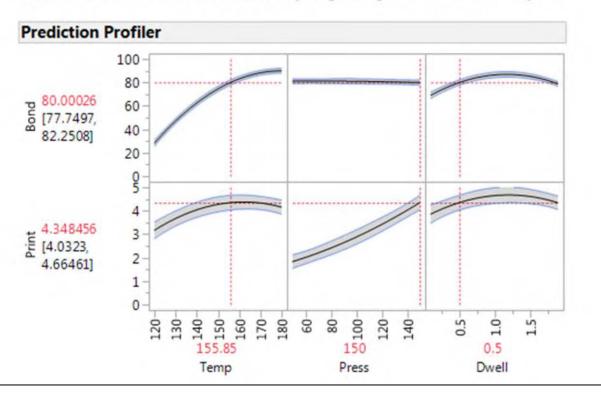
- The Effect Summary displays the lowest p-value from each of the response's Effects Tests
- This makes it easy to find terms to remove from the model
- Remove insignificant terms, as before, using the Effect Summary



Notes			

Example 1 (cont'd)

We want Bond = 80 and Print as large as possible. Here is a solution based on manually exploring the $Prediction\ Profiler$.



Notes			
·			

In this example is it easy to find solutions by manually exploring the *Prediction Profiler*.

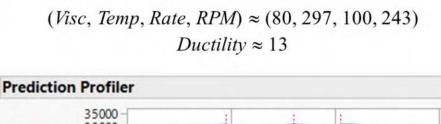
- ✓ Press should be set to 150, because this increases Print without significantly affecting Bond.
- ✓ The baseline value for *Dwell* was 1.0. Reducing this to 0.5 increases throughput while staying above the lowest feasible dwell time (0.2)
- ✓ Once these settings are in place, we can manipulate *Temp* to achieve something very close to 80 psi for *Bond*.

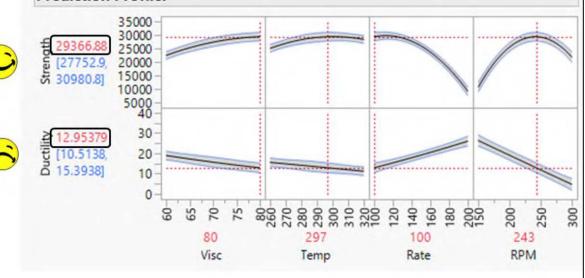
Joint optimization of response variables was not needed in this example. In most applications, however, manual optimization will not achieve the desired results. Extreme versions of this are illustrated in the next two examples.

Close the analysis window and the data table without saving.

Notes			

Example 2: extrusion process



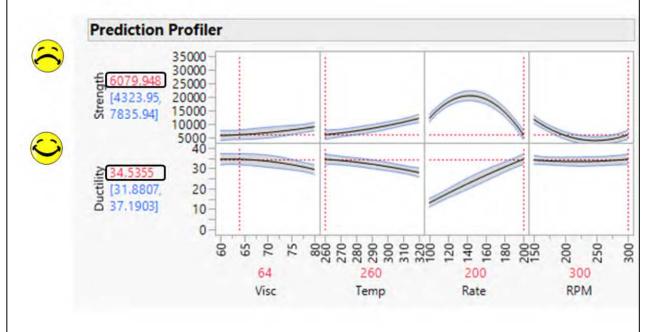


Data sets \ extrusion 2

Notes			

This example is based on data from an experiment to optimize the mechanical properties of an extruded plastic material. We want <i>Strength</i> to be as high as possible while maintaining a lower bound of 20 for <i>Ductility</i> . The solution for <i>Strength</i> (29367) shown above was found by visually exploring the <i>Prediction Profiler</i> . However, this approach resulted in an unacceptably low <i>Ductility</i>
마이트 아들은 아들이 얼마나 얼마나 아들이
(13).
Notes

(Visc, Temp, Rate, RPM) \approx (64, 260, 200, 300) Strength \approx 6080



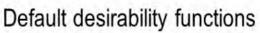
Notes			

The solution for <i>Ductility</i> (35) shown above was found by visually exploring the <i>Prediction Profiler</i> . However, this approach resulted in an unacceptably low <i>Strength</i> (6080).
NI-4
Notes

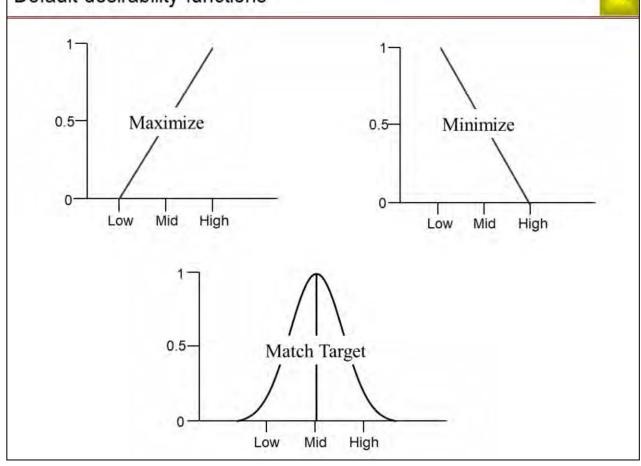
- Each response has a goal (minimize, maximize or target)
- · Define a "desirability function" for each response
- Combine the individual desirabilities into a single overall desirability function
- Maximize the overall desirability to jointly optimize all responses

Notes			

Notes 15
Desirability is a unitless quantity between 0 and 1, defined so that higher is better. JMF supplies default desirability functions based on the experimental data for your response variables. You must redefine the desirability functions so that they represent your objectives for each response variable.
You start by setting the general goal for each response: Maximize, Minimize or Match Target. Then you specify low, middle, and high data values to fine tune the shape of the desirability functions.
Notes







Notes			

Notes	160
The desirability function is increasing for <i>Maximize</i> responses and decreasing for <i>Minimize</i> responses. It is bell-shaped for <i>Match Target</i> responses.	
For <i>Minimize</i> responses with a lower bound of 0, it is a good idea to make the <i>Low</i> value equal to 0. Examples are number of defects, fraction defective, cycle time, standard deviation, cost of waste, etc.	
The low and high values for a <i>Match Target</i> response are used to define the allowable deviation from the target value.	ole
Notes	

The overall desirability function for the response variables (Y₁, Y₂, ···) is

$$\sqrt{(Y_1 \text{ desirability}) \times (Y_2 \text{ desirability}) \times \cdots}$$

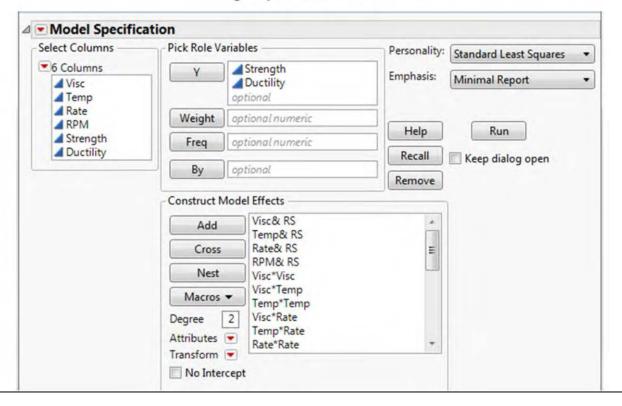
- It is the geometric mean of the desirability functions for all the individual response variables
- With a geometric mean, the overall desirability will be zero whenever any individual response desirability is zero

Notes			

Notes	102
A weighted geometric mean can be used. The weights (called <i>importance</i> in JMP) allow users to specify relative priorities for the responses. The higher the important the greater the influence the response has in determining the overall solution found the optimization algorithm.	ce,
The vast majority of users do not go into this level of detail.	
Notes	

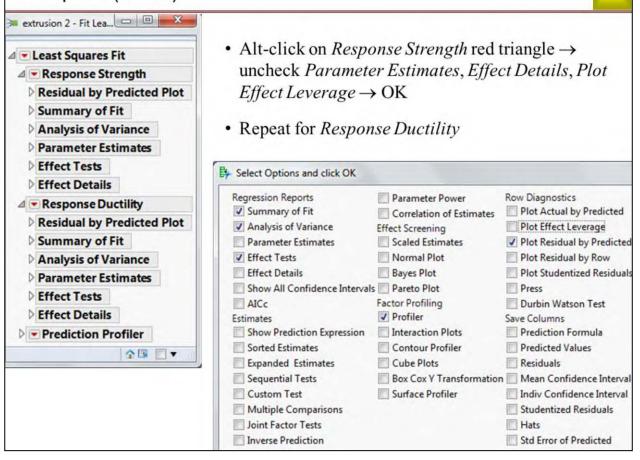
Example 2 (revisited)

DOE Participant Files \ extrusion 2.jmp \rightarrow Model script \rightarrow Model Specification \rightarrow Run



Notes			

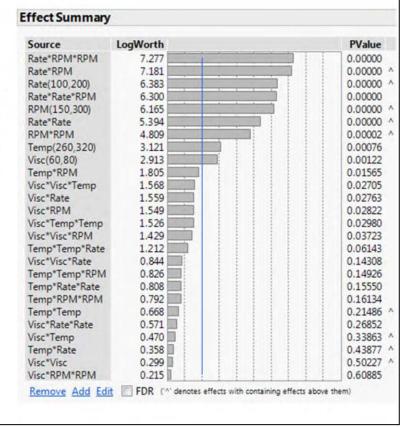
Example 2 (cont'd)



Notes			

"Pruning" the models

- The Effect Summary combines the P-values for all responses
- Removing terms here applies to the Effects Tests for one or more responses
- The usual threshold is P > 0.15



Notes				

Source

Visc(60,80)

Temp(260,320)

Rate(100,200)

RPM(150,300)

Visc*Rate

Rate*Rate

Visc*RPM

Temp*RPM

Rate*RPM

RPM*RPM

Visc*Visc*Temp

Visc*Visc*Rate

Visc*Visc*RPM

Visc*Temp*Temp

Temp*Temp*Rate

Temp*Temp*RPM

Temp*Rate*Rate

Rate*Rate*RPM

Rate*RPM*RPM

0.1001

0.0116*

0.0140*

0.0635

0.0577

0.0844

<.0001"

<.0001"

Prob > F

<.0001*

0.0001*

0.0003*

0.0005*

0.4624

0.8364

0.5440

0.7358

<.0001*

0.4084

0.0527

0.8994

0.8700

0.8114

0.9857

0.3483

0.3080

0.9424

0.5257

Visc*Visc*Rate

Visc*Visc*RPM

Visc*Temp*Temp

Temp*Temp*Rate

Temp*Temp*RPM

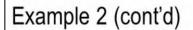
Temp*Rate*Rate

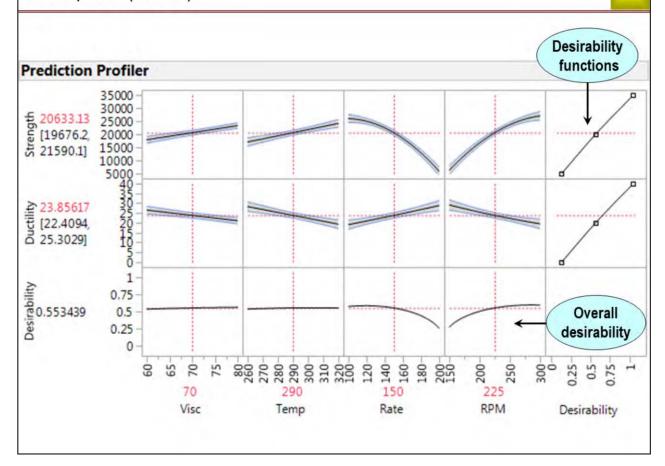
Rate*Rate*RPM

Rate*RPM*RPM

Effect Summary PValue LogWorth Source Rate*RPM*RPM 11.346 0.00000 Rate*RPM 10.339 0.00000 Rate*Rate*RPM 10.023 0.00000 Rate(100,200) 9.762 0.00000 RPM(150,300) 9.741 0.00000 Rate*Rate 8.273 0.00000 RPM*RPM 7.572 0.00000 Visc(60,80) 6.093 0.00000 Temp(260,320) 4.727 0.00002 Temp*RPM 2.347 0.00449 Visc*RPM 2.138 0.00727 Visc*Visc*RPM 1.935 0.01163 Effect Tests for Strength **Effect Tests for Ductility** Visc*Temp*Temp 1.853 0.01404 Prob > F Source Visc*Rate 1.815 0.01531 <.0001* Visc(60,80) Visc*Visc*Temp 1.499 0.03171 <.0001* Temp*Temp*RPM Temp(260,320) 1.238 0.05774 <,0001* Temp*Temp*Rate 1.197 Rate(100,200) 0.06350 <.0001* Temp*Rate*Rate 1.074 0.08435 RPM(150,300) 0.0153* Visc*Visc*Rate 1.000 0.10006 Visc*Rate <.0001* Rate*Rate 0.0073* Visc*RPM 0.0045* Temp*RPM <.0001* Rate*RPM <.0001* RPM*RPM 0.0317* Visc*Visc*Temp

Notes			

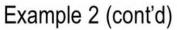




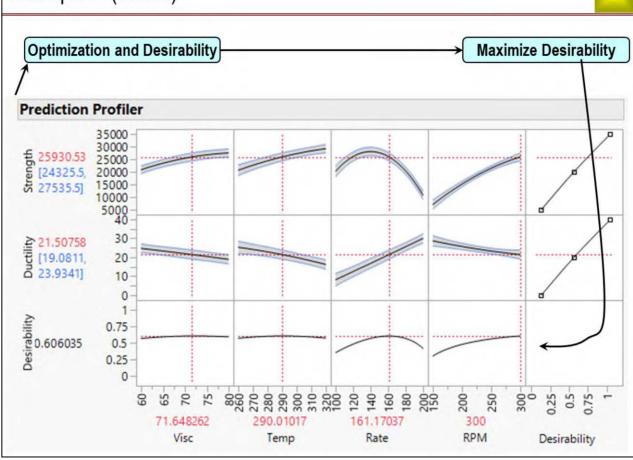
Notes			

Notes
Here is the default <i>Prediction Profiler</i> for the four-factor extrusion experiment. The individual desirability functions are shown in the right-most column. In this case they are both increasing functions because our general objective for both responses is <i>Maximize</i> .
The overall desirability is a function of the experimental factors, and is shown in the bottom row. By default, it is the unweighted geometric mean of the individual desirability functions.

Notes			







Notes			

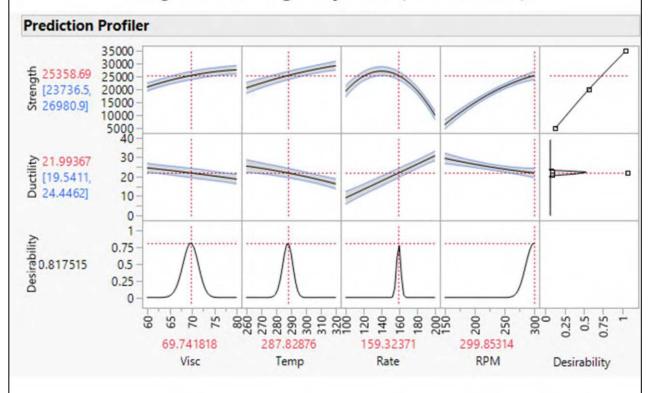
Notes	170
Shown above is the <i>Prediction Profiler</i> after selecting <i>Maximize Desirability</i> from red triangle menu. We have increased average <i>Strength</i> to 25930, and decreased average <i>Ductility</i> to 21.5.	the
Notes	

Notes			



Example 2 (cont'd)

Using a Match Target objective (see next slide)

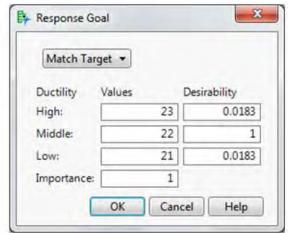


Notes			

To obtain the results shown above, double-click in the individual *Desirability* pane (on the right) for *Ductility*. Change the specifications as shown below, click OK, run *Maximize Desirability* again.

Predicted average *Strength* is now 25359, predicted average *Ductility* is 22.

The 95% confidence interval is (19.5, 24.4). This is an improvement over the previous confidence interval (19.0, 24.0), which would have allowed *Ductility* to vary a little further below 20.



Note: Due to the iterative process used in the prediction profiler, results may vary slightly from what's shown in the above slide.

Least Squares Fit red triangle \rightarrow Save Script \rightarrow To Data Table \rightarrow Save Script As \rightarrow Name: Fit Least Squares \rightarrow OK.

Notes			

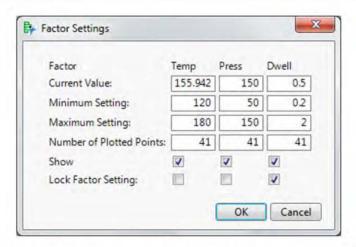
Exercise 12.1

- (a) DOE Participant Files \ heat sealing 2. Run the model script. Use the Effect Summary to remove model terms with P > 0.15.
- (b) Go to the Prediction Profiler. Our target for average Bond is 80, with a tolerance of ±5. The highest possible value for average Print is 5. Average Print must exceed 4. Modify the desirability functions for Bond and Print accordingly. Click Prediction Profiler red triangle → Optimization and Desirability → Save Desirabilities.
- (c) Click Prediction Profiler red triangle → Optimization and Desirability → Maximize Desirability.
- d) The Production Manager is unhappy with our solution. It achieves excellent bond strength (80) and print quality (4.8), but the proposed increase in dwell time would reduce throughput from 300 to 50 bags per minute!

To look for a compromise, select *Reset Factor Grid* on the *Prediction Profiler* red triangle. We want to hold *Dwell* at a low value, say 0.5. Type 0.5 for *Current Value*, check the *Lock Factor Setting* box, then click OK. The vertical line on the *Dwell* profile should now be solid.

Notes			

Exercise 12.1 (cont'd)



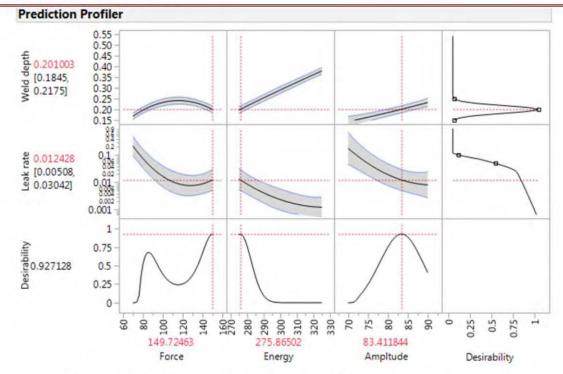
- e) Run Maximize Desirability again. The optimal factor settings are shown in the Current Value row. The response averages are 80.08 for Bond and 4.35 for Print.
- f) Save your script, close and save the data table.

Notes			

a)	Assembly of inkjet print cartridges includes an ultrasonic welding operation with X variables Force, Energy, Amplitude, and Cavity (identifies the tool cavity in which each plastic cartridge was molded). The response variables are Weld depth and Leak rate.	
b)	DOE Participant Files \ ultrasonic welding 2. Run the model script. Use a Log transformation for Leak rate. Use Effect Summary to prune the models.	
c)	Go to the <i>Prediction Profiler</i> . The target for average <i>Weld depth</i> is 0.20, with a tolerance of \pm 0.05. The lowest possible value for average <i>Leak rate</i> is 0. We require mean <i>Leak Rate</i> to be no larger than 0.10.	
d)	Modify the desirability functions for Weld depth and Leak rate accordingly. Click Prediction Profiler red triangle \rightarrow Optimization and Desirability \rightarrow Save Desirabilities.	
e)	Click Prediction Profiler red triangle → Optimization and Desirability → Maximize Desirability. See next slide.	
		_

Notes			

Exercise 12.2 (cont'd)



- f) Least Squares Fit \rightarrow Save Script \rightarrow To Data Table \rightarrow Name: Fit Least Squares \rightarrow OK
- g) Save data table.

Notes			

Exercise 12.3 (Homework)

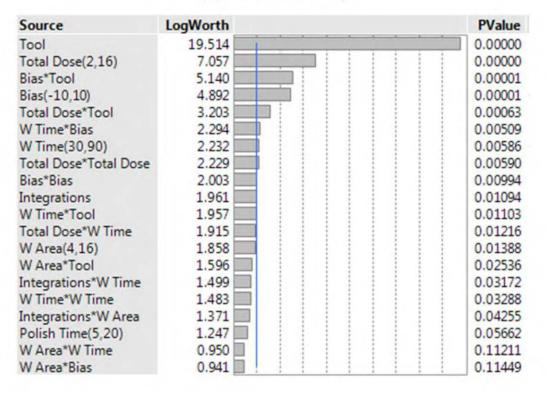
f) Save your script, close and save the data table.

a)	DOE Participant Files \ electron microscope. Run the Model script. In this case, it will take you directly to the Model Dialog. Apply Log transformations to all 4 response variables, then run the model.
b)	Click Least Squares Fit red triangle \rightarrow Effect Summary \rightarrow prune the models. See slide below.
c)	Go to the <i>Prediction Profiler</i> . We want to minimize all 4 responses. Use the same desirability functions for all 4 responses: High = 2, Middle = 1, Low = 0. Click <i>Prediction Profiler</i> red triangle \rightarrow <i>Optimization and Desirability</i> \rightarrow <i>Save Desirabilities</i> .
d)	Click Prediction Profiler red triangle \rightarrow Reset Factor Grid \rightarrow Factor Settings \rightarrow click the Lock Factor Setting box under Tool \rightarrow OK. See next page.
e)	Run Maximize Desirability separately for each Tool (A, B, C). Give the average values of the 4 responses for each tool. See next page.

Notes			

Exercise 12.3 (cont'd)

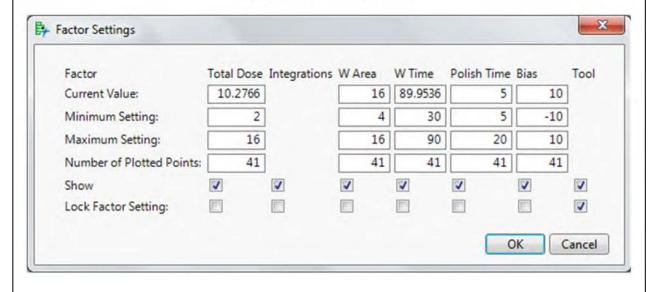
(b) Effect Summary



Notes			

Exercise 12.3 (cont'd)

(d) Reset Factor Grid



Notes			

Exercise 12.3 (cont'd)

(e) Average responses by tool

Tool	S-Height	S-Width	D-Height	D-Width
A	1.33	1.13	1.10	0.95
В	1.41	0.76	1.36	1.08
С	1.48	1.32	1.94	1.57

Notes			

13 Screening Experiments

Optimization	Screening
Smaller number of factors	Larger number of factors
Main and interactive effects	Main and interactive effects if categorical factors at only 2-levels; otherwise main effects only
Quantitative factors have 3 levels	All factors have 2 levels (usually)
Identify the best factor levels	Identify the "active" factors

Notes			

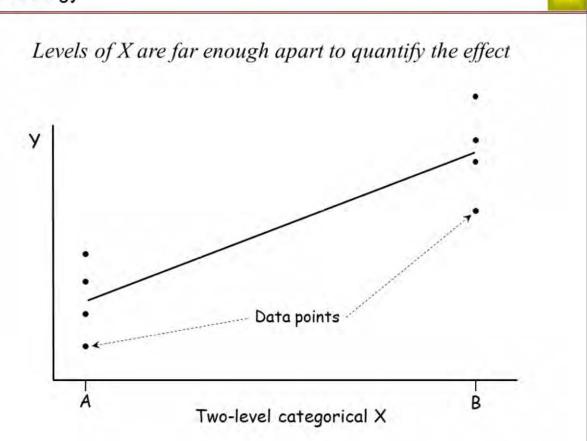
About screening experiments

- · They are usually conducted early in the process of optimization
- They involve a relatively large number of factors
- Their objective is to identify a smaller set of influential factors for further experimentation
- It is likely that many factors considered have little or no effect on the response (sparsity-of-effects)
- They use the smallest feasible design for the given number of factors saves time and money
- They are based on main-effect models, although with some designs, factors with interactions and quadratic effects can be identified
- They usually consist of factors at only two levels
- · They rank the factors by the size of their estimated effects

Notes			



Bold strategy



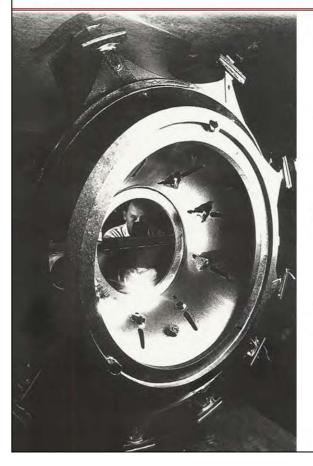
Notes			

Not bold enough

Levels of X are too close to quantify the effect В Two-level categorical X

Notes			

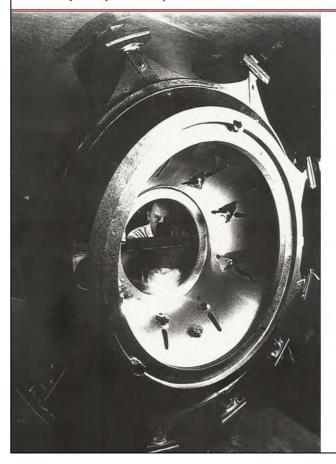
Example



- Titanium castings → strong & light
- Ti develops surface oxidation during the cooling phase
- Large Ti castings were failing the customer O₂ requirement
- Analysis of file cabinet data yielded no significant correlations

Notes			

Example (cont'd)



Black Belt

"We should brainstorm factors for a DOE."

Plant manager

"We can't experiment with such an expensive part!"

Ti metallurgist

"The problem doesn't replicate on smaller parts."

Part engineer

"What have got to lose? It's been weeks since we shipped any of these!"

<u>Notes</u>			

Example (cont'd)

Process area	Factor	Levels	Current state X variable	Possible future state solution
	Slurry	Batch 1 vs Batch 2	✓	
ci u di	# Dips	14 vs 18		1
Shell making	Bake time	6 hrs vs 48 hrs	~	
	Bake temp	1950° vs 2050°		1
	Alloy cost	Low vs High		✓
Continu	Alloy status	New vs Revert	1	
Casting	Heat shield	Mild vs Stainless		✓
	Fan speed	2400 vs 3200		✓

Notes			

Above is the list that emerged from the brainstorming session.

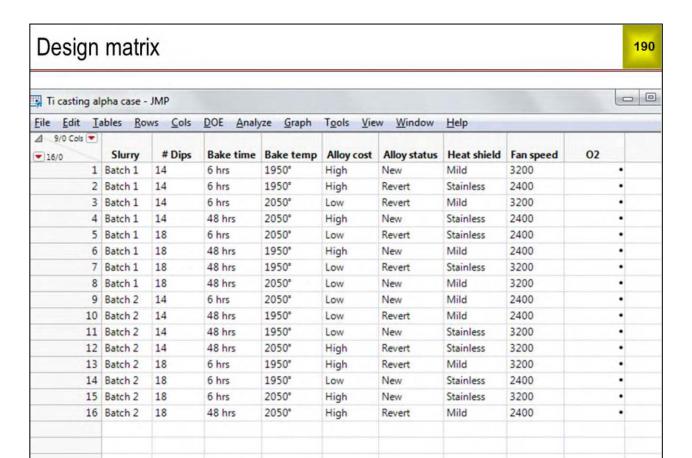
- Three of the factors are variables in the current state.
- The other five are possible improvement ideas for the future state.
- · Total: 8 factors
- Plant manager agreed to 16 castings
- All factors are at two levels

Notes			

Steps in creating a Screening Design

- 1) $DOE \rightarrow Classical \rightarrow Two Level Screening \rightarrow Screening Design$
- 2) Responses \rightarrow Response Name \rightarrow O2 \rightarrow Goal \rightarrow Minimize
- Factors → Add all factors as in previous designs (continuous or categorical, number of levels for categorical)
- 4) Enter factor names and levels from the table on the previous page ightarrow Continue
- 5) Choose Screening Type → Construct a main effects screening design → Continue → Make Design → Make Table
- 6) (The matrix below has been sorted by Slurry, # Dips, Bake time and Bake temp)
- 7) Save as Ti casting alpha case

Notes			

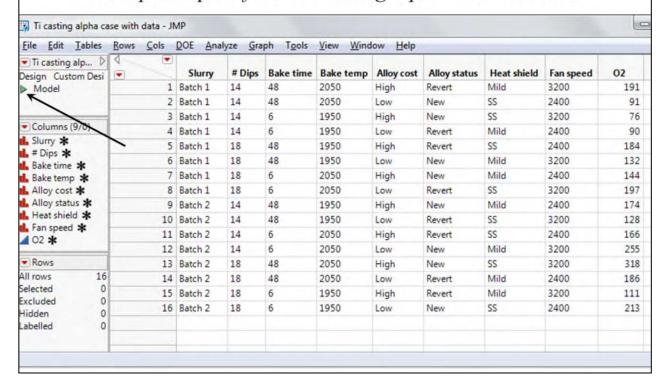


Notes			

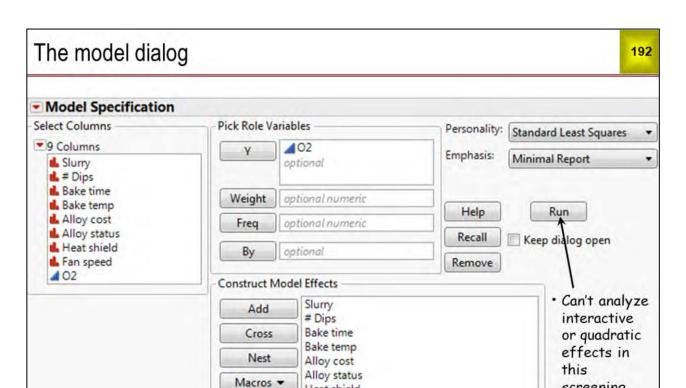
Analyzing the Screening Experiment . . .

... two months (and many sleepless nights) later...

DOE participant files \ Ti casting alpha case with data



Notes			



Heat shield Fan speed

Degree Attributes 💌

Transform 💌

No Intercept

screening

experiment

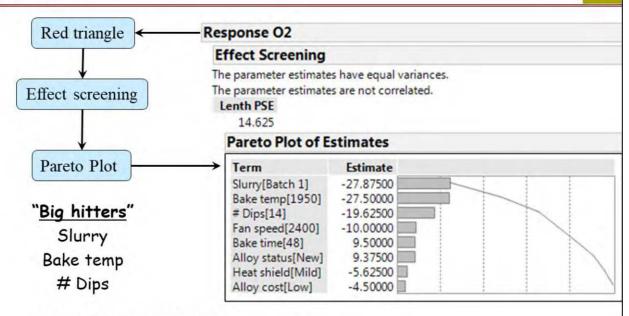
· Just click on

☆ □ ▼

Run

Notes			

Analysis



- Slurry is a variable in the current state
- ullet The O_2 values for castings made from Batch 1 shells were much lower than those from Batch 2
- The operators did not report any differences in the make-up of the two batches

Notes			

Notes 194
To interpret screening experiments, use the <i>Effects Screening</i> analysis element as shown above. It shows showing the relative magnitude of the factor effects. The idea is to use the factors with the largest effects in a subsequent optimization experiment.
The interactive and quadratic effects are left out of the model. This biases the signal-to-noise ratios downward. The P-values are not to be trusted, so factors appear less significant than they really are.

Notes			

Notes			

- They changed Bake temp to 1950 and # Dips to 14 (easy)
- The problem immediately went away
- 13 of the 16 DOE castings were good to ship as is
- · Only 1 eventually scrapped
- · Worst-case annual cost avoidance: \$20.8M
- · No immediate follow-up

Notes		

 Investigation of the slurry effect eventually lead to the root cause of the problem

- → The density of the ceramic powder used to make the shell had increased over time, resulting in heavier shells
- → The increase had been noted, but no action was taken because the densities were still within spec limits
- → At the time, shell weights were not monitored
- · Why no significant correlations in the "file cabinet" data?
 - ightarrow The O_2 data in the engineering database was post rework rather than first pass

Notes		

Notes			

Exercise 13.1

a)	Create a standard screening design matrix for the 10 factors shown below.
	Note: A sample size of 16 would have been adequate, but the project team
	decided to use a sample size of 24.

b) Save the table of factors for use in the next exercise:

Click the red triangle next to Screening Design > Save Factors (table opens)

File > Save as... > extrusion design factors

- c) Save your design matrix as extrusion design 1.jmp.
- d) DOE Participant Files \ extrusion 0 with data.jmp. Analyze the data as shown for standard screening designs.
- e) Based on the results for *Strength* and *Ductility*, find the best set of 4 factors for a subsequent optimization experiment.

Notes			

Factors	Feasible ranges
Polymer variables	
Smoother	0.0 to 0.5
Filler	2.0 to 4.0
Viscosity	60 to 80
Moisture	0.1 to 0.25
Process variables	
Zone 1 temp	260 to 320
Zone 2 temp	260 to 320
Zone 3 temp	260 to 320
Zone 4 temp	260 to 320
Rate	100 to 200
RPM	150 to 300

Responses are Strength and Ductility of the extrusions

Notes			

Another way to analyze

The experiment in the previous example was conducted years ago. JMP can now analyze this experiment differently, giving more information!

The O2 experiment can be analyzed using JMP's Fit Two Level Screening

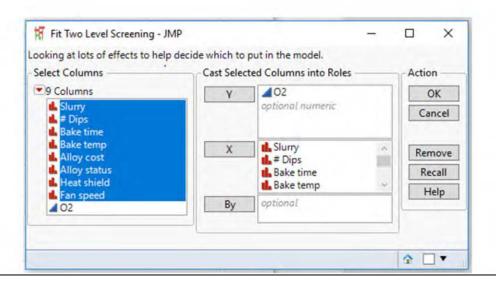
- · Requirement for this type of analysis: All factors are at 2 levels
- · Reports and interpretation are very different
- · Based on the assertion that relatively few of the effects are active
- · Most are inactive (insignificant), meaning their effects are negligible
- Often, in screening experiments, there are no degrees of freedom for error
- Estimates of inactive effects are used to estimate random error in this analysis
- · Some information can be gained about 2-factor interactions
- · 2-Factor interactions are aliased with each other

Notes		

Fit Two Level Screening

DOE participant files \ Ti casting alpha case with data

- DOE > Classical > Two Level Screening > Fit Two Level Screening
- Set up as shown (all factors are cast into X)
- · Click OK



Notes			

Below is the Contrasts report:

- Contrast column shows the regression parameter estimate
 - o An asterisk shows estimate is not the same as the regression estimate
 - o An asterisk would indicate that we need to use the Fit Model platform
 - There are no asterisks in this report
- · Individual p-Values indicate significant effects
- Bar Chart shows terms significant at the 0.10 level
- Analysis may not be exactly the same if re-run, due to the analysis process
- Note that there is an interaction that is significant!
 - We cannot tell if the significant interaction is Bake temp*Fan speed
 - It could be any of the interactions under Aliases
 - The estimate of the effect (Contrast) is actually the sum of all of the aliased interactions
 - o This is because this is a screening design
 - o Additional experimentation is needed determine the active interaction

Notes		

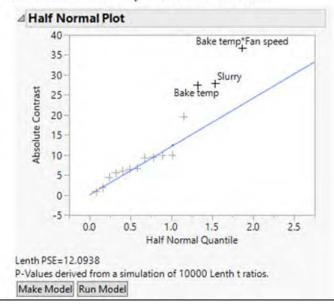
Contrasts report

Term	Contrast	Lenth t-Ratio		Simultaneous p-Value	
Slurry	27.8750	2.30	0.0415*	0.3224	
Bake temp	27.5000	2.27		0.3370	
# Dips	19.6250	1.62	0.1126	0.7222	
Fan speed	10.0000	0.83	0.3818	1.0000	
Bake time	9.5000	0.79	0.4068	1.0000	
Alloy status	-9.3750	-0.78	0.4133	1.0000	
Heat shield	5.6250	0.47	0.6697	1.0000	
Alloy cost	4.5000	0.37	0.7320	1.0000	
Slurry*Bake temp	9.8750	0.82	0.3882	1.0000	# Dips*Bake time, Fan speed*Alloy status, Heat shield*Alloy cost
Slurry*# Dips	-6.5000	-0.54	0.6237	1.0000	Bake temp*Bake time, Alloy status*Heat shield, Fan speed*Alloy cos
Bake temp*# Dips	-1.8750	-0.16	0.8871	1.0000	Slurry*Bake time, Fan speed*Heat shield, Alloy status*Alloy cost
Slurry*Fan speed	-0.8750	-0.07	0.9474	1.0000	Bake temp"Alloy status, Bake time"Heat shield, # Dips"Alloy cost
Bake temp*Fan speed	36.7500	3.04	0.01901	0.1617	Slurry*Alloy status, # Dips*Heat shield, Bake time*Alloy cost
# Dips*Fan speed	-6.1250	-0.51	0.6434	1.0000	Bake time"Alloy status, Bake temp"Heat shield, Slurry"Alloy cost
Fan speed*Bake time	6.7500	0.56	0.6115	1.0000	# Dips*Alloy status, Slurry*Heat shield, Bake temp*Alloy cost

Notes			

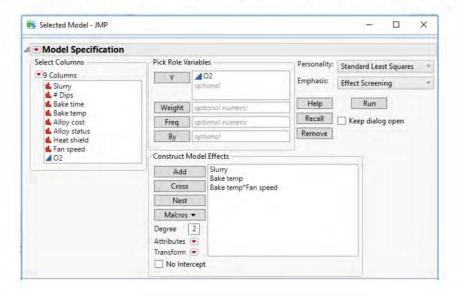
The Half Normal Plot graphically identifies significant effects

- · Significant effects or terms fall off (away from) the blue line
 - · The additional point off the line is # Dips, which was near the cut-off
 - · Here, it appears to be significant
 - · One could choose to carry this term forward



Notes			
			_

- Click Make Model
- · Fit Model window will come up
 - o Significant terms have been carried forward
 - o Terms can be added to the model
 - o # Dips could be added (probably should be, based on Half Normal Plot)

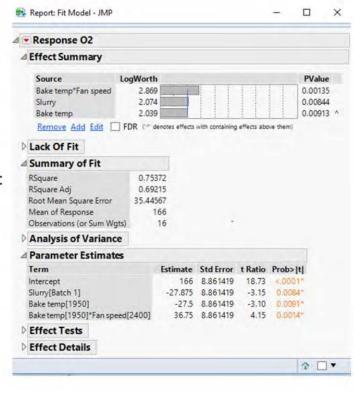


Notes			

- This familiar report comes up
- This analysis got us further

Click Run

- Presence of interaction
- o Need higher level terms
- Additional experimentation to:
 - Determine interaction
 - Optimize



Notes			

Definitive Screening Design

A Definitive Screening Design is a very effective screening design

- Factors must be either continuous or two-level categorical
- It can be a good alternative to a Custom Design when six or more factors

"A minimum run-size DSD is capable of correctly identifying active terms with high probability if the number of active effects is less than about half the number of runs and if the <u>effects sizes exceed twice the standard deviation</u>. However, by augmenting a minimum run-size DSD with four or more properly selected runs, you can identify substantially more effects with high probability. . . . Extra Runs substantially increase the design's ability to detect second-order effects."

--From JMP's Overview of the Fit Definitive Screening Platform

"Effect sizes exceed twice the standard deviation" $\Rightarrow \frac{b_n}{\sigma} \ge 1$,

which means that the difference between the average response at the high level and at the low level is 2σ, or 2 * std dev. (Remember, the coefficient is the effect/2.)

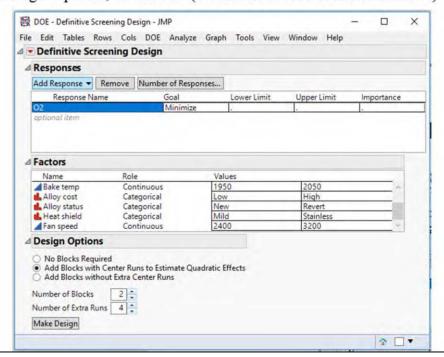
"Second order effects" include 2-level interactions and quadratic terms.

Notes			

Example

Using the same situation as in the previous example:

- · Enter response and factors, as usual
- Set up Design Options, as shown. (4 Extra Runs are recommended!!!)



Notes			

Example (cont'd)

This Definitive Screening Design requires 22 runs

- · In the previous example, only 16 runs were required
- · However, a follow-on optimization experiment was needed

The Definitive Screening can be run, then augmented, if needed

· This requires many fewer runs (and other resources) overall

1			# 0:							03
*	Block	Slurry	and the second second second		Andrew Control of the	The second second second	Alloy status		and the second second second second	02
1	1	No. of Concession,	18	27		High	Revert	Stainless	2800	
2	1	Batch 2		6	2050	Low	Revert	Stainless	2800	
3	1	Batch 1	18	6	1950	Low	New	Stainless	3200	
4	1	Batch 2	18	48	1950	Low	New	Stainless	3200	
5	1	Batch 1	14	6	2050	High	Revert	Mild	2400	
6	1	Batch 1	14	48	2050	High	New	Stainless	3200	
7	1	Batch 1	18	48	1950	High	New	Mild	2800	
8	1	Batch 2	18	. 27	2050	High	Revert	Stainless	3200	
9	1	Batch 1	14	27	2000	Low	New	Mild	2800	
10	1	Batch 2	14	48	2050	High	Revert	Mild	2400	
11	1	Batch 2	18	6	1950	Low	Revert	Mild	2400	
12	1	Batch 1	14	27	1950	Low	New	Mild	2400	
13	2	Batch 2	18	48	2050	Low	New	Stainless	2400	
14	2	Batch 1	18	6	2050	Low	New	Stainless	2400	
15	2	Batch 2	18	48	1950	High	Revert	Stainless	2400	
16	2	Batch 1	18	48	2050	Low	Revert	Mild	3200	
17	2	Batch 1	14	6	1950	High	Revert	Mild	3200	
18	2	Batch 1	14	6	2050	Low	New	Mild	3200	
19	2	Batch 2	14	48	1950	High	Revert	Mild	3200	
20	2	Batch 2	14	6	1950	High	New	Stainless	2400	
21	2	Batch 1	14	48			Revert	Stainless	2400	
22	2		18	6		High	New	Mild	3200	

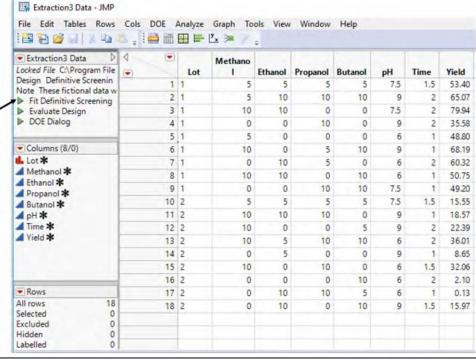
Notes			

Analyzing the Definitive Screening Design

When you create a Definitive Screening Design in JMP, the Table will contain a script for analysis

Help > Sample Data Library Design Experiment / Extraction 3 Data

- Run the experiment
- Enter data into the table
- Click on the green triangle to analyze the data (run the script)
- You must use
 Fit Definitive
 Screening for
 the analysis, to
 take advantage
 of the design
 structure



Notes			

Analyzing the Definitive Screening Design (cont'd)

- JMP does all the work:
 - Stage 1 tests Main Effects
 - Stage 2 tests interactions and quadratic terms of significant Main Effects
 - o Combined Model includes both

Term		Estimate	Std Error	t Ratio	Prob> t
ntercept		34.568	1.0452	33.074	<.0001*
Lot[1]		17.197	0.6023	28.552	<.0001*
Methanol		9.7133	0.4281	22.691	<.0001*
Ethanol		2.3166	0.4281	5.4118	0.0010*
Time		4.0798	0.4281	9.5307	<.0001*
Methanol	*Ethanol	-0.367	0.5534	-0.663	0.5287
Methanol	*Time	0.5266	0.5534	0.9516	0.3730
Ethanol*T	ime	9.8258	0.6627	14.828	<.0001*
Methanol	*Methanol	7.637	1.1581	6.5945	0.0003*
Ethanol*E	thanol	-1.449	1.1469	-1.264	0.2468
Time*Time	e	-3.297	1.1469	-2.875	0.0238*
Statistic	Value				
RMSE	1.6017				
DF	7				

Stage 1	- Main E	ffect Esti	mates	
Term	Estimate	Std Error	t Ratio	Prob> t
Methanol	9.7133	0.3674	26.438	<.0001*
Ethanol	2.3166	0.3674	6.3055	0.0015*
Time	4.0798	0.3674	11,104	0.0001*
Statistic	Value			
RMSE	1.3747			
DF	5			

Stage 2	- Even O	ruer Erre	ect Estima	ates	
Term		Estimate	Std Error	t Ratio	Prob> t
Intercept		34.568	1.3459	25.683	0.0015*
Lot[1]		17.197	0.7757	22.171	0.0020*
Methanol	*Ethanol	-0.367	0.7127	-0.515	0.6581
Methanol	*Time	0.5266	0.7127	0.7389	0.5369
Ethanol*T	ime	9.8258	0.8534	11.514	0.0075*
Methanol	*Methanol	7.637	1.4914	5.1208	0.0361*
Ethanol*E	thanol	-1.449	1.477	-0.981	0.4299
Time*Time	e	-3.297	1.477	-2.232	0.1552
Statistic	Value				
RMSE	2.0626				
DF	2				

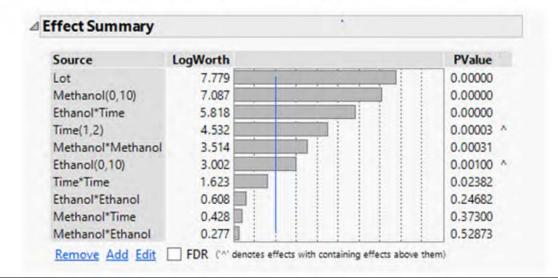
- Click Run Model

Notes			

Analyzing the Definitive Screening Design (cont'd)

A familiar report comes up

- · Proceed as before: Check residuals and remove insignificant terms
- · Note that interactions and quadratic terms are estimated!
- · This is what is meant by Definitive Screening
- · In this case, an additional optimization experiment is not necessary!



Notes			

Full Factorial vs. Definitive Screening Design (not randomized)

Full Factorial Design with 4 Center Runs:

X1	X2	Х3	X4	Y
-1	-1	-1	-1	
-1	-1	-1	1	
-1	-1	1	-1	
-1	-1	1	1	
-1	1	-1	-1	
-1	1	-1	1	
-1	1	1	-1	
-1	1	1	1	
1	-1	-1	-1	
1	-1	-1	1	
1	-1	1	-1	
1	-1	1	1	
1	1	-1	-1	
1	1	-1	1	
1	1	1	-1	
1	1	1	1	
0	0	0	0	
0	0	0	0	
0	0	0	0	
0	0	0	0	

Definitive Screening Design with 4 Extra Runs and 2 Center Runs:

Y	X6	X5	X4	X3	X2	X1
- 19	1	1	1	1	1	0
	-1	-1	-1	-1	-1	0
	1	-1	1	1	0	1
	-1	1	-1	-1	0	-1
	-1	1	1	0	-1	1
	1	-1	-1	0	1	-1
	1	1	0	-1	-1	1
	-1	-1	0	1	1	-1
	1	0	-1	-1	1	1
	-1	0	1	1	-1	-1
	0	-1	-1	1	-1	1
	0	1	1	-1	1	-1
	-1	-1	1	-1	1	1
	1	1	-1	1	-1	-1
	-1	1	-1	1	1	1
1.4	1	-1	1	-1	-1	-1
	0	0	0	0	0	0
	0	0	0	0	0	0

Note the structural differences in these two classes of designs.

<u>Notes</u>			

Exercise 13.2

Using the same factors and levels as Exercise 20.1, create a Definitive Screening Design.

- · When you are ready to enter the factors:
 - ➤ Click the red triangle next to Definitive Screening Design > Load Factors (select the file extrusion design factors saved during Exercise 20.1)
- · Be sure to add the recommended 4 runs!
- The previous experiment required 16 runs, but they used 24 runs. Further
 experimentation would be needed with that screening design.
- · How many runs does this Definitive Screening Design require?

Notes			

Factors	Feasible ranges
Polymer variables	
Smoother	0.0 to 0.5
Filler	2.0 to 4.0
Viscosity	60 to 80
Moisture	0.1 to 0.25
Process variables	
Zone 1 temp	260 to 320
Zone 2 temp	260 to 320
Zone 3 temp	260 to 320
Zone 4 temp	260 to 320
Rate	100 to 200
RPM	150 to 300

Responses are Strength and Ductility of the extrusions

Notes			